

# A High-Spin Journey with Robert

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*Daryl Hartley*  
*U.S. Naval Academy*

*The views expressed in this talk are those of the authors and do not reflect the official policy or position of the US Naval Academy, Department of the Navy, Department of Defense, or the US Government*



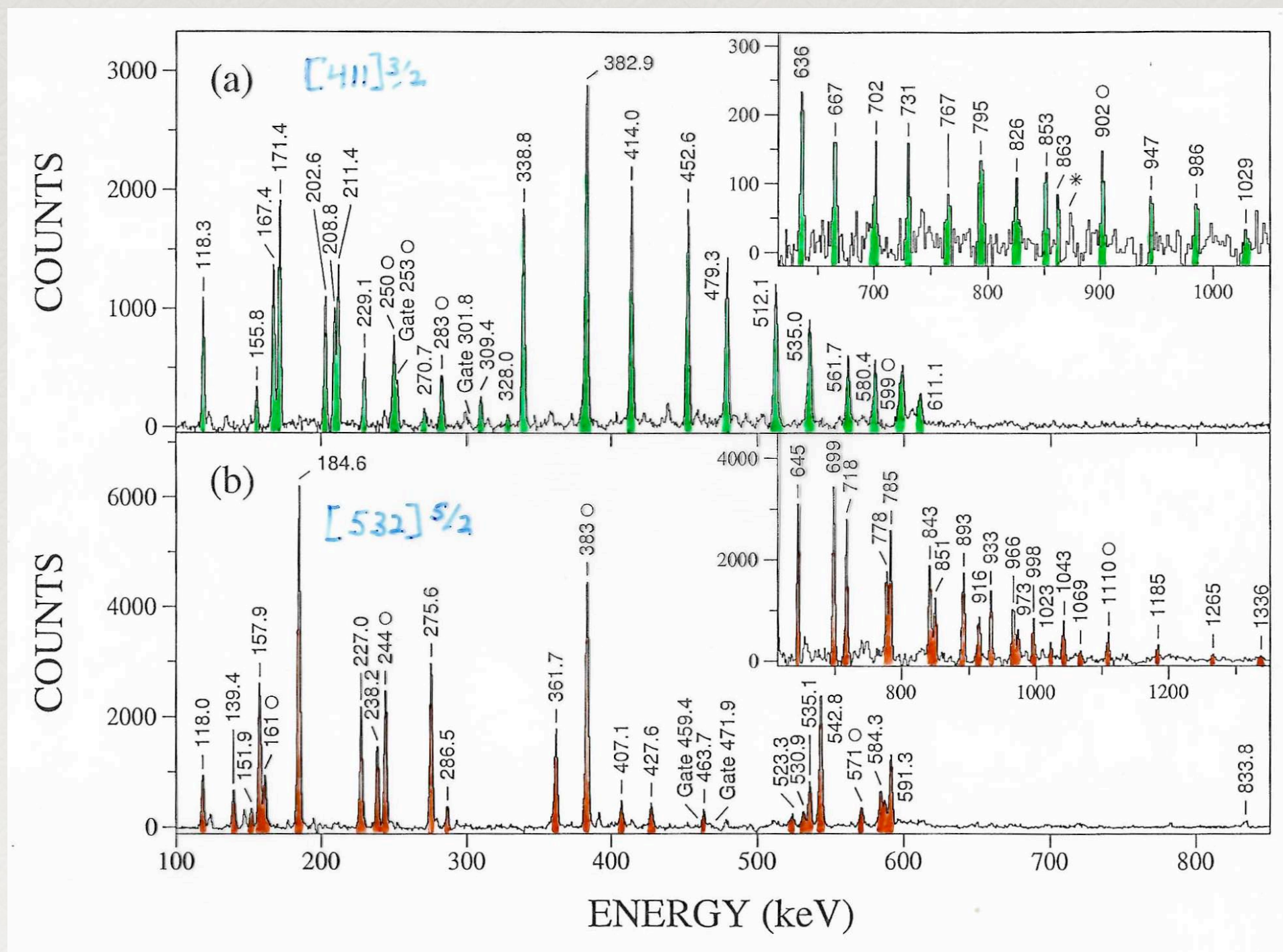
# In the beginning (for me)...

- *First met in Tallahassee, circa 1995*
- *Robert taught me a thing or two about properly setting up a Compton-Suppressed system (in less than 2 minutes)*





# In the beginning (for me)...



PHYSICAL REVIEW C

VOLUME 58, NUMBER 5

NOVEMBER 1998

## High-spin structures in $^{155}\text{Tb}$ and signature splitting systematics of the $\pi h_{11/2}$ bands in odd $A \approx 160$ nuclei

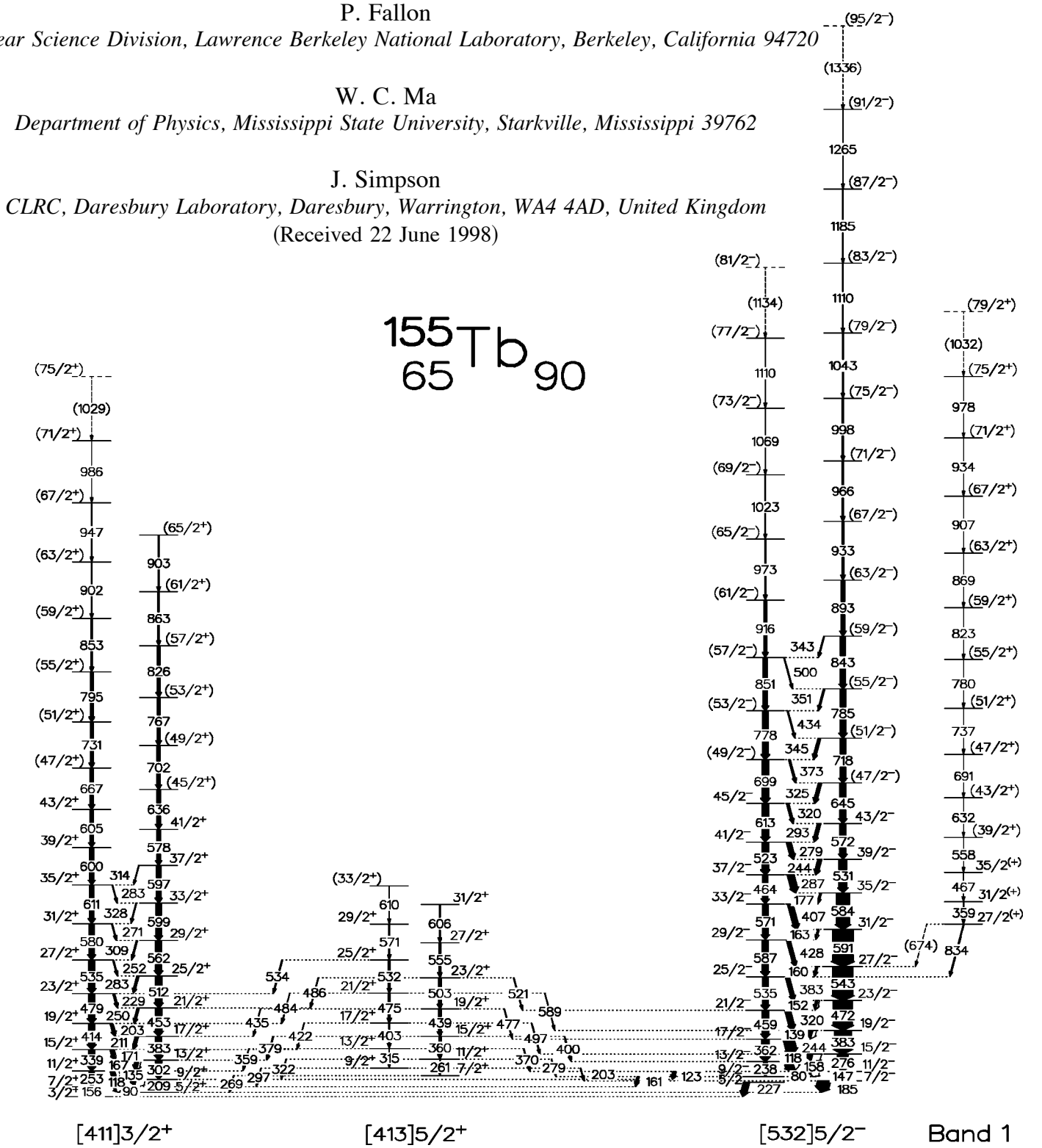
D. J. Hartley,\* T. B. Brown, F. G. Kondev, J. Pfohl, and M. A. Riley  
*Department of Physics, Florida State University, Tallahassee, Florida 32306*

S. M. Fischer, R. V. F. Janssens, and D. T. Nisius  
*Argonne National Laboratory, Argonne, Illinois 60439*

P. Fallon  
*Nuclear Science Division, Lawrence Berkeley National Laboratory, Berkeley, California 94720*

W. C. Ma  
*Department of Physics, Mississippi State University, Starkville, Mississippi 39762*

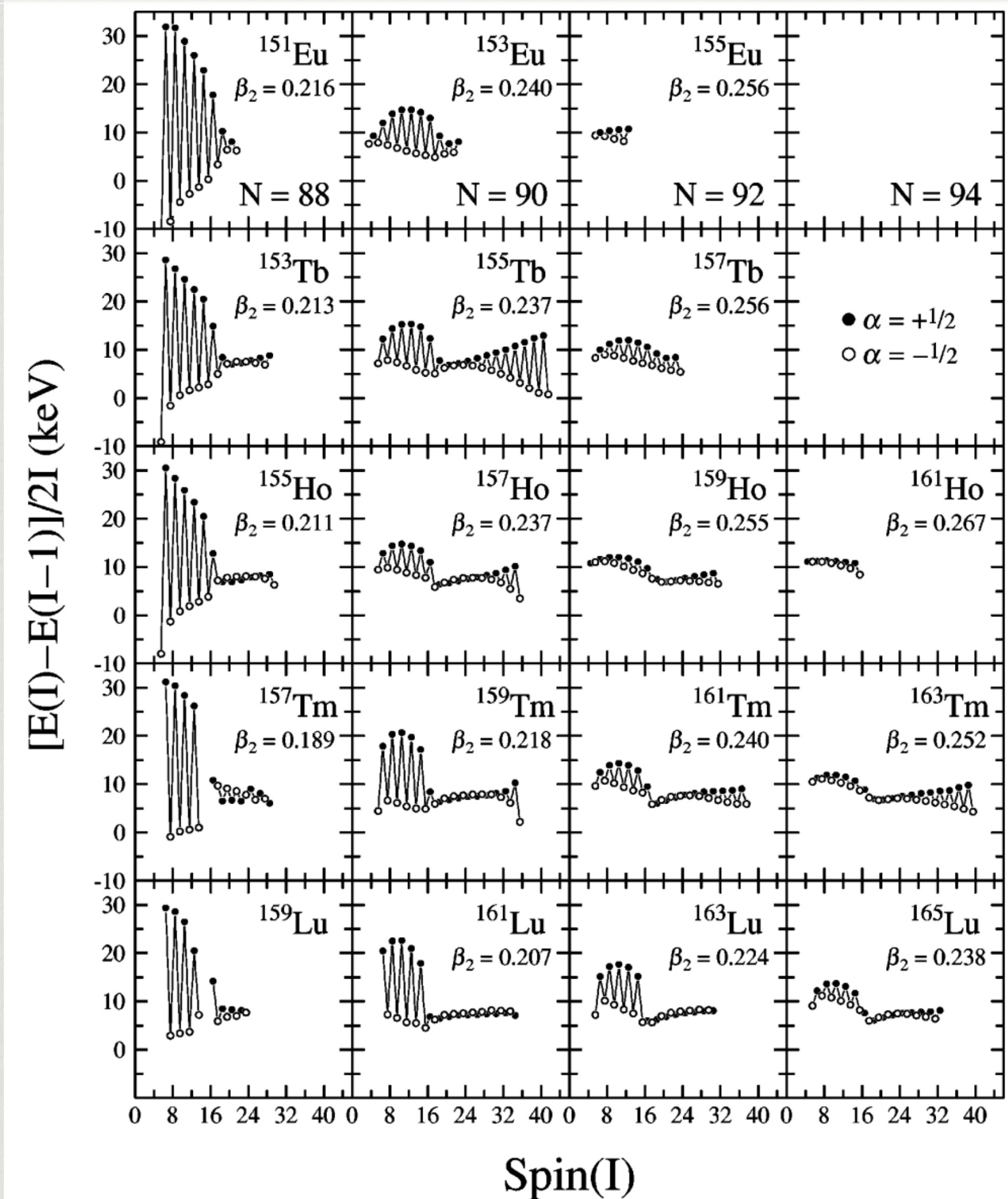
J. Simpson  
*CLRC, Daresbury Laboratory, Daresbury, Warrington, WA4 4AD, United Kingdom*  
(Received 22 June 1998)





# In the beginning (for me)...

- *Systematic study of signature splitting*
- *Likely associated with triaxial deformation at low spin*





# In the beginning (for Robert)...

Z. Physik A 274, 113–119 (1975)  
© by Springer-Verlag 1975

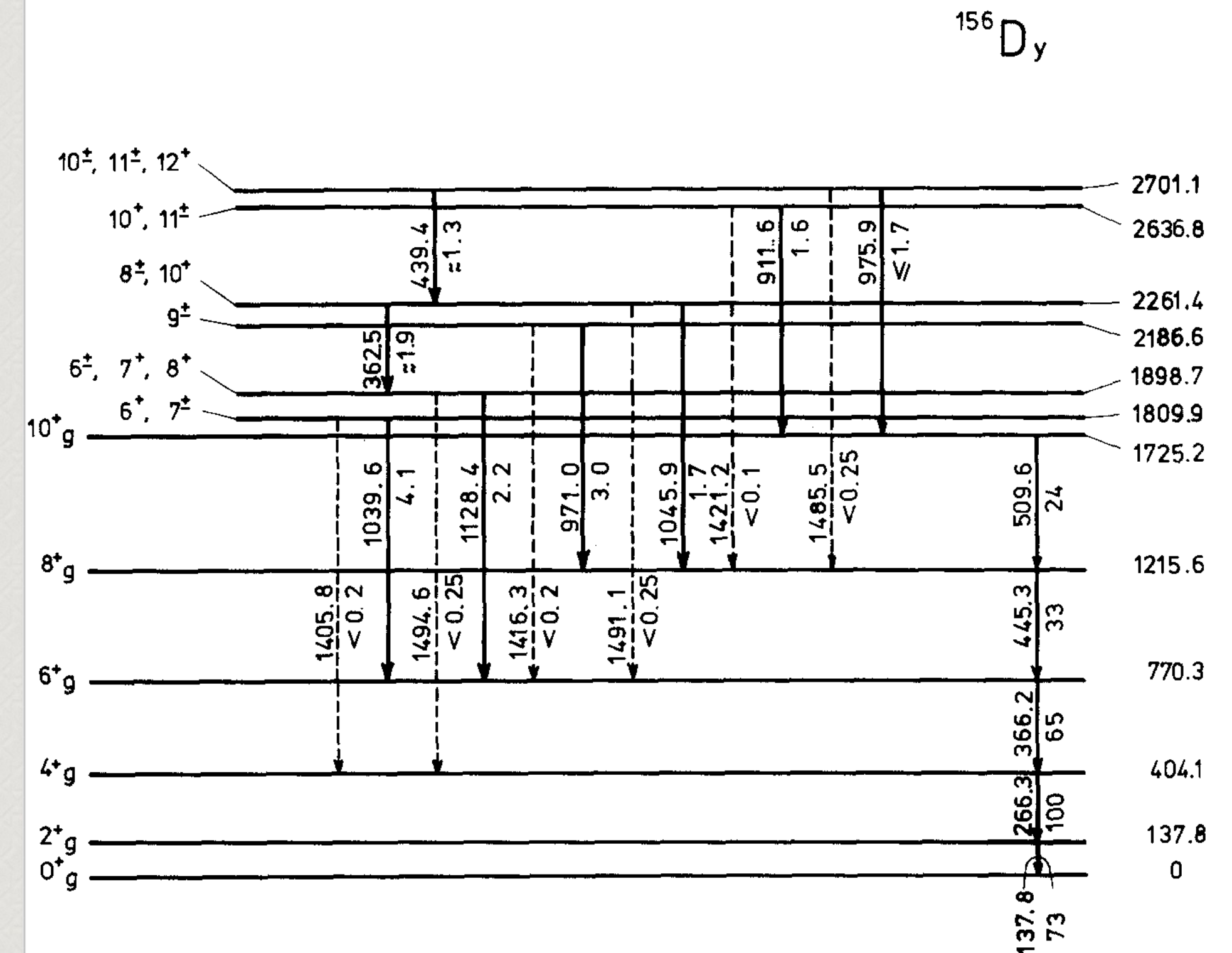
## Experimental Evidence for Low-Spin Members of “Upper” Bands in $^{156}\text{Dy}$

Y. El Masri, R. Janssens, C. Michel, P. Monseu, J. Steyaert, and J. Vervier  
Institut de Physique Corpusculaire, Louvain-la-Neuve, Belgium

Received May 26, accepted June 16, 1975

**Abstract.** Study of the energy levels of  $^{156}\text{Dy}$  through the  $^{159}\text{Tb}(p, 4n)^{156}\text{Dy}$  reaction has revealed the existence of six states with excitation energies between 1.8 and 2.8 MeV and spins between 6 and 12. Some of them can tentatively be assigned as low-spin members of “upper” bands which are thought to be responsible for the backbending phenomenon experimentally observed in the ground-state and  $\beta$ -vibrational bands of this nucleus. Others could be levels of a negative-parity octupole band.

Y. El Masri *et al.*: Experimental Evidence for Low-Spin Members





# In the beginning (for Robert)...

ELSEVIER

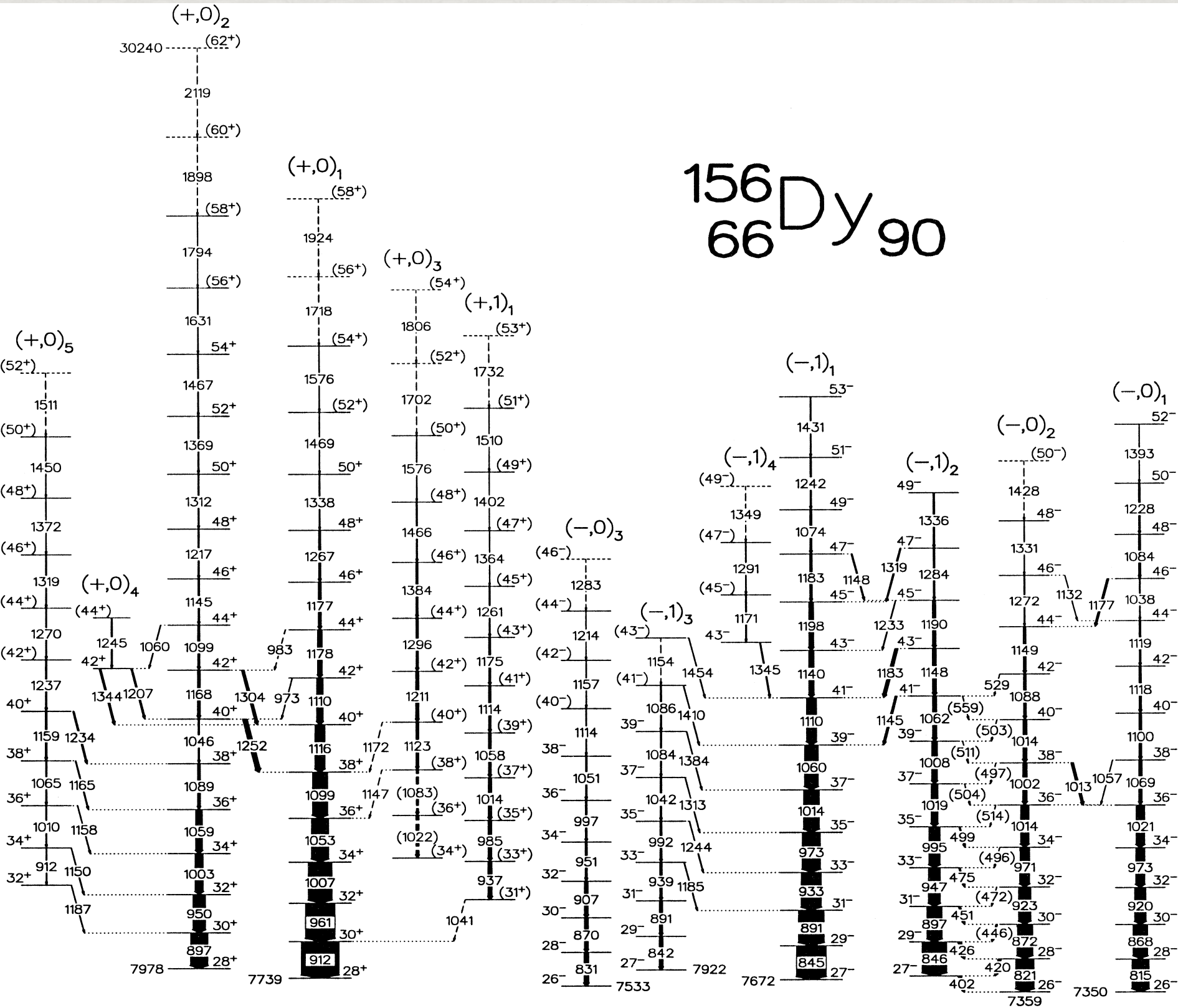
Physics Letters B 437 (1998) 35–43

Spin  $\sim 60 \hbar$  in  $^{156}\text{Dy}$ :  
competition between collective and terminating structures  
at very high-spin

F.G. Kondev <sup>a,1</sup>, M.A. Riley <sup>a</sup>, R.V.F. Janssens <sup>b</sup>, J. Simpson <sup>c</sup>, A.V. Afanasjev <sup>d,2</sup>,  
I. Ragnarsson <sup>d</sup>, I. Ahmad <sup>b</sup>, D.J. Blumenthal <sup>b</sup>, T.B. Brown <sup>a</sup>, M.P. Carpenter <sup>b</sup>,  
P. Fallon <sup>e</sup>, S.M. Fischer <sup>b</sup>, G. Hackman <sup>b</sup>, D.J. Hartley <sup>a</sup>, C.A. Kalfas <sup>f</sup>, T.L. Khoo <sup>b</sup>,  
T. Lauritsen <sup>b</sup>, W.C. Ma <sup>g</sup>, D. Nisius <sup>b</sup>, J.F. Sharpey-Schafer <sup>h</sup>, P.G. Varmette <sup>g</sup>

F.G. Kondev et al. / Physics Letters B 437 (1998) 35–43

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# In the beginning (for Robert)...

PHYSICAL REVIEW C **95**, 014321 (2017)

## Investigation of negative-parity states in $^{156}\text{Dy}$ : Search for evidence of tetrahedral symmetry

D. J. Hartley,<sup>1</sup> L. L. Riedinger,<sup>2</sup> R. V. F. Janssens,<sup>3</sup> S. N. T. Majola,<sup>4</sup> M. A. Riley,<sup>5</sup> J. M. Allmond,<sup>6,7</sup> C. W. Beausang,<sup>6</sup> M. P. Carpenter,<sup>3</sup> C. J. Chiara,<sup>3,8,9,\*</sup> N. Cooper,<sup>10</sup> D. Curien,<sup>11,12</sup> B. J. P. Gall,<sup>11,12</sup> P. E. Garrett,<sup>13</sup> F. G. Kondev,<sup>9</sup> W. D. Kulp,<sup>14</sup> T. Lauritsen,<sup>3</sup> E. A. McCutchan,<sup>3,15</sup> D. Miller,<sup>2,†</sup> S. Miller,<sup>5</sup> J. Piot,<sup>11,12</sup> N. Redon,<sup>16</sup> J. F. Sharpey-Schafer,<sup>17</sup> J. Simpson,<sup>18</sup> I. Stefanescu,<sup>3,8</sup> X. Wang,<sup>5,‡</sup> V. Werner,<sup>10,§</sup> J. L. Wood,<sup>14</sup> C.-H. Yu,<sup>7</sup> S. Zhu,<sup>3</sup> and J. Dudek<sup>11,19</sup>

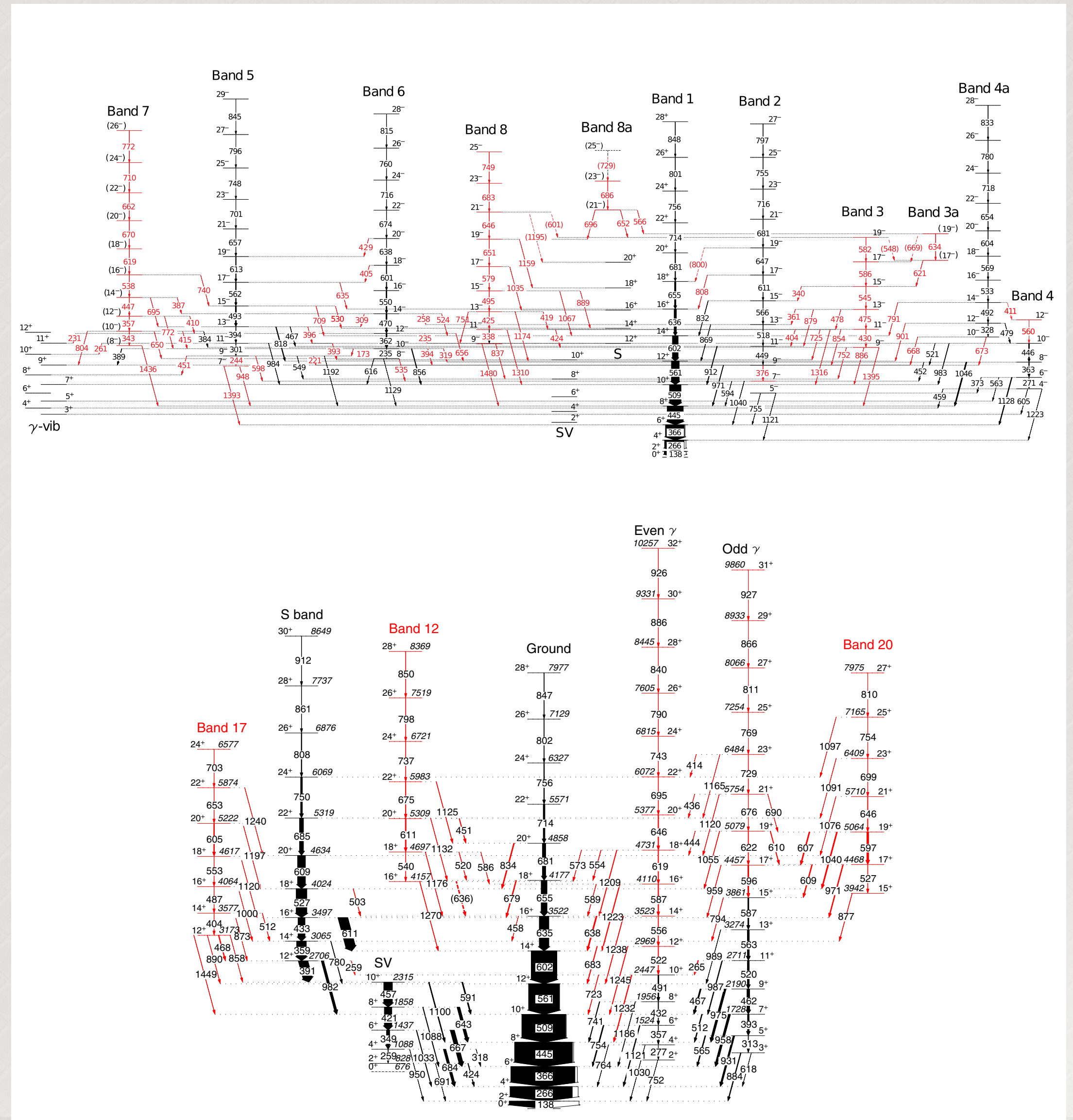
PHYSICAL REVIEW C **91**, 034330 (2015)

## Observation of $\gamma$ vibrations and alignments built on non-ground-state configurations in $^{156}\text{Dy}$

S. N. T. Majola,<sup>1,2,\*</sup> D. J. Hartley,<sup>3</sup> L. L. Riedinger,<sup>4</sup> J. F. Sharpey-Schafer,<sup>5</sup> J. M. Allmond,<sup>6,17</sup> C. Beausang,<sup>6</sup> M. P. Carpenter,<sup>7</sup> C. J. Chiara,<sup>8</sup> N. Cooper,<sup>9</sup> D. Curien,<sup>10</sup> B. J. P. Gall,<sup>10</sup> P. E. Garrett,<sup>11</sup> R. V. F. Janssens,<sup>7</sup> F. G. Kondev,<sup>8</sup> W. D. Kulp,<sup>12</sup> T. Lauritsen,<sup>7</sup> E. A. McCutchan,<sup>7,13</sup> D. Miller,<sup>4</sup> J. Piot,<sup>10</sup> N. Redon,<sup>14</sup> M. A. Riley,<sup>15</sup> J. Simpson,<sup>16</sup> I. Stefanescu,<sup>7</sup> V. Werner,<sup>9</sup> X. Wang,<sup>15</sup> J. L. Wood,<sup>12</sup> C.-H. Yu,<sup>17</sup> and S. Zhu<sup>7</sup>

*Robert's Golden Rule:*

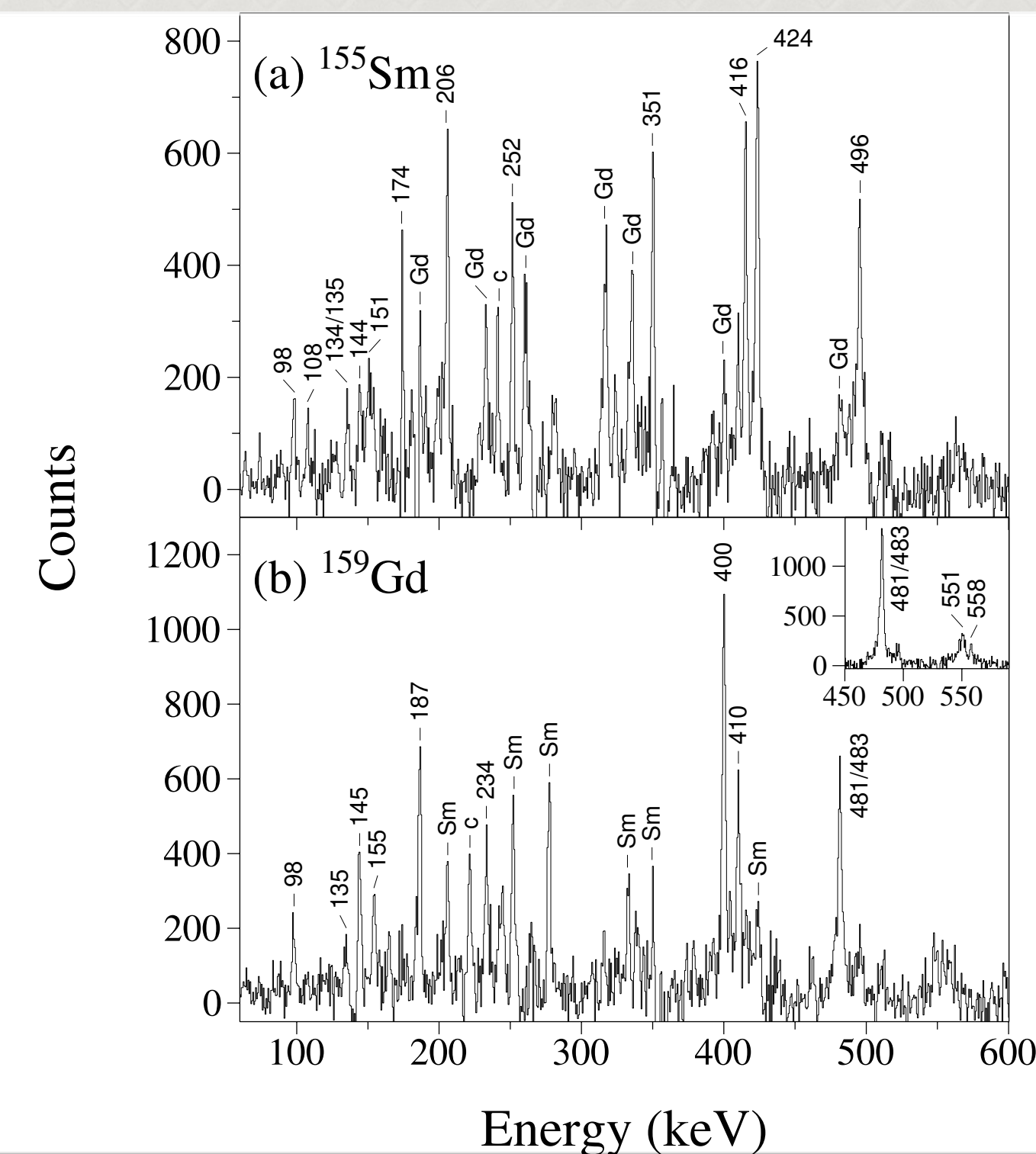
Always do an experiment on  $^{156}\text{Dy}$   
every 15-20 years





# Onto to More Recent Work...

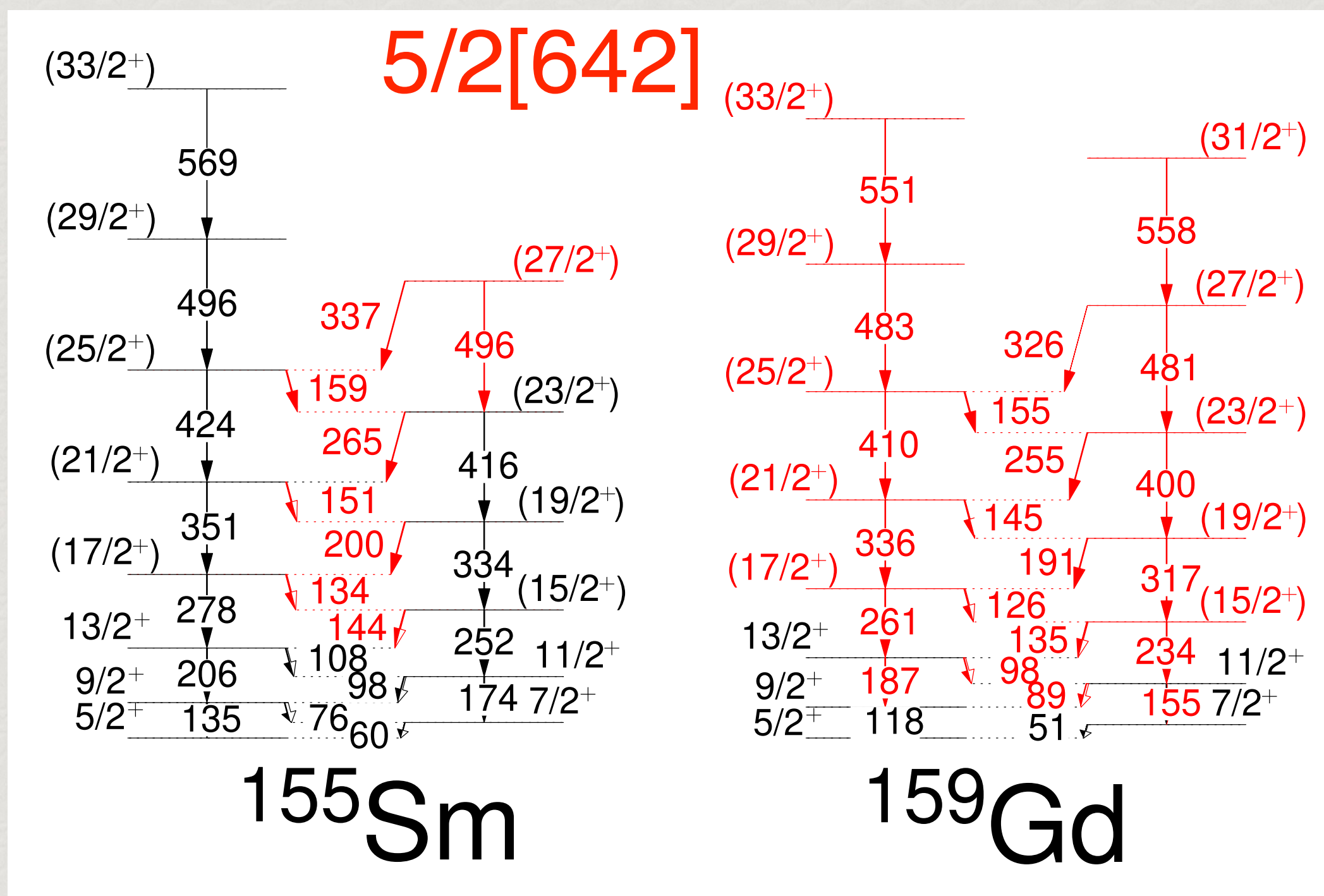
- *Mutli-nucleon transfer reactions allow for the observance of neutron-rich nuclei*
- *Produce large variety of nuclei with moderately high spin that come in pairs*
- $^{160}\text{Gd} + ^{154}\text{Sm}$  reaction at 1000 MeV
- *Gammasphere had 73 detectors - focus on prompt spectroscopy*





# Onto to More Recent Work...

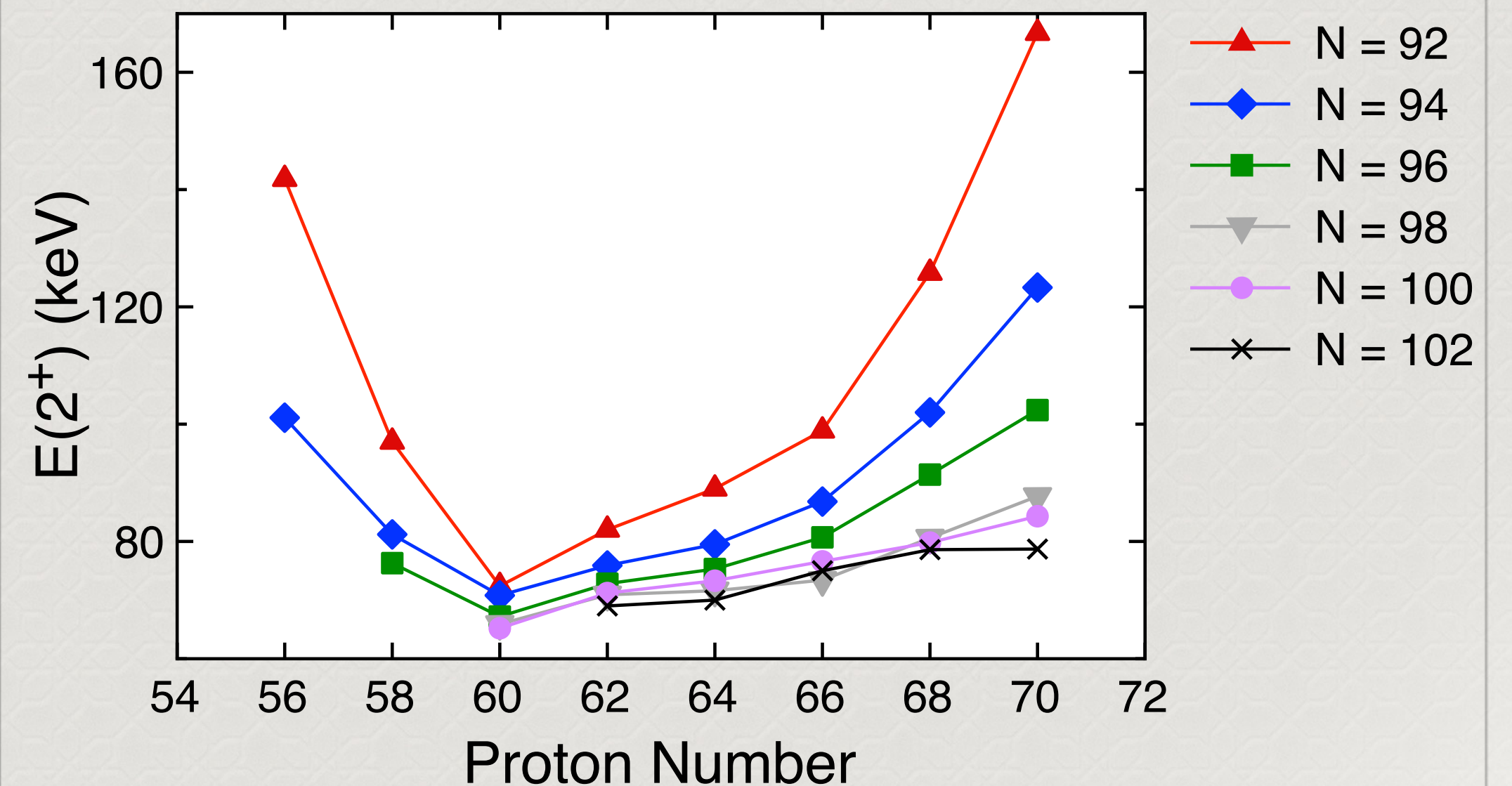
- *Mutli-nucleon transfer reactions allow for the observance of neutron-rich nuclei*
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- *Gammasphere had 73 detectors - focus on prompt spectroscopy*





# Evidence of $Z = 60$ Subshell Gap

- *A low energy of the first  $2^+$  state  $[E(2^+)]$  in even-even nuclei is associated with large deformation*
- *Note that for each isotone group,  $Z = 60$  (Nd) has lowest  $E(2^+)$*
- *Indicates high-deformation subshell gap at  $Z = 60$ , rather than at midshell,  $Z = 66$  (Dy)*





# Origin of Energy Staggering

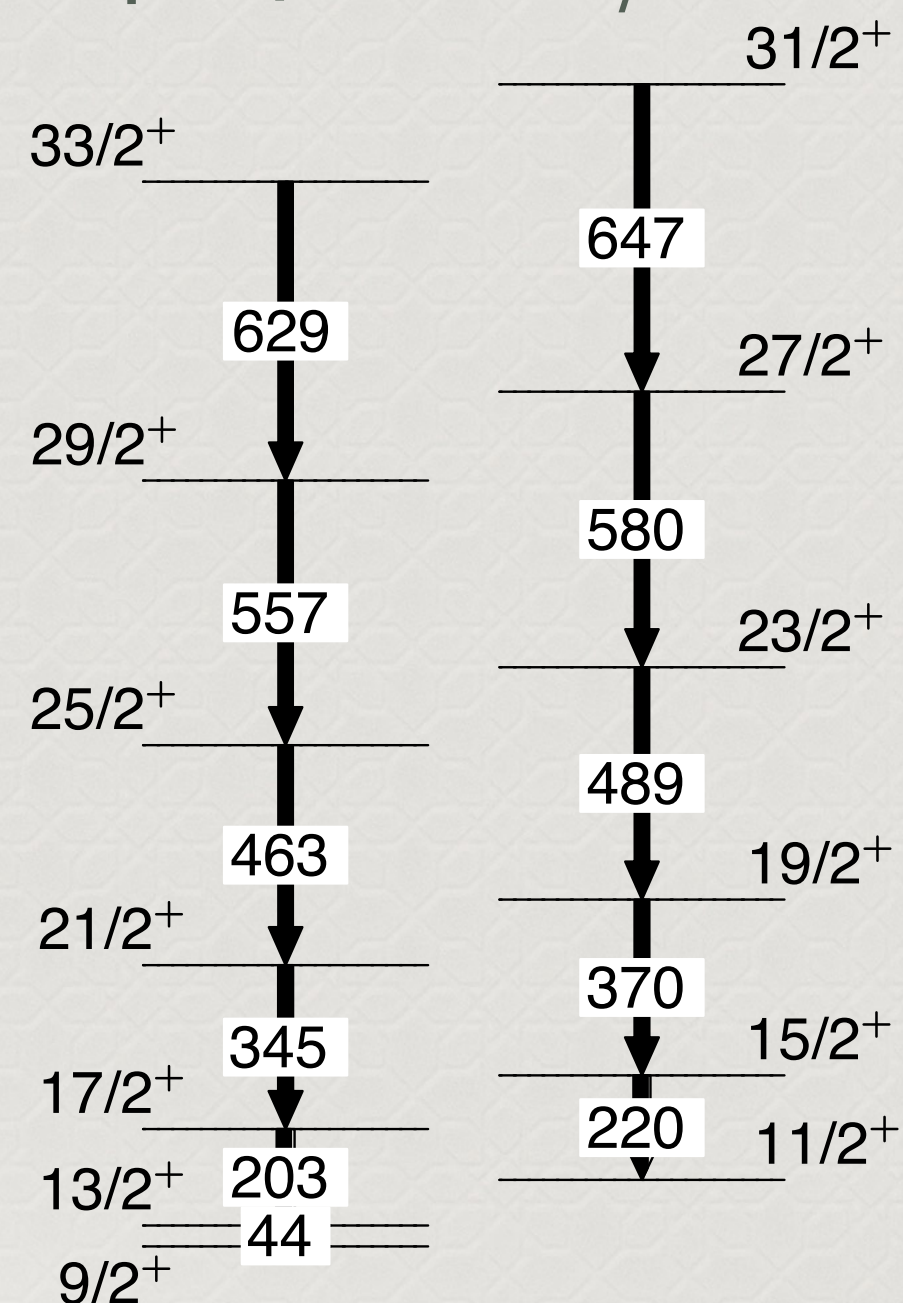
Signature

$\alpha = +1/2$

$-1/2$

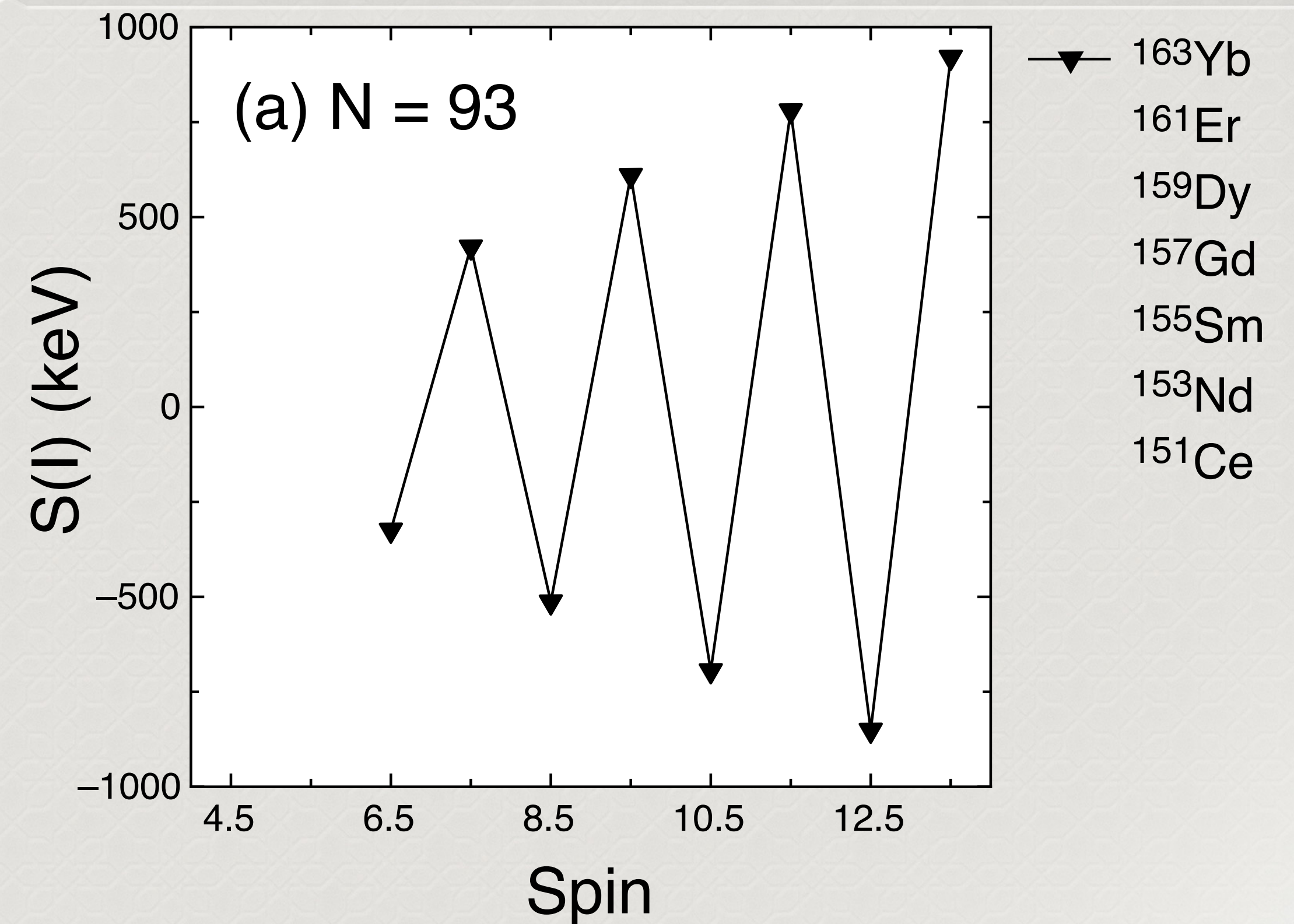
$^{163}\text{Yb}$

$5/2[642]$



$$E_{K=1/2}(I) = \frac{\hbar^2}{2\mathcal{J}} [I(I+1) + \underbrace{a(-1)^{I+1/2}}_{\text{Creates energy staggering}} (I+1/2)]$$

Creates energy staggering

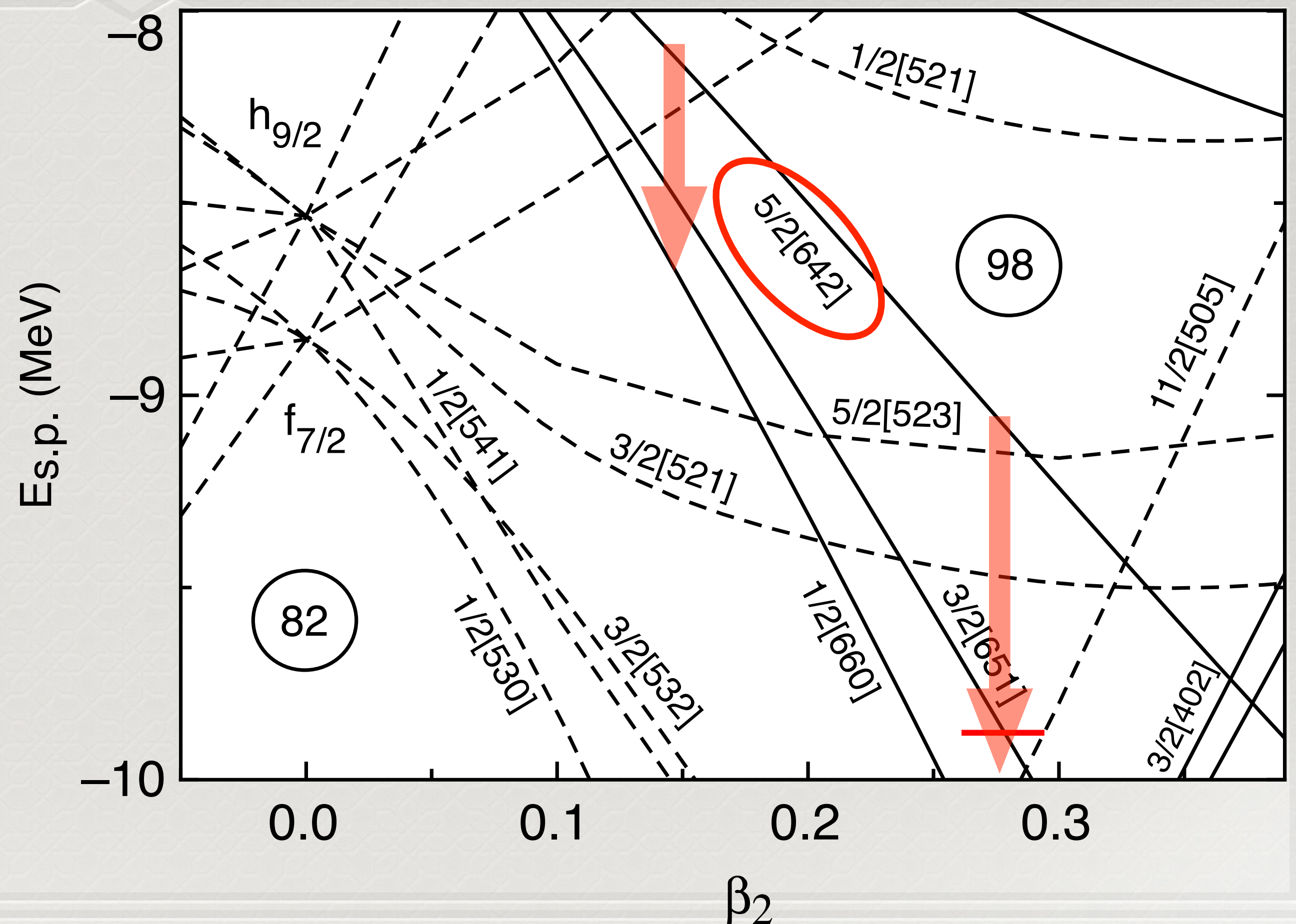


$$S(I) = E(I) - (E-1) - 1/2[E(I+1) - E(I) + E(I-1) - E(I-2)]$$



# Origin of Energy Staggering

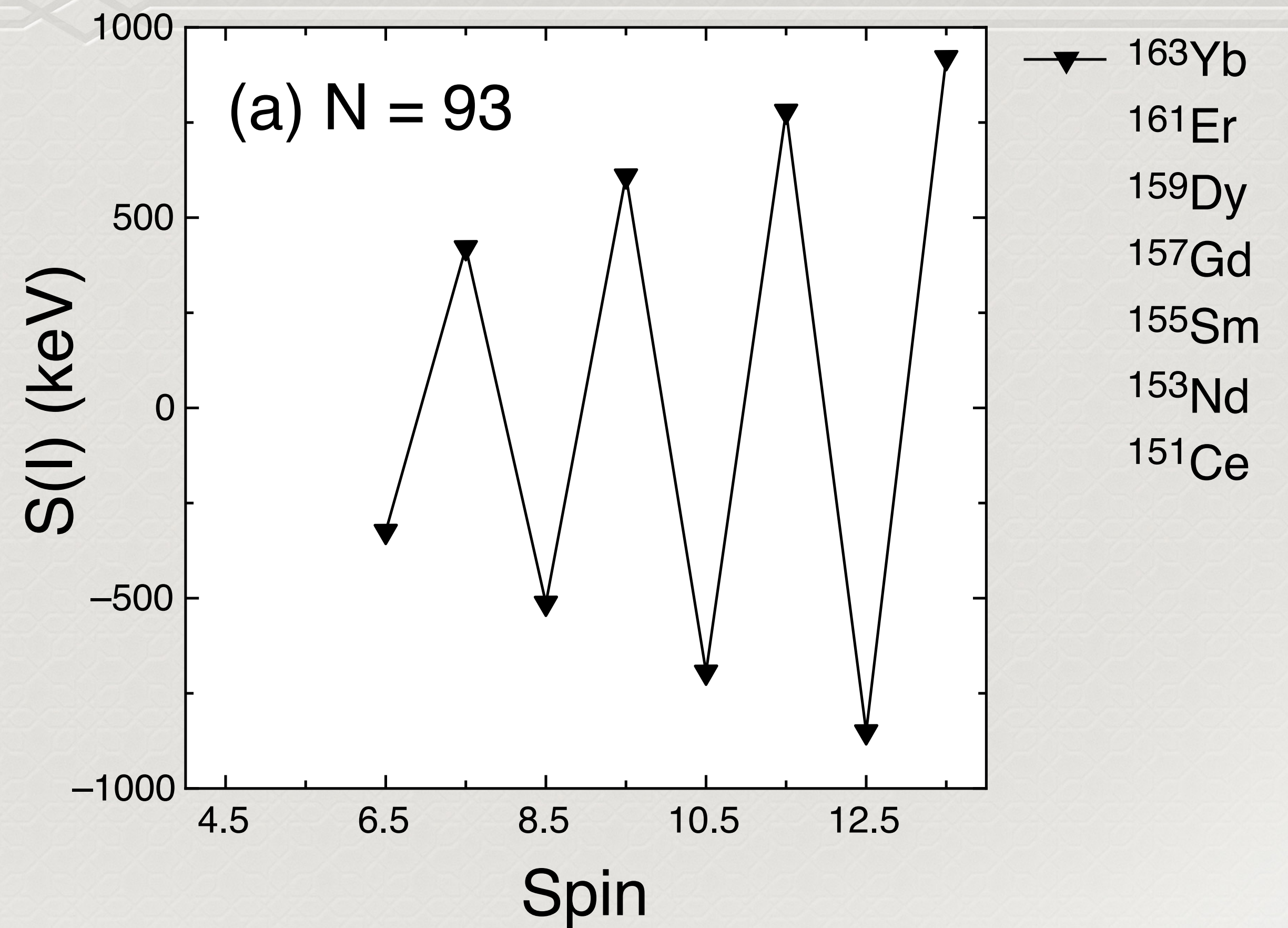
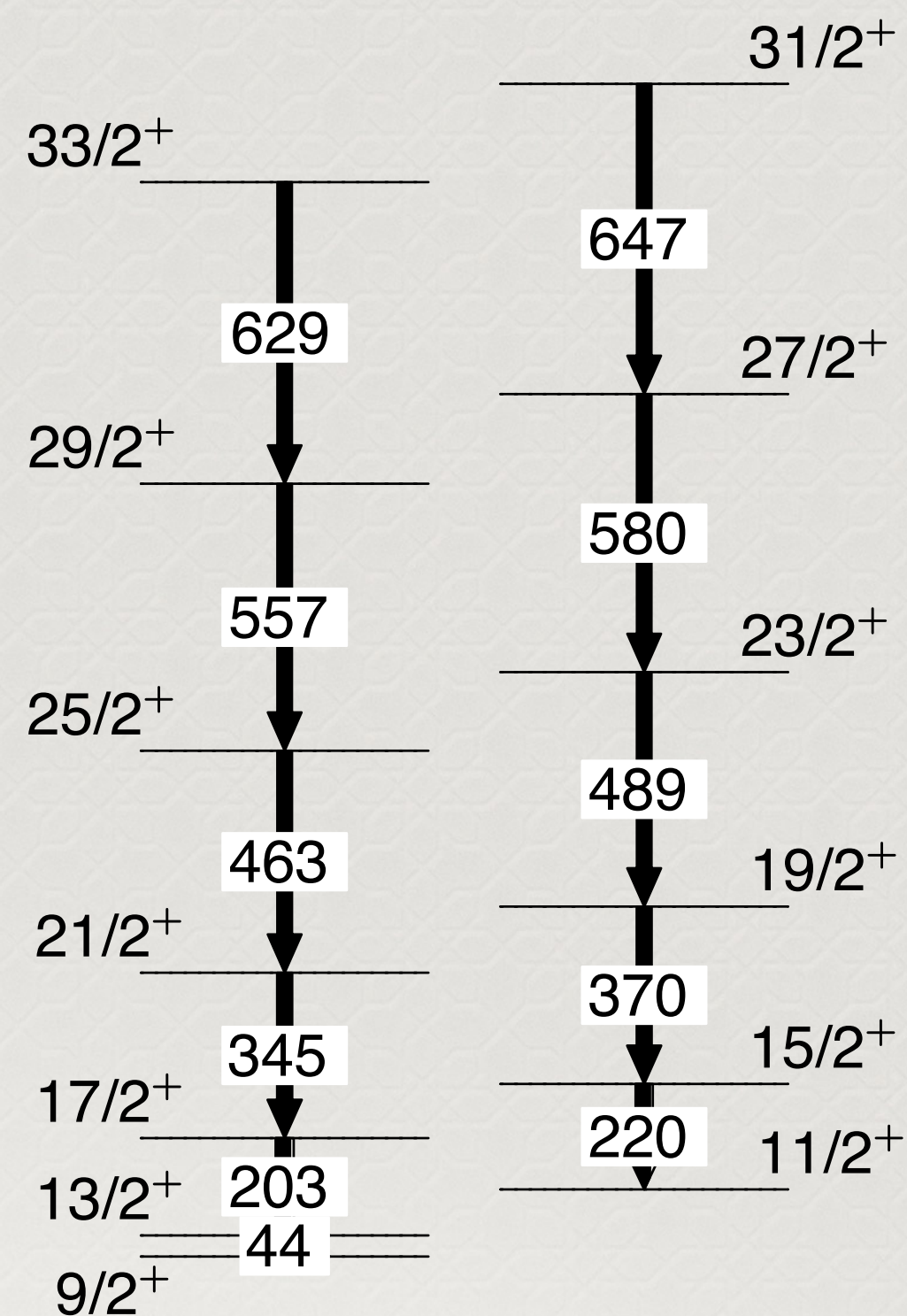
- Only  $K = 1/2$  orbital has decoupling constant,  $a$ , that produces energy staggering
- Higher  $K$  orbitals are mixed and will have  $K = 1/2$  component
- The amount of  $K = 1/2$  admixture is dependent on the location of the Fermi surface
- Low  $\beta_2 =$  large  $K$  mix = large splitting  
High  $\beta_2 =$  low  $K$  mix = low splitting





# Energy Staggering in $5/2[642]$ Band

$^{163}\text{Yb}$

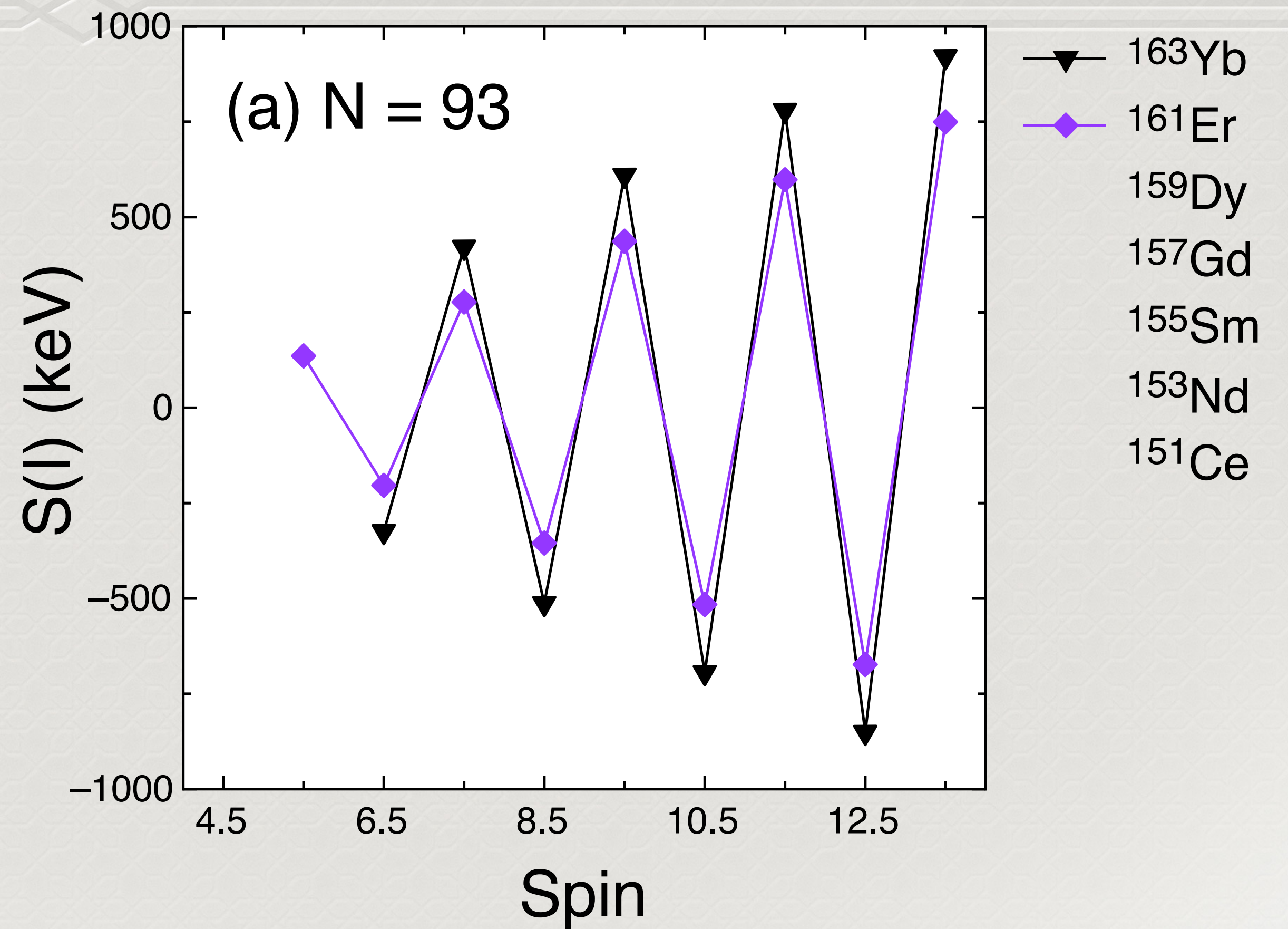
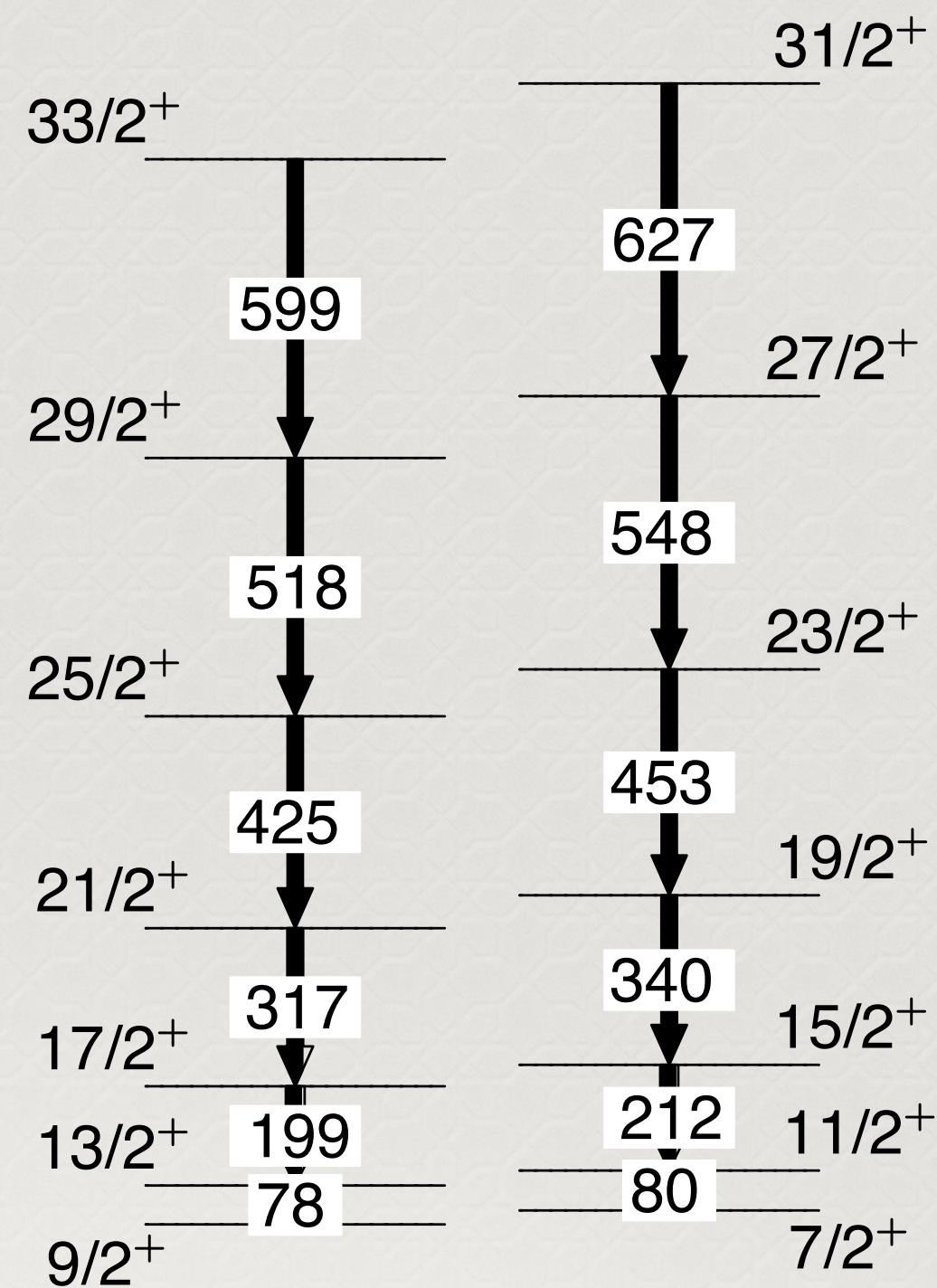


J. Kownacki *et al.*, NPA 394, 269 (1983)



# Energy Staggering in $5/2[624]$ Band

$^{161}\text{Er}$

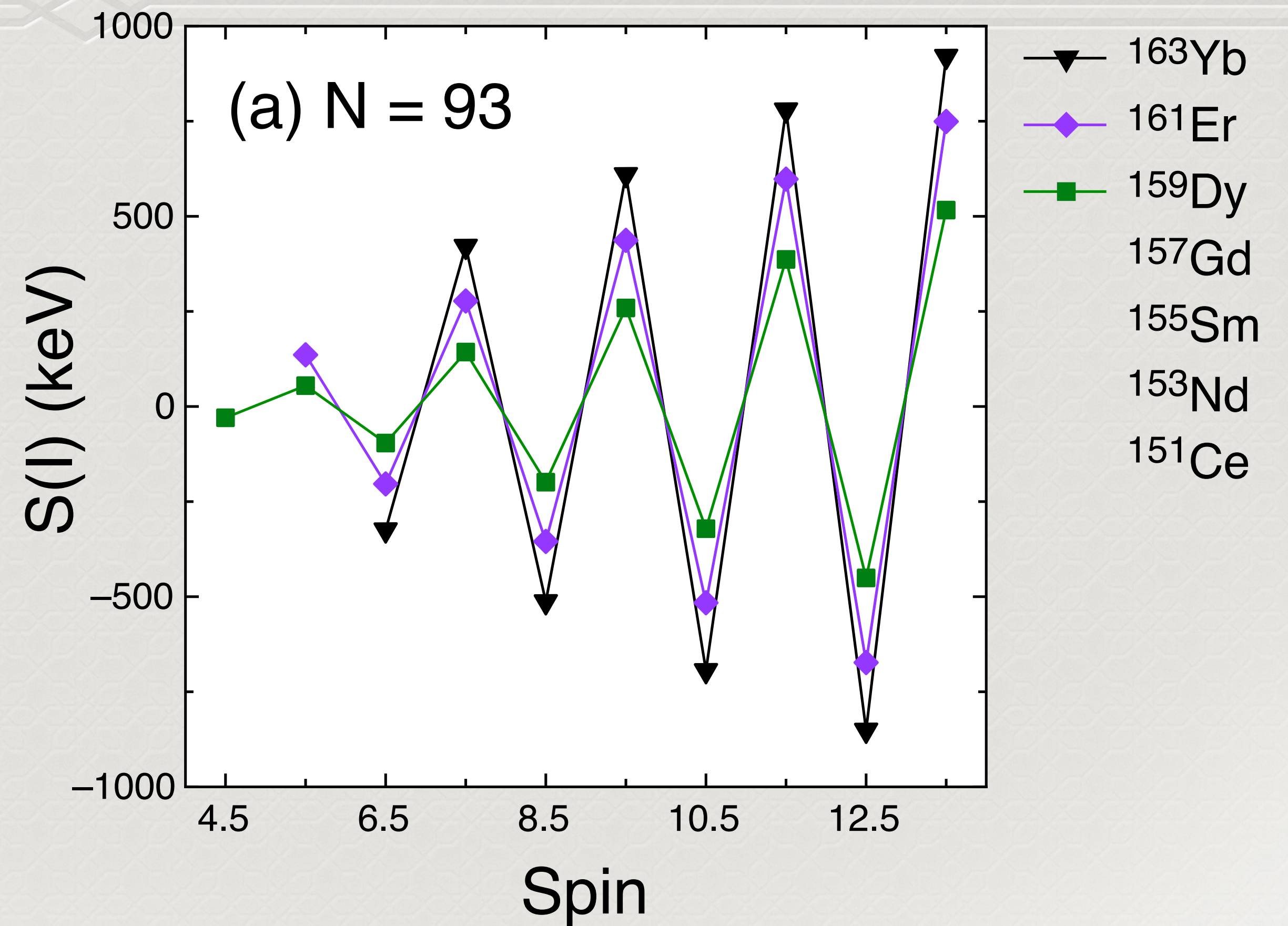
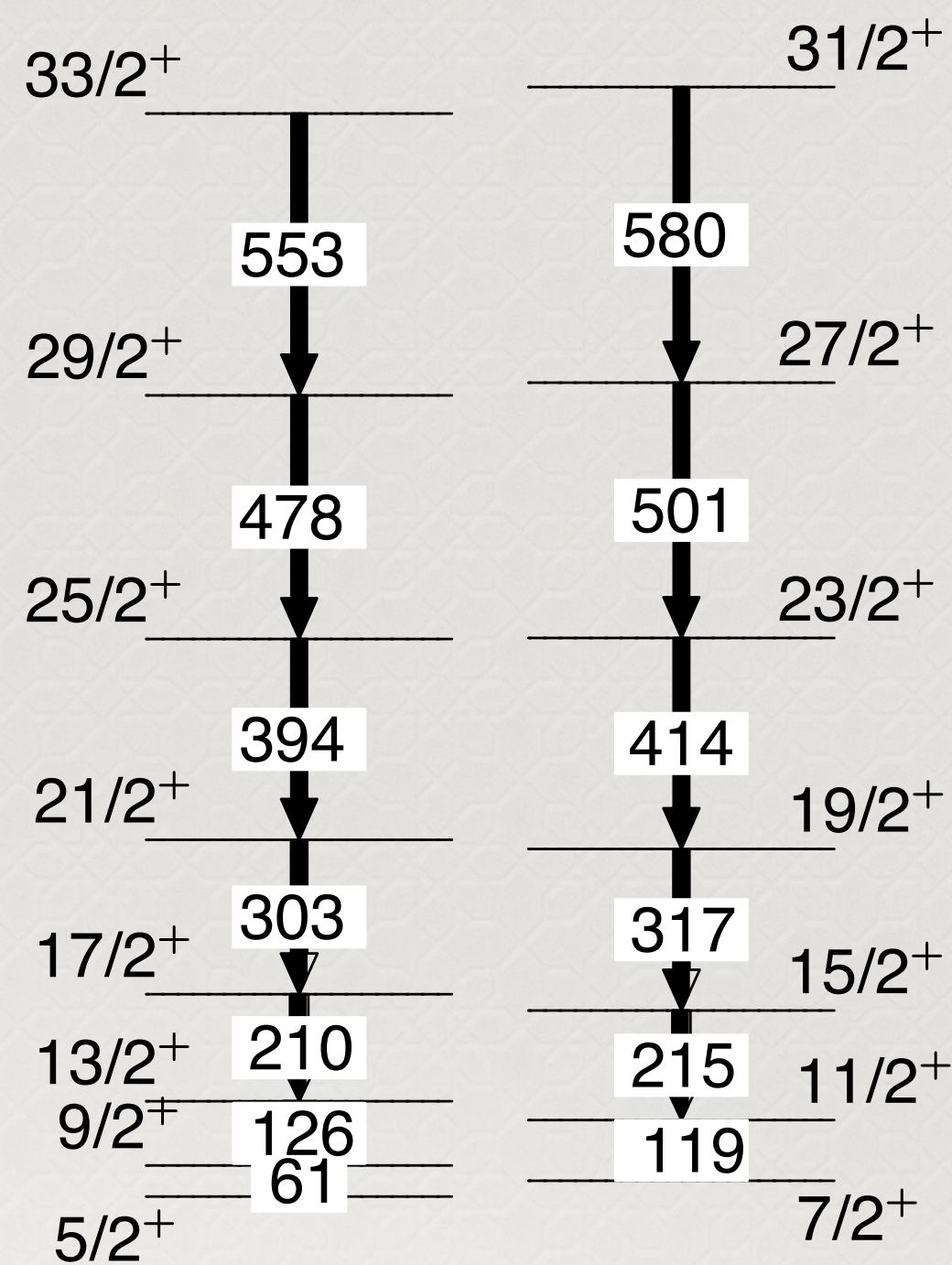


J. D. Garrett *et al.*, PLB **118**, 297 (1982)



# Energy Staggering in $5/2[624]$ Band

$^{159}\text{Dy}$

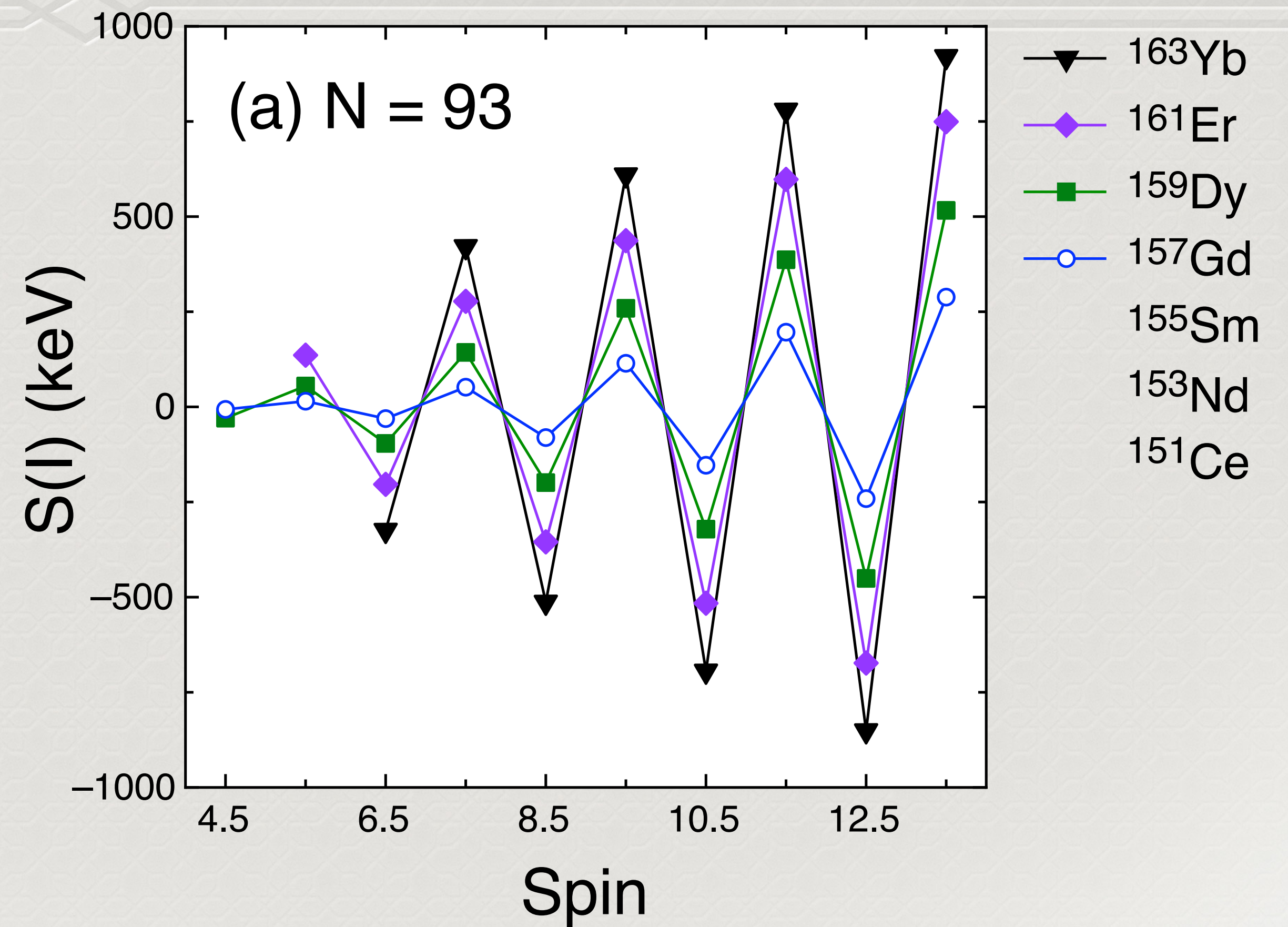
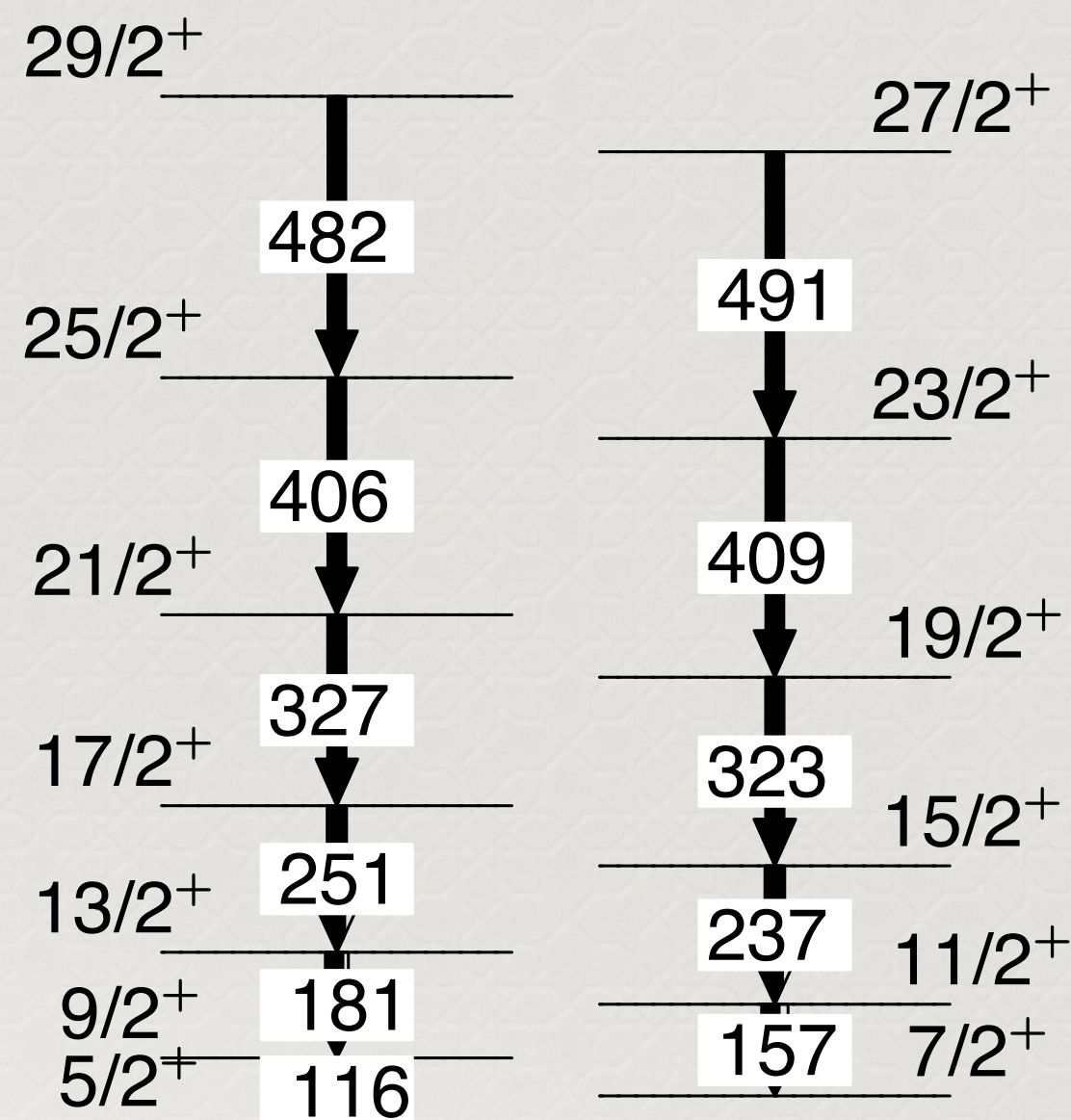


A. Jungclaus *et al.*, PRC **67**, 034302 (2003)



# Energy Staggering in $5/2[624]$ Band

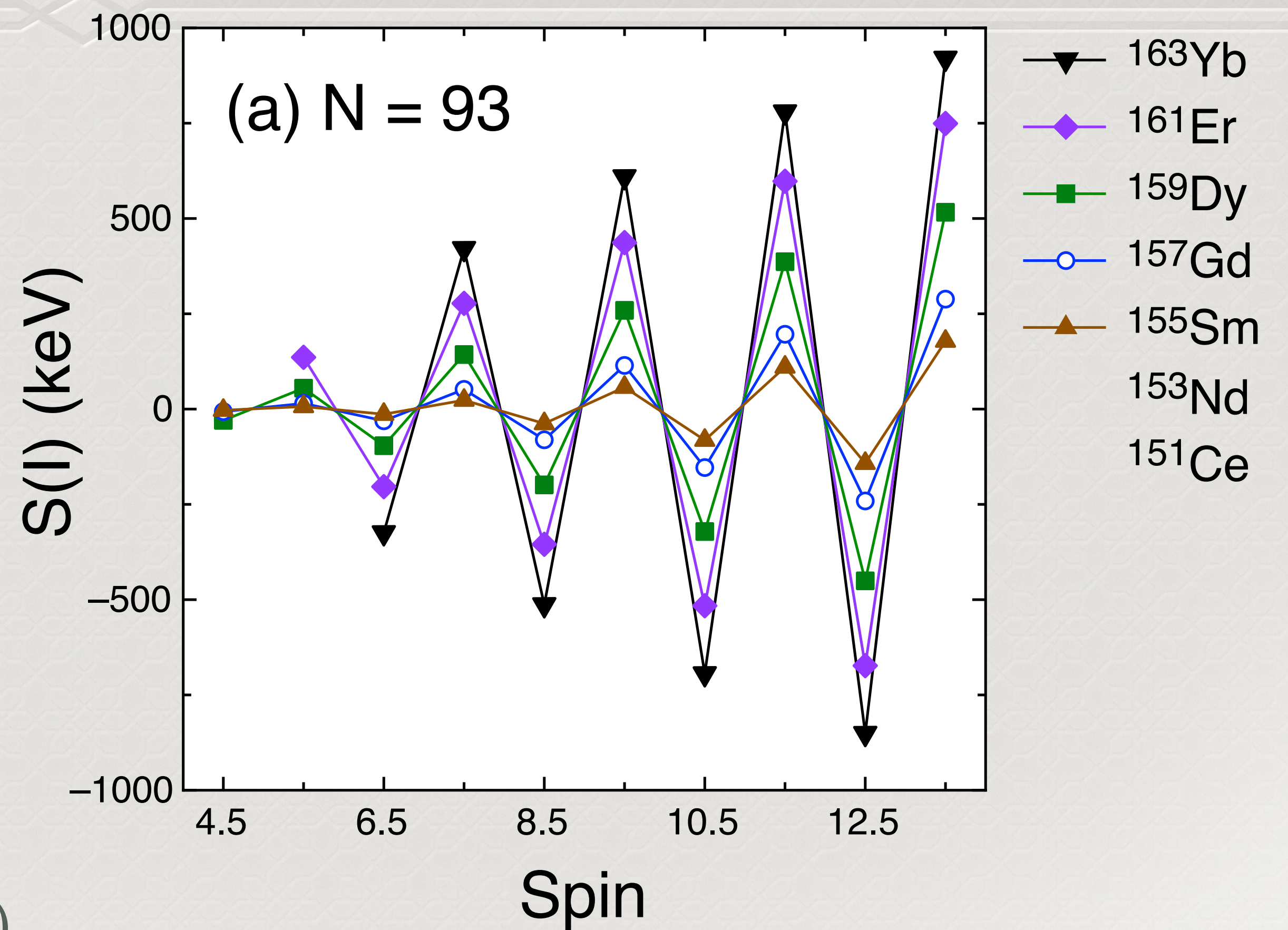
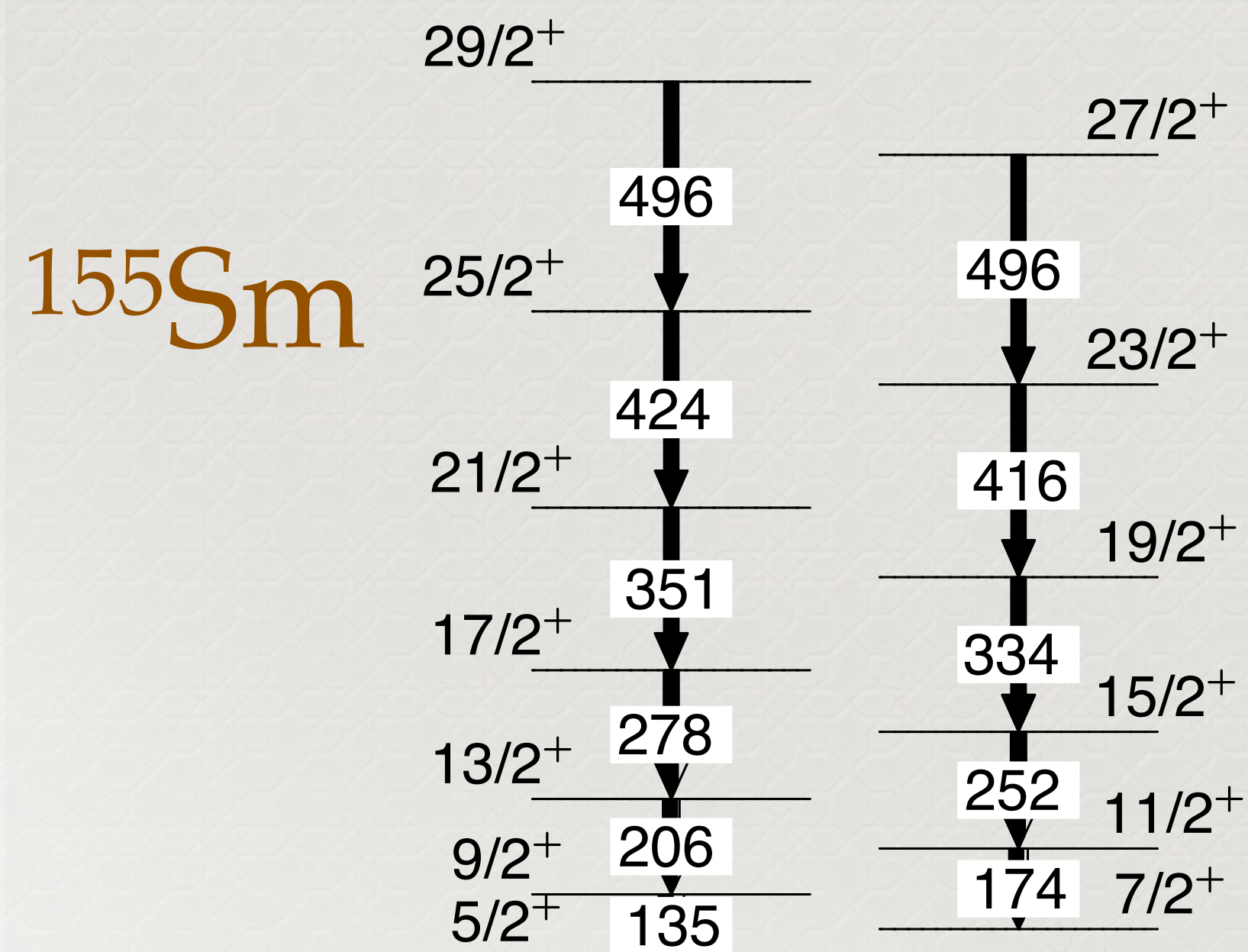
$^{157}\text{Gd}$



T. Hayakawa *et al.*, PLB 551, 79 (2003)



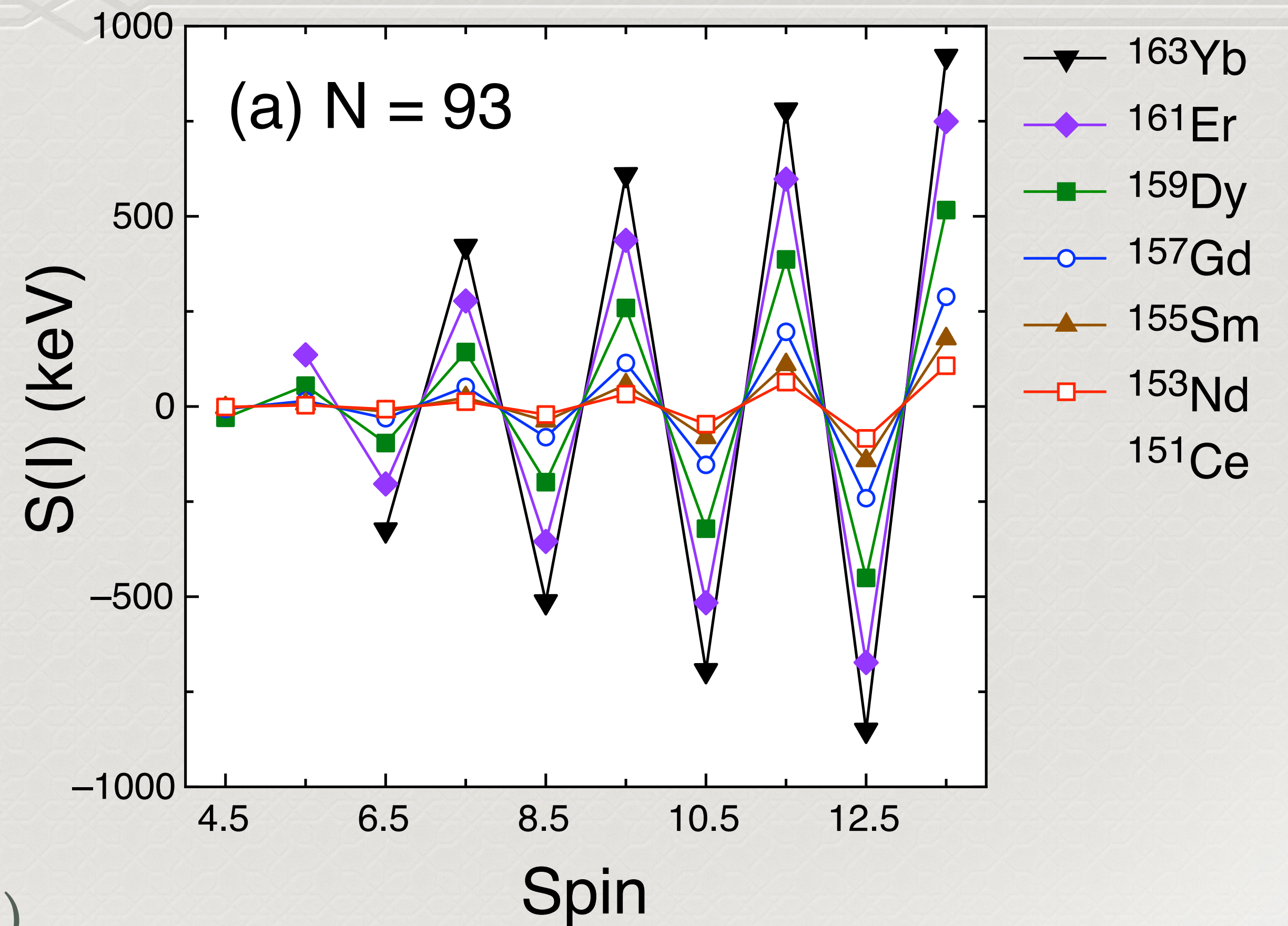
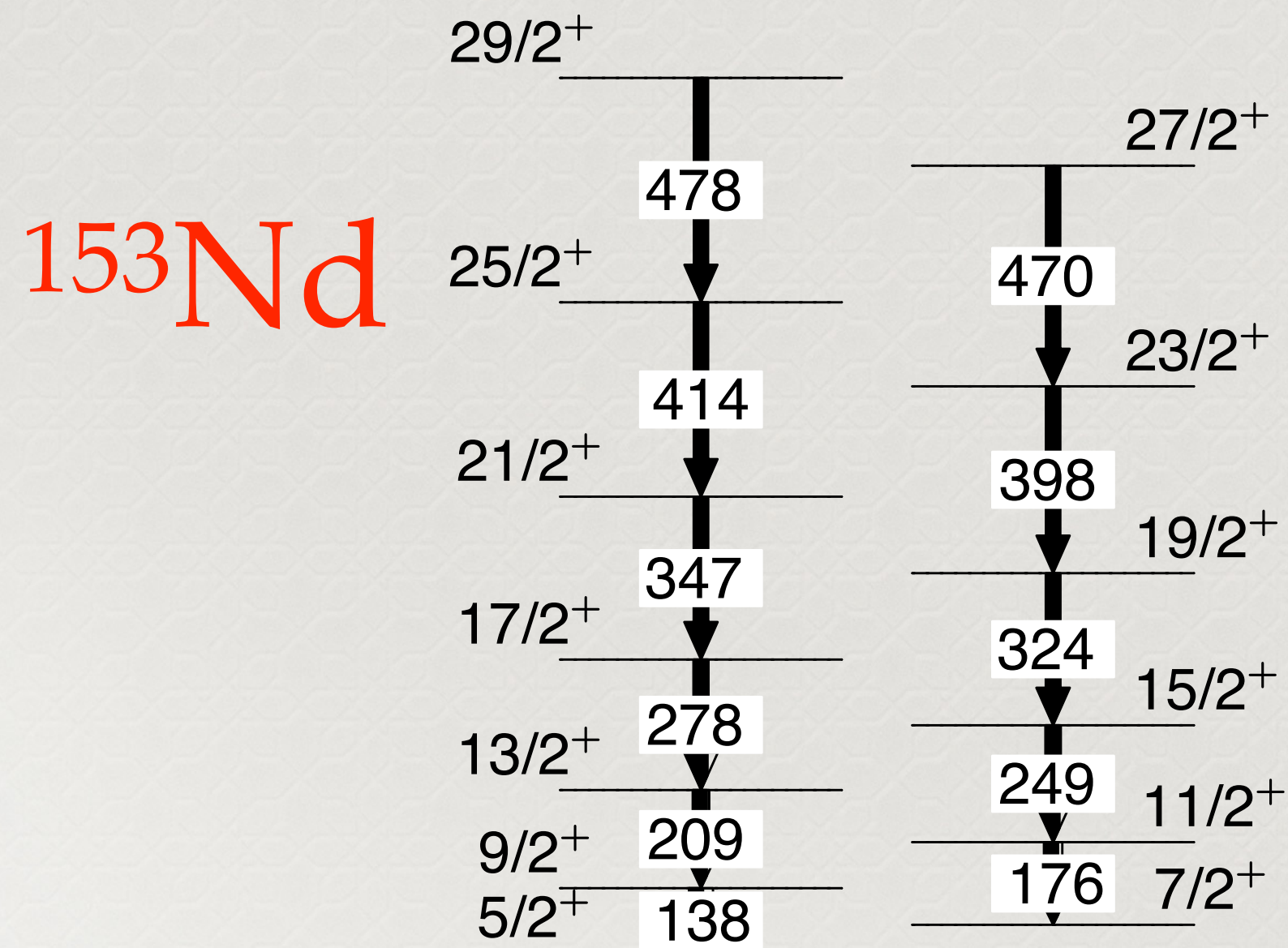
# Energy Staggering in $5/2[624]$ Band



S. J. Asztalos *et al.*, PRC **60**, 044307 (1999)



# Energy Staggering in $5/2[624]$ Band

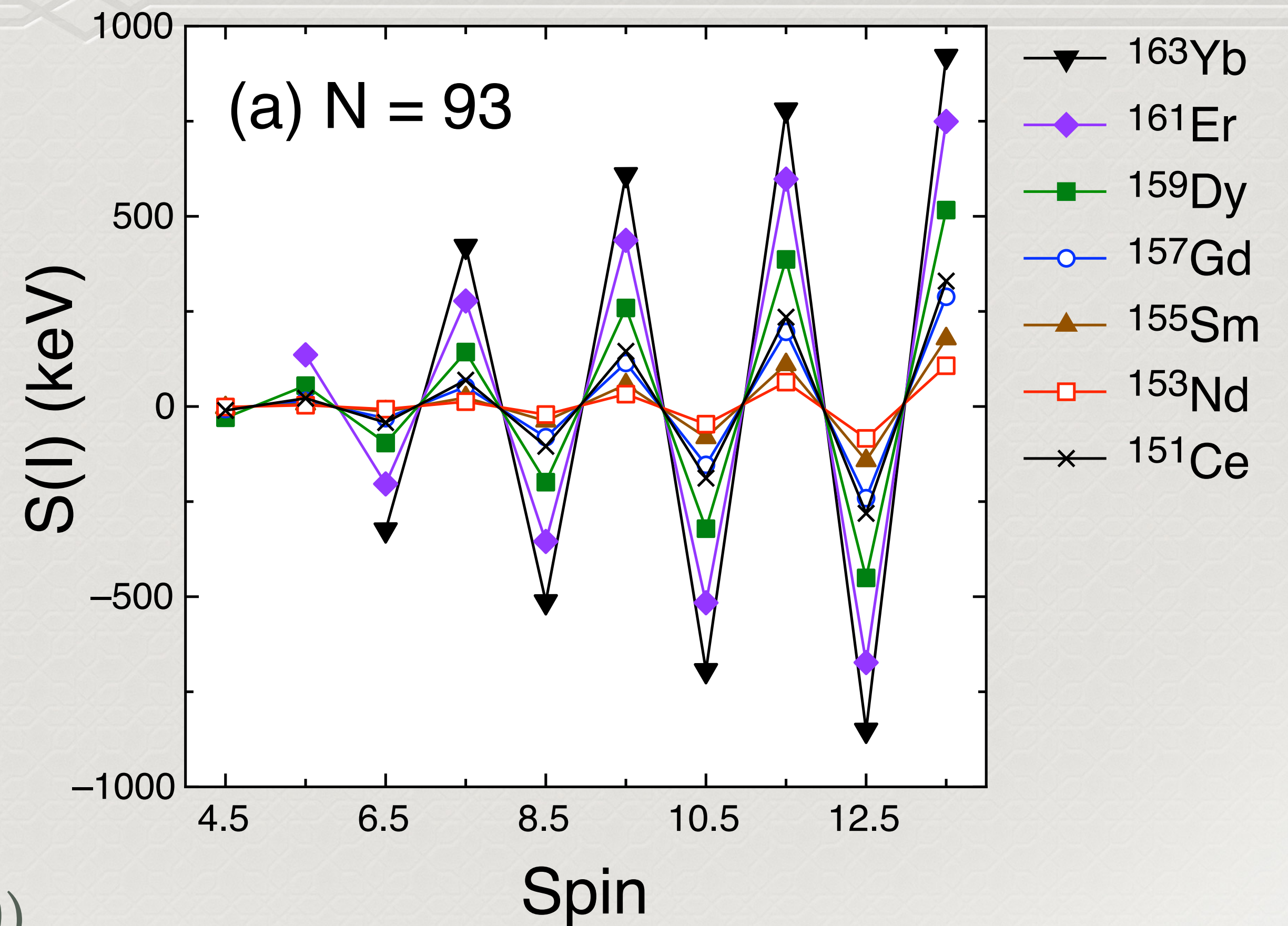
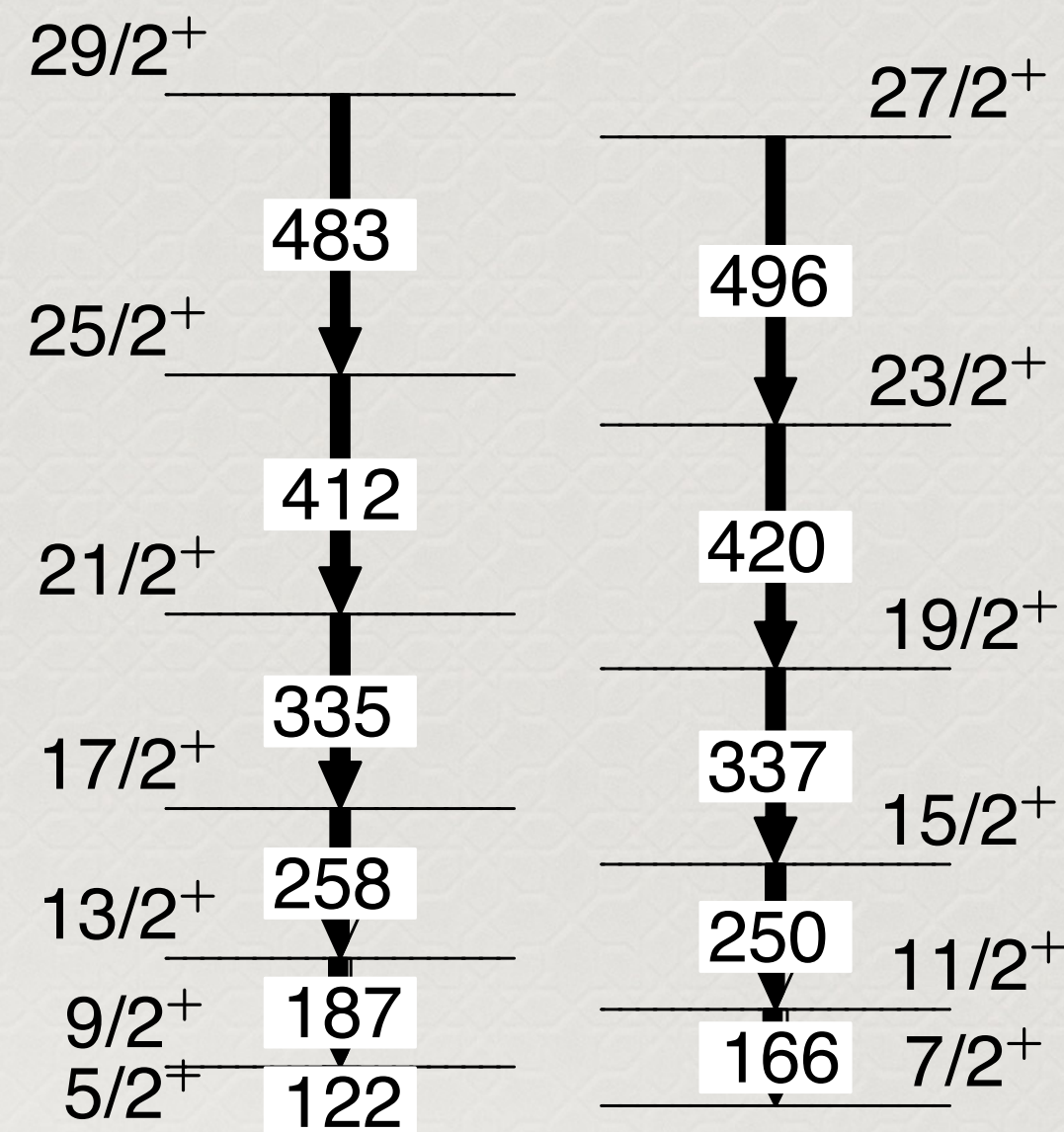


G. S. Simpson *et al.*, PRC 81, 024313 (2010)



# Energy Staggering in $5/2[624]$ Band

$^{151}\text{Ce}$

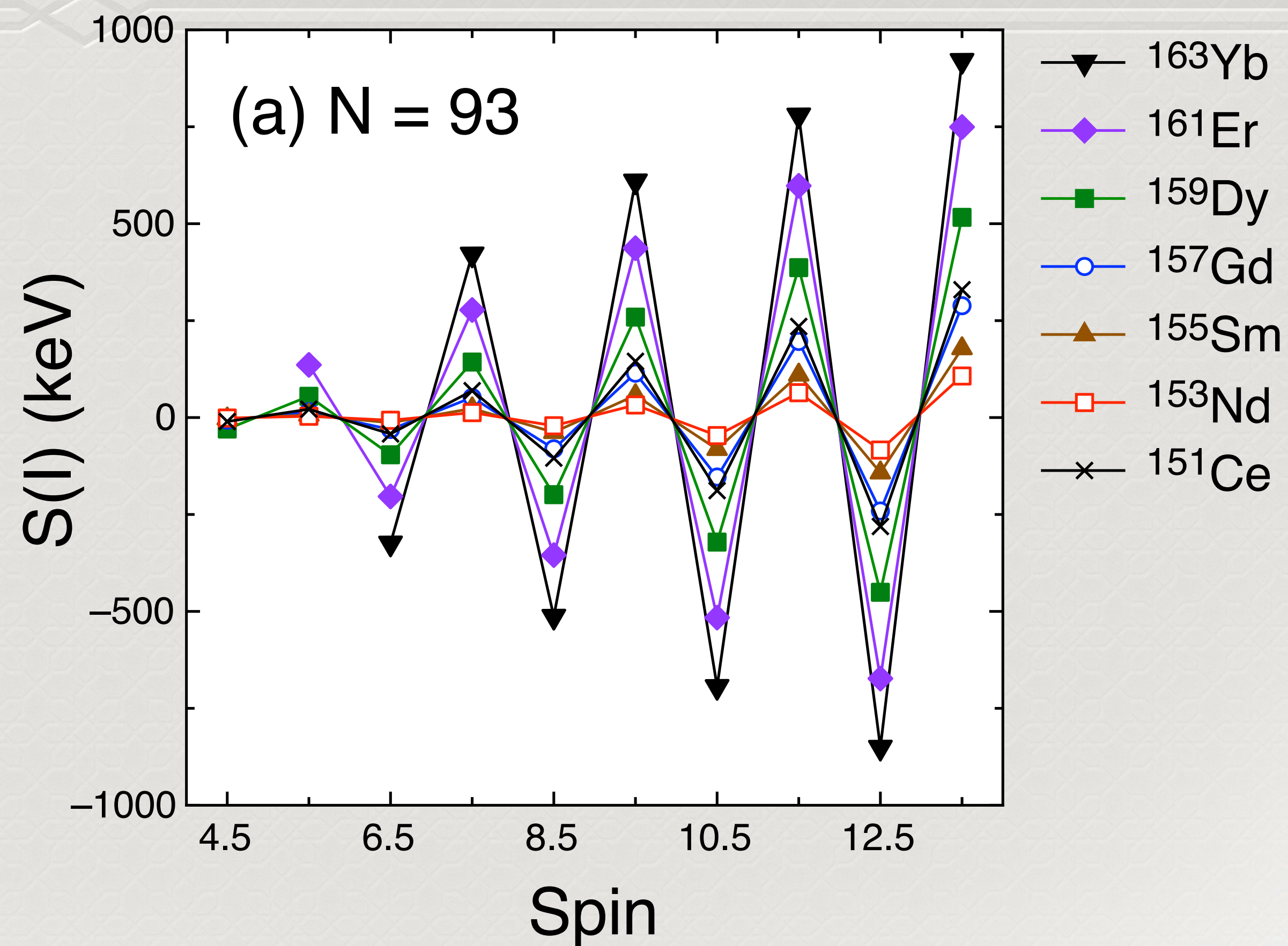


G. S. Simpson *et al.*, PRC **81**, 024313 (2010)



# Energy Staggering in $5/2[624]$ Band

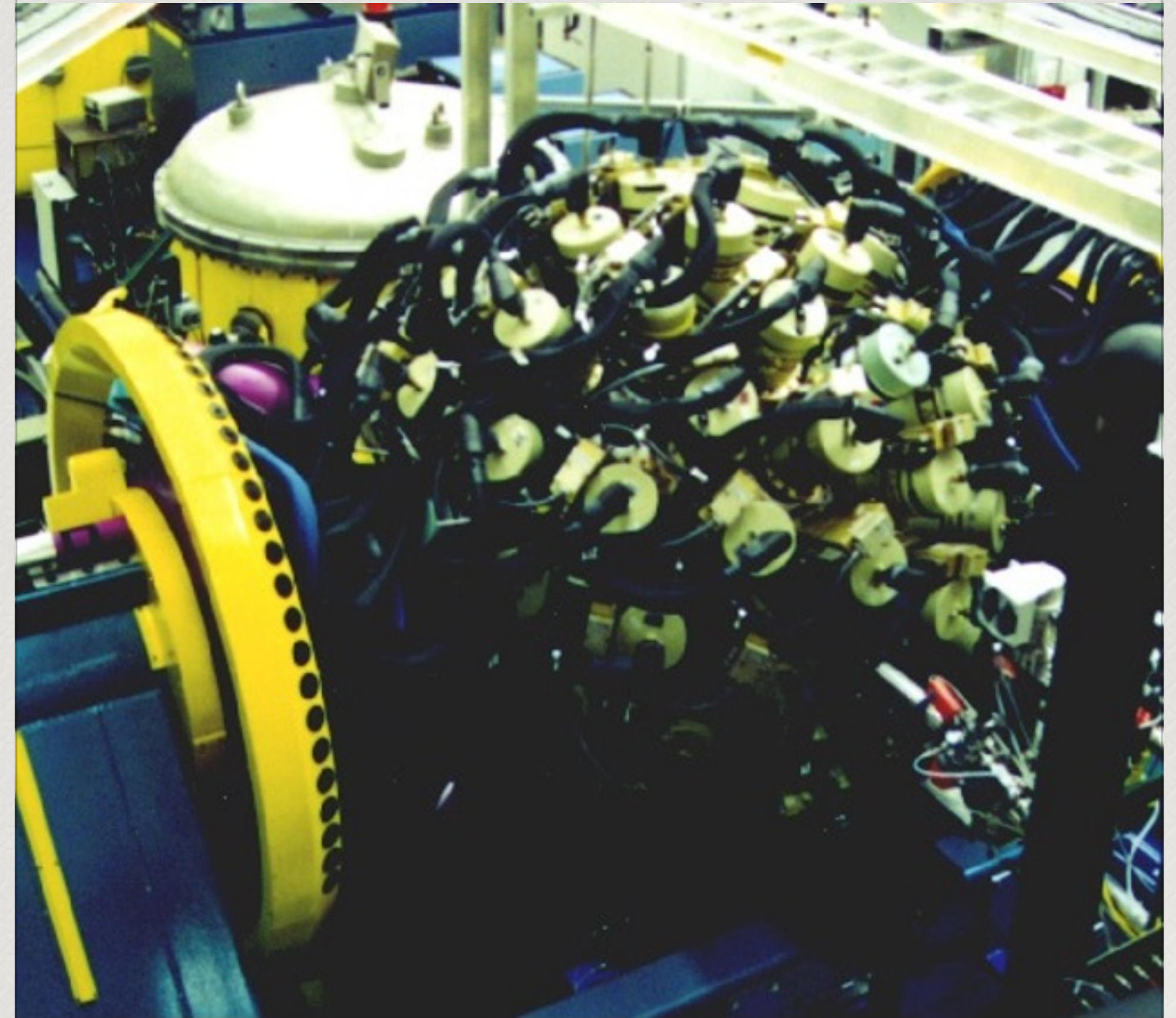
- *Energy staggering of the  $5/2[642]$  band in this region is an indicator of deformation*
- *See same trend in  $N = 95$  nuclei*
- *Maximum deformation is not at midshell ( $Z = 66$ , Dy), but appears to be located at  $Z = 60$  (Nd)*
- *Consistent with  $E(2^+)$  systematics*





# Isomers in Neutron-Rich, Rare-Earth Nuclei

- ~20 years ago, Dracoulis, Kondev, & Lane ran a series of multi-nucleon transfer reactions to produce neutron-rich nuclei that are likely to have isomers
- $^{136}\text{Xe} + ^{176}\text{Yb}$  at 820 MeV, performed at ATLAS
- 1/10 pulsing (825 ns between beam bursts)
- Gammasphere had 101 detectors operating - focus on out-of-beam





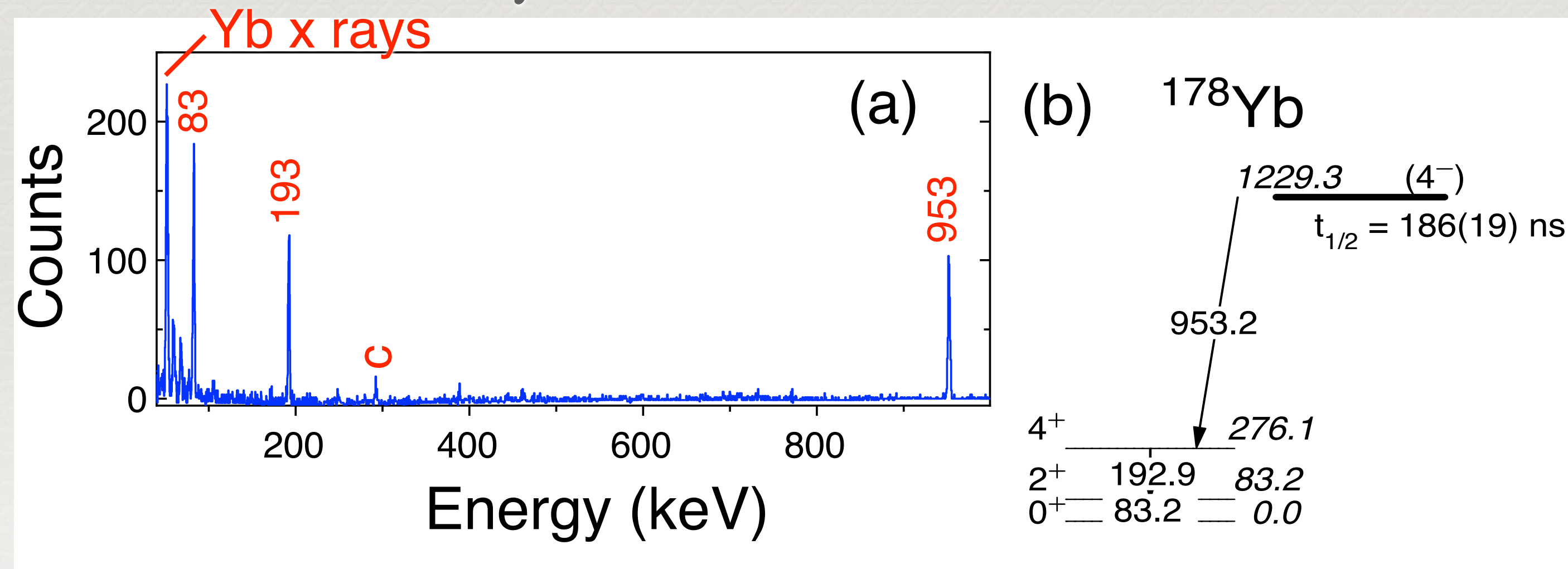
# What was made...

Neutrons	102	103	104	105	106	107	108	109	110
W					<sup>180</sup> W	<sup>181</sup> W	<sup>182</sup> W		<sup>184</sup> W
Ta			<sup>177</sup> Ta	<sup>178</sup> Ta	<sup>179</sup> Ta		<sup>181</sup> Ta		<sup>183</sup> Ta
Hf	<sup>174</sup> Hf		<sup>176</sup> Hf	<sup>177</sup> Hf	<sup>178</sup> Hf	<sup>179</sup> Hf	<sup>180</sup> Hf	<sup>181</sup> Hf	<sup>182</sup> Hf
Lu			<sup>175</sup> Lu	<sup>176</sup> Lu	<sup>177</sup> Lu	<sup>178</sup> Lu	<sup>179</sup> Lu	<sup>180</sup> Lu	
Yb	<sup>172</sup> Yb		<sup>174</sup> Yb	<sup>175</sup> Yb	<sup>176</sup> Yb	<sup>177</sup> Yb	<sup>178</sup> Yb		
Tm	<sup>171</sup> Tm	<sup>172</sup> Tm	<sup>173</sup> Tm	<sup>174</sup> Tm	<sup>175</sup> Tm				
Er	<sup>170</sup> Er		<sup>172</sup> Er	<sup>173</sup> Er	<sup>174</sup> Er				



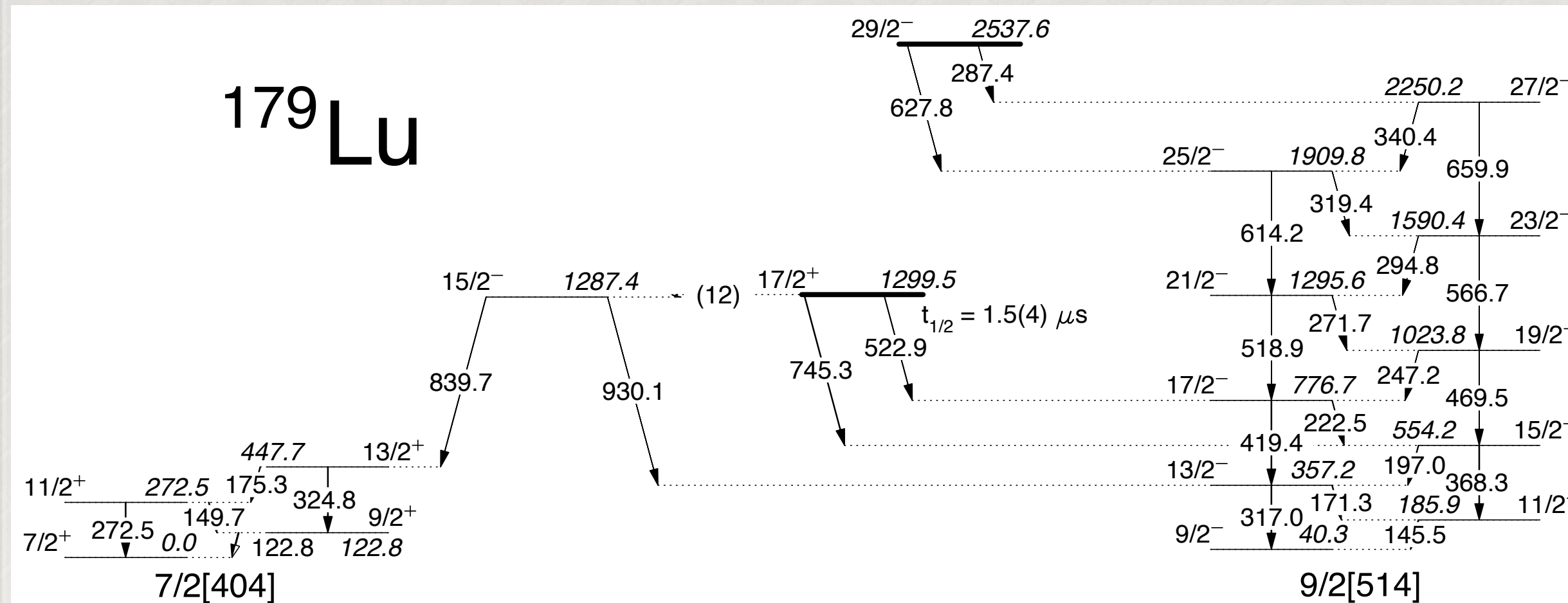
# Two-quasiparticle Isomer in $^{178}\text{Yb}$

- Most neutron-rich Yb nucleus with known excited states
- Spectra are from cube resulting from data between beam bursts
- Sum of the 83/193, 83/953, and 193/953 gates
- Observed coincident x rays are from Yb

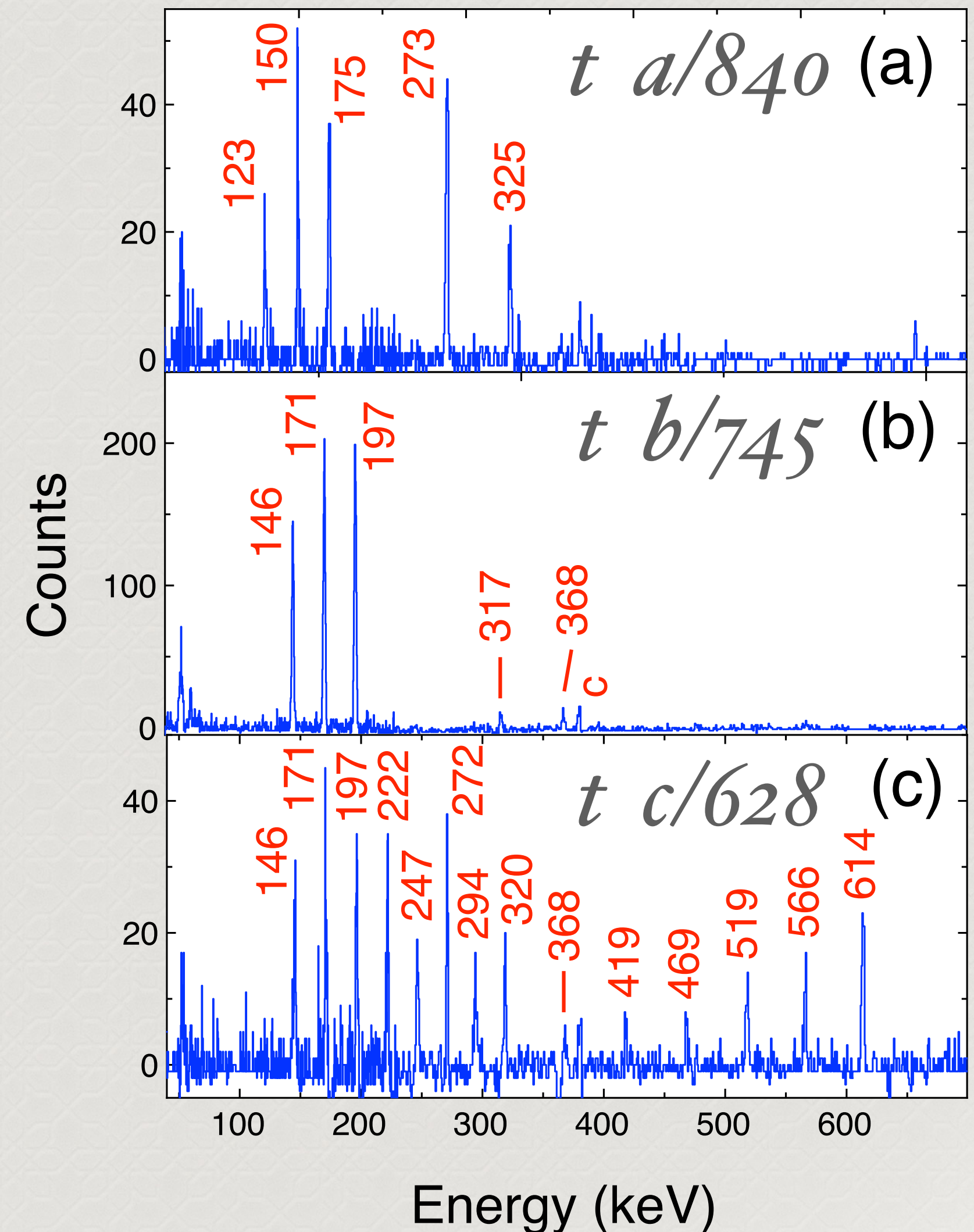




# Multiple 3-quasiparticle isomers in $^{179}\text{Lu}$



- *Most neutron-rich, odd-A Lu*
  - *No  $\gamma$ 's previously known, excited states up to  $13/2$  from proton spectra*
- Burke & Garrett, NPA **550**, 179 (1992)





# Multi-Quasiparticle Calculations

**$^{178}\text{Yb}$**

Experiment

$$\boxed{(4^-) \quad \underline{1229}}$$

Multi-QP Calculation

$$\begin{array}{cc} 5^- & 1432 \\ \hline 4^- & 1132 \\ \hline \nu(1/2^-, 9/2^+) \end{array} \quad \begin{array}{cc} 3^+ & 1438 \\ \hline \pi(1/2^+, 7/2^+) \end{array} \quad \begin{array}{cc} 6^- & 1456 \\ \hline \nu(3/2^-, 9/2^+) \end{array}$$

**$\nu(1/2[510], 9/2[624])$**

$$0^+ \quad \underline{0}$$

Experiment

$$\boxed{29/2^- \quad \underline{2538}}$$

**$^{179}\text{Lu}$**  Multi-QP Calculations

$$\boxed{\begin{array}{cc} 29/2^- & 2289 \\ \hline \pi 9/2^- \\ \nu(9/2^+, 11/2^+) \end{array}} \quad \begin{array}{cc} 27/2^+ & 2378 \\ \hline \pi 7/2^+ \\ \nu(9/2^+, 11/2^+) \end{array}$$

$$17/2^- \quad \underline{1651}$$

$$\boxed{\begin{array}{cc} 17/2^+ & 1299 \\ \hline 15/2^- & 1287 \end{array}}$$

$$\boxed{\begin{array}{cc} 15/2^- & 1250 \\ \hline \pi 7/2^+ \\ \nu(1/2^-, 9/2^+) \end{array}}$$

$$\boxed{\begin{array}{cc} 19/2^+ & 1434 \\ \hline 17/2^+ & 1277 \\ \hline \pi 9/2^- \\ \nu(1/2^-, 9/2^+) \end{array}}$$

$$\begin{array}{cc} 21/2^+ & 1566 \\ \hline \pi 9/2^- \\ \nu(3/2^-, 9/2^+) \end{array}$$

$$7/2^+ \quad \underline{0}$$



# Thank You, Robert!!

- *Have had a terrific time exploring rare-earth nuclei at high spin and not-so-high spin together*
- *You have greatly aided me in my scientific and professional endeavors*
- *You have been an advocate, a mentor, and a friend throughout the years*
- *Congratulations on your retirement!!*

*This work was supported by various grants from the NSF (PHY-2208137) and DOE (DE-AC02-06CH11357, DE-FG02-97ER41041, DE-FG02-97ER41033)*



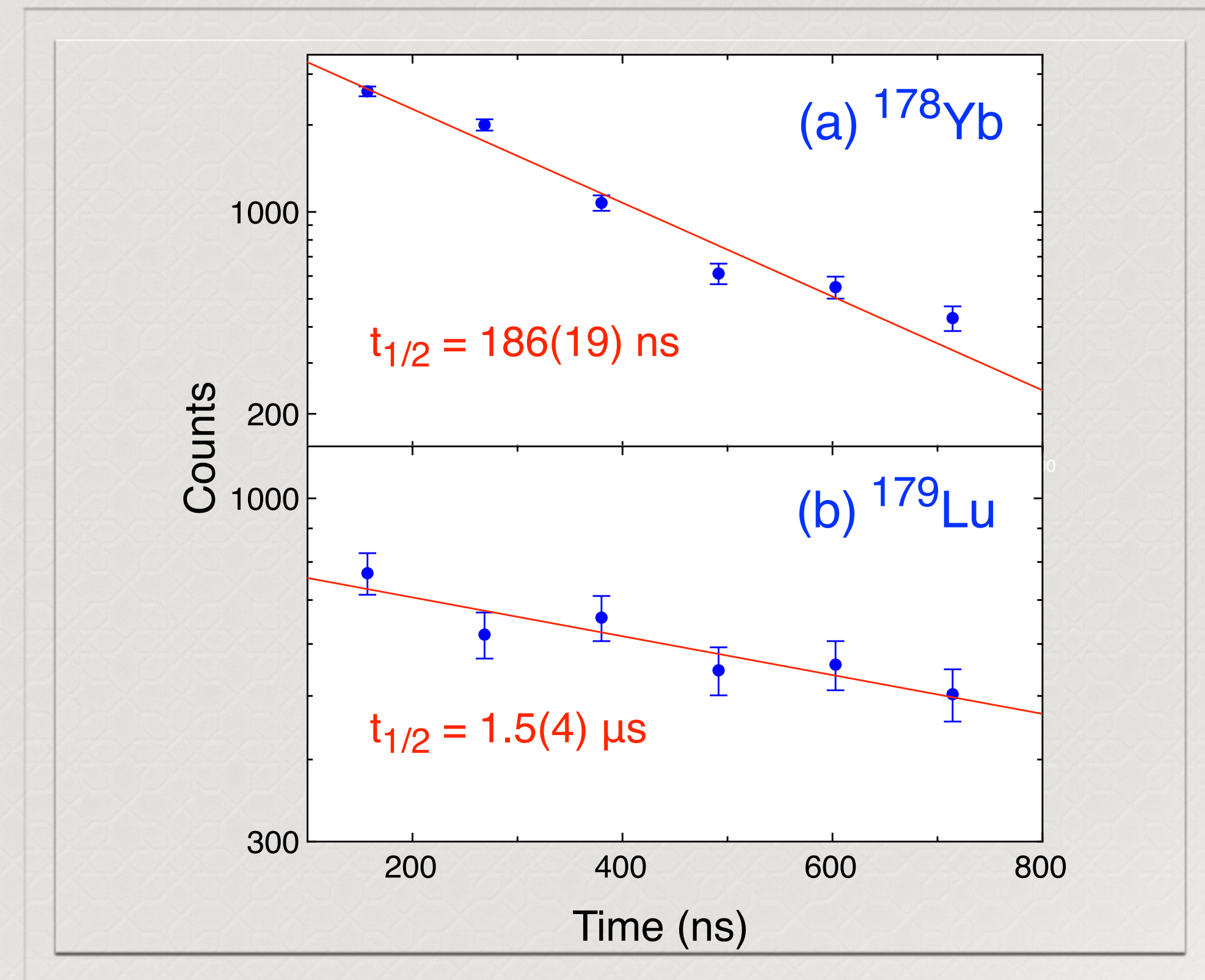
# Thank you to my many collaborators

*F. G. Kondev, M. A. Riley, L. L. Riedinger, M. P. Carpenter, G. J. Lane, G. D. Dracoulis, T. B. Brown, J. Pfohl, S. M. Fischer, D. T. Nisius, P. Fallon, W. C. Ma, J. Simpson, S. N. T. Majola, J. M. Allmond, C. W. Beausang, C. J. Chiara, N. Cooper, D. Curien, B. J. P. Gall, P. E. Garrett, W. D. Kulp, T. Lauritsen, E. A. McCutchan, D. Miller, S. Miller, J. Piot, N. Redon, J. F. Sharpey-Schafer, I. Stefanescu, X. Wang, V. Werner, J. L. Wood, C.-H. Yu, S. Zhu, J. Dudek, K. Villafana, K. Auranen, A. D. Ayangeakaa, J. S. Baron, A. J. Boston, J. A. Clark, J. P. Greene, J. Heery, C. R. Hoffman, J. Li, E. S. Paul, D. Seweryniak, S. Stolze, G. L. Wilson, J. Wu, A. P. Byrne, P. Chowdhury, H. Watanabe*



# Half lives

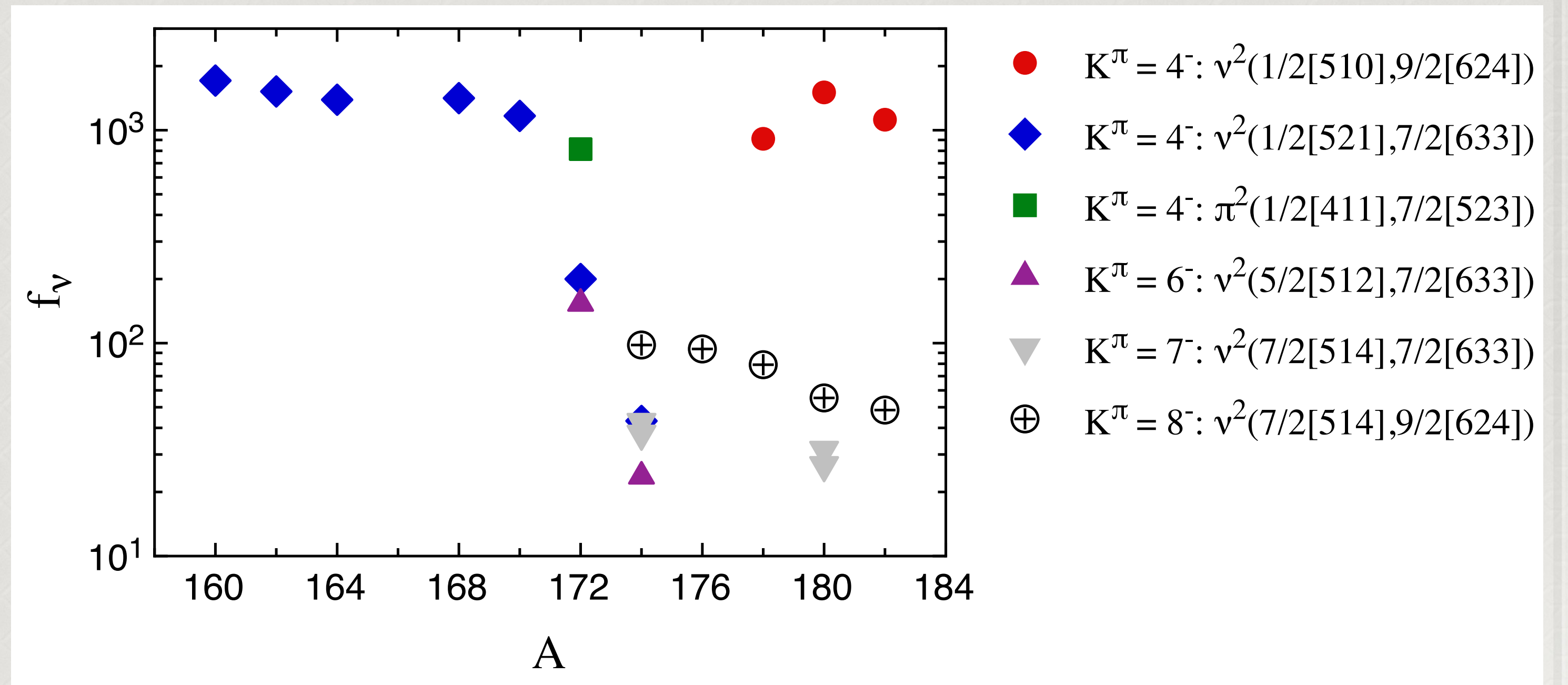
- *Six cubes were constructed dividing the out-of-beam period into  $\sim 110$  ns intervals*
- *To obtain enough statistics, a single (clean) gate was placed to track the intensity of a  $\gamma$  in the decay sequence*





# Systematics of E1 Reduced Hindrance Factors

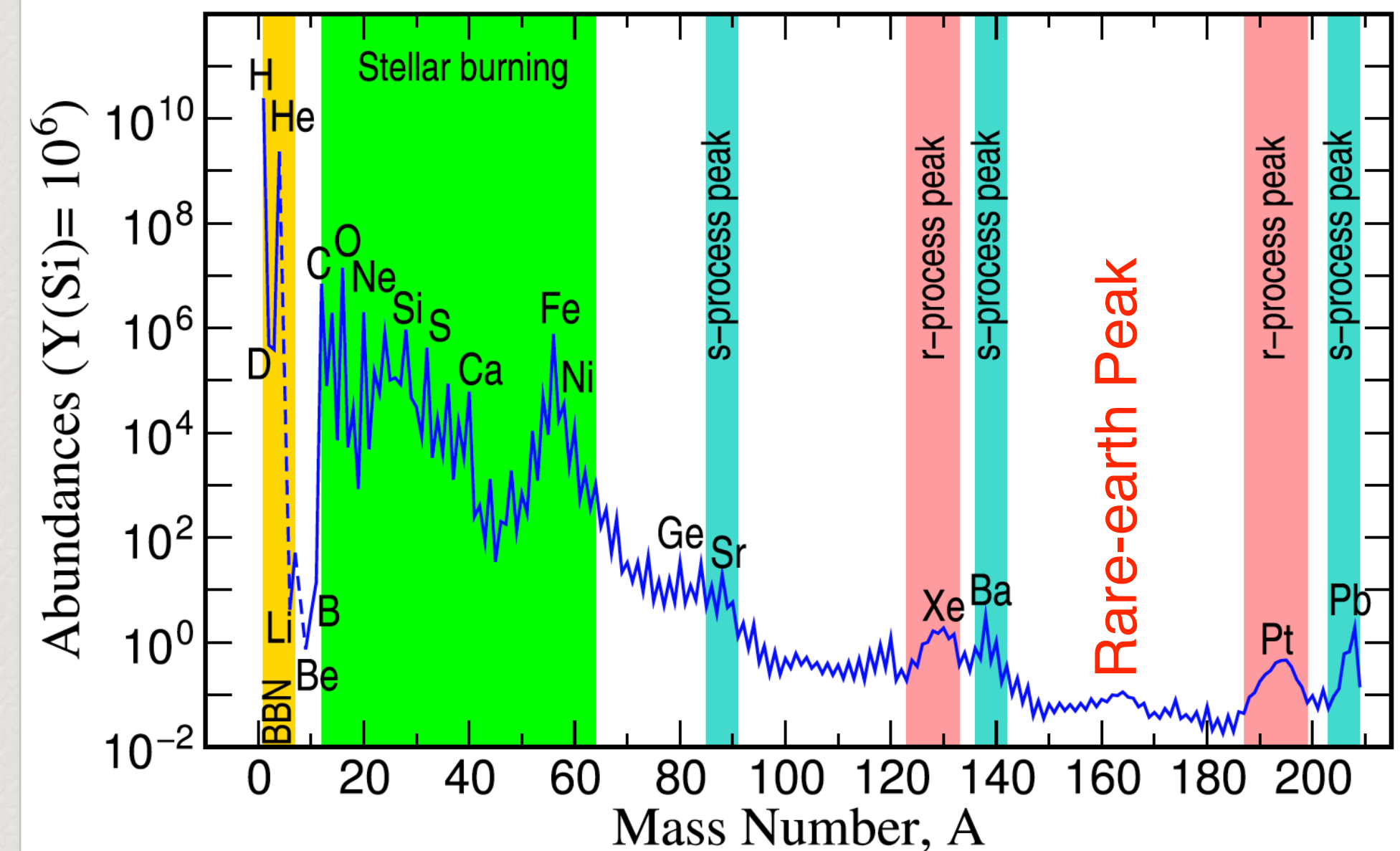
- $f_v = (t^{\gamma}_{1/2}/t^W_{1/2})^{1/v}$
- *Note that the  $K = 4$  isomers are a factor of 10 higher*
- *The re-coupling of particles is an effective*  
 $1/2[510] \rightarrow 9/2[624]$   
*transition*
- *This  $\Delta K = \Delta \Lambda = 4$  transition is greatly hindered by Alaga*





# On to (kinda) new things

- *Understand conditions to sustain  $r$ -process*
- *Reproducing the rare-earth peak may be a key component to this understanding*
- *~20 years ago, Dracoulis, Kondev, & Lane ran a series of multi-nucleon transfer reactions to produce neutron-rich nuclei that are likely to have isomers*



*J. J. Cowan et al., Rev. Mod. Phys. 93, 015002 (2021)*