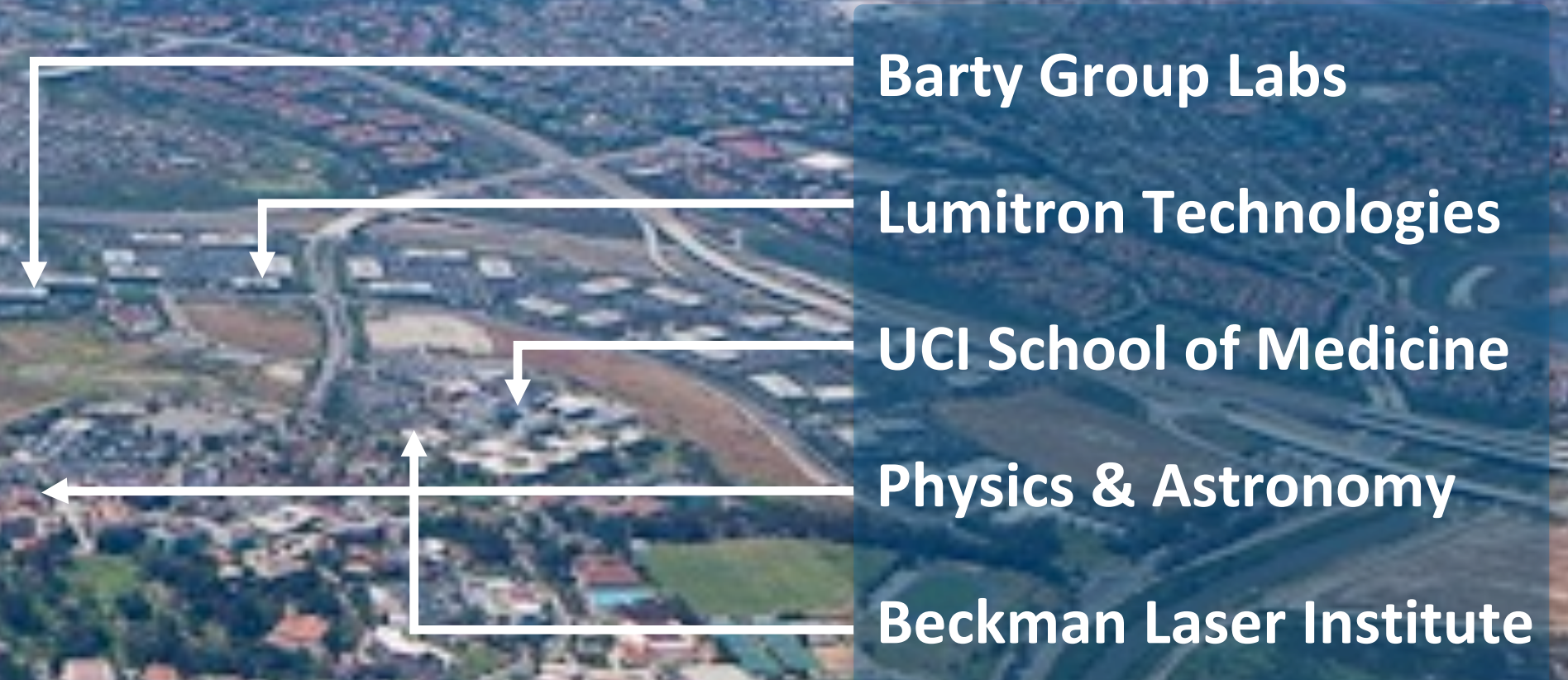
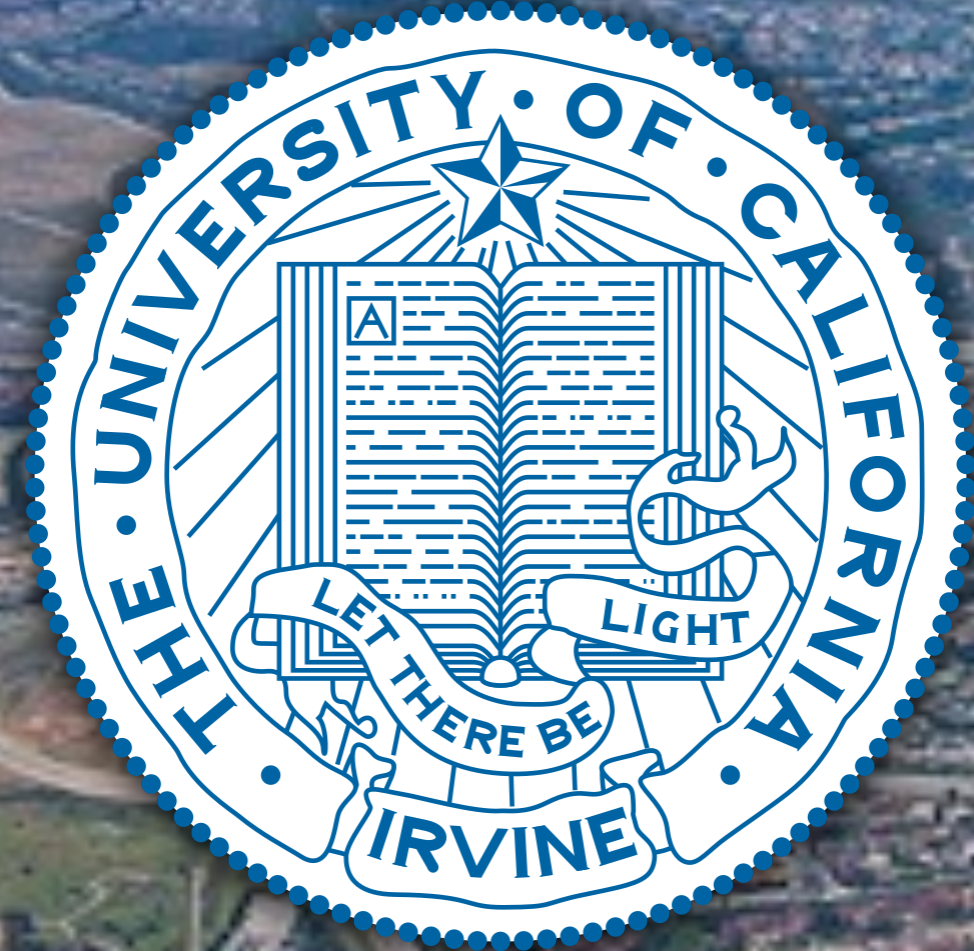


2D and 3D Imaging by Nuclear Resonance Absorption/Fluorescence Using Extremely Brilliant Compton Sources

Newport Beach

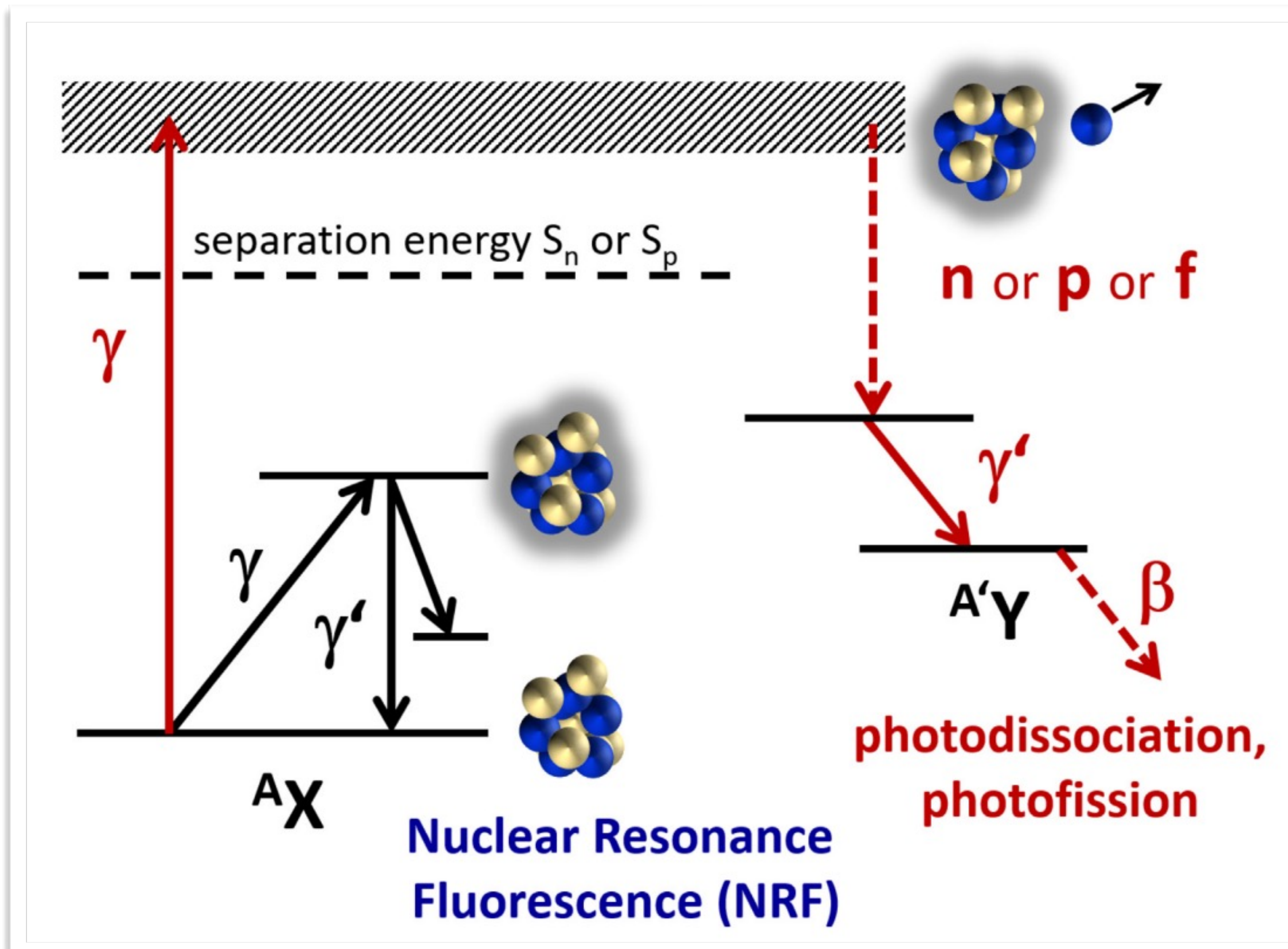


Trevor Reutershan and Prof. CPJ Barty

Medical Scientist Training Program (MD/PhD)
Department of Physics and Astronomy
Barty Research Group

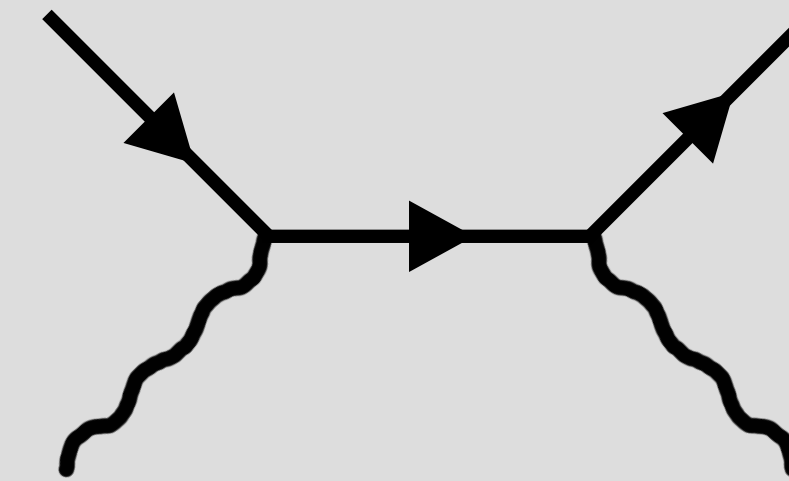
Nuclear Photonics 2023 : Durham, North Carolina : September 11th, 2023

Nuclear Resonance Absorption and Fluorescence

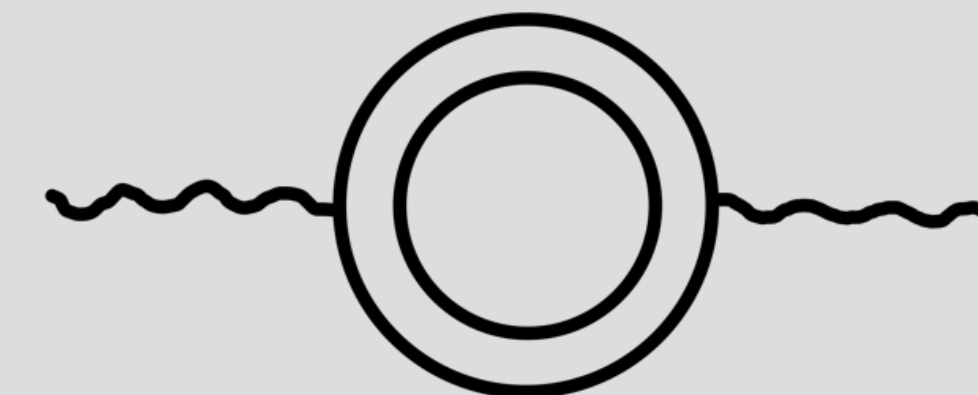


Other interactions include:

- Nuclear Thomson/Compton Scattering

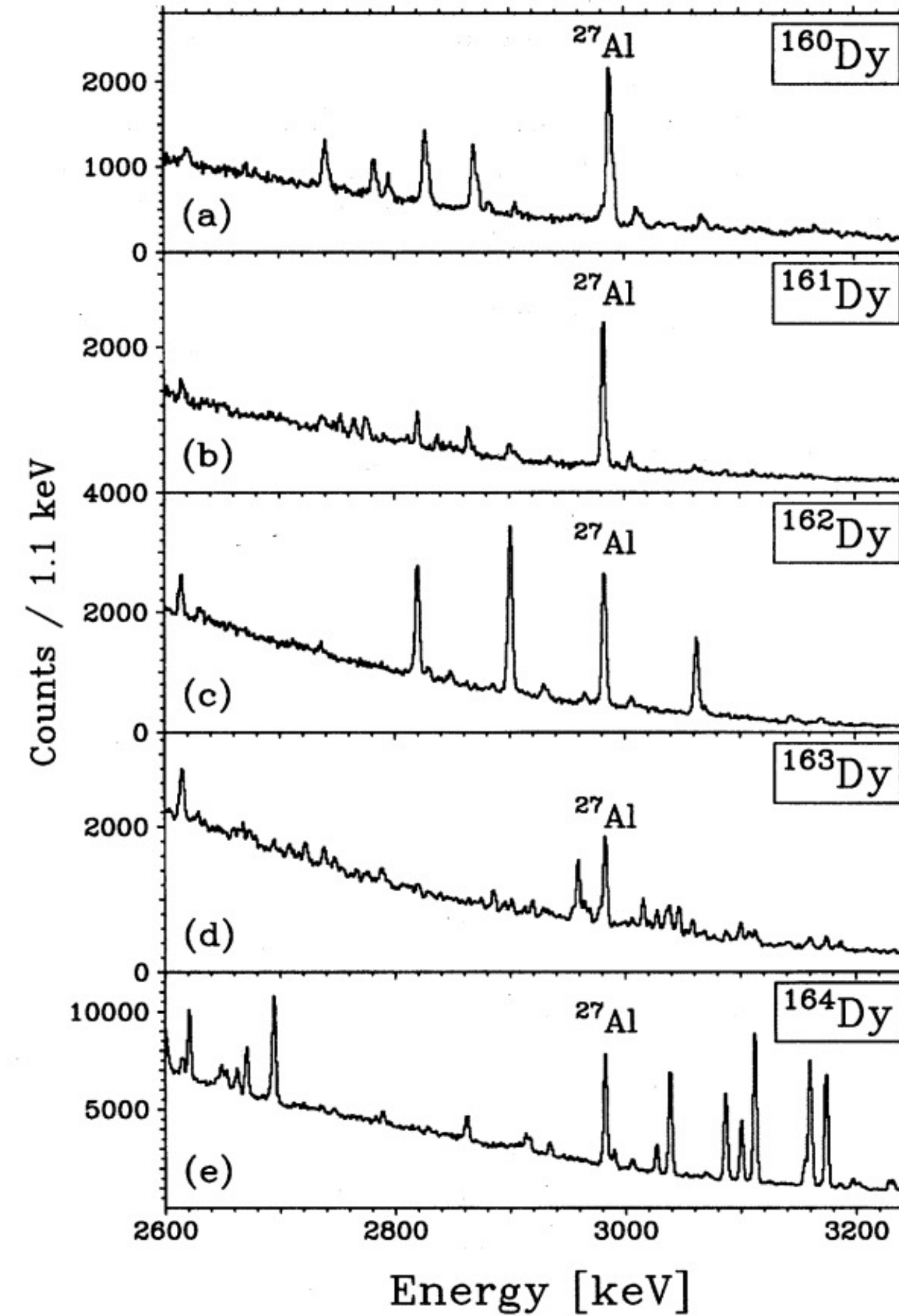
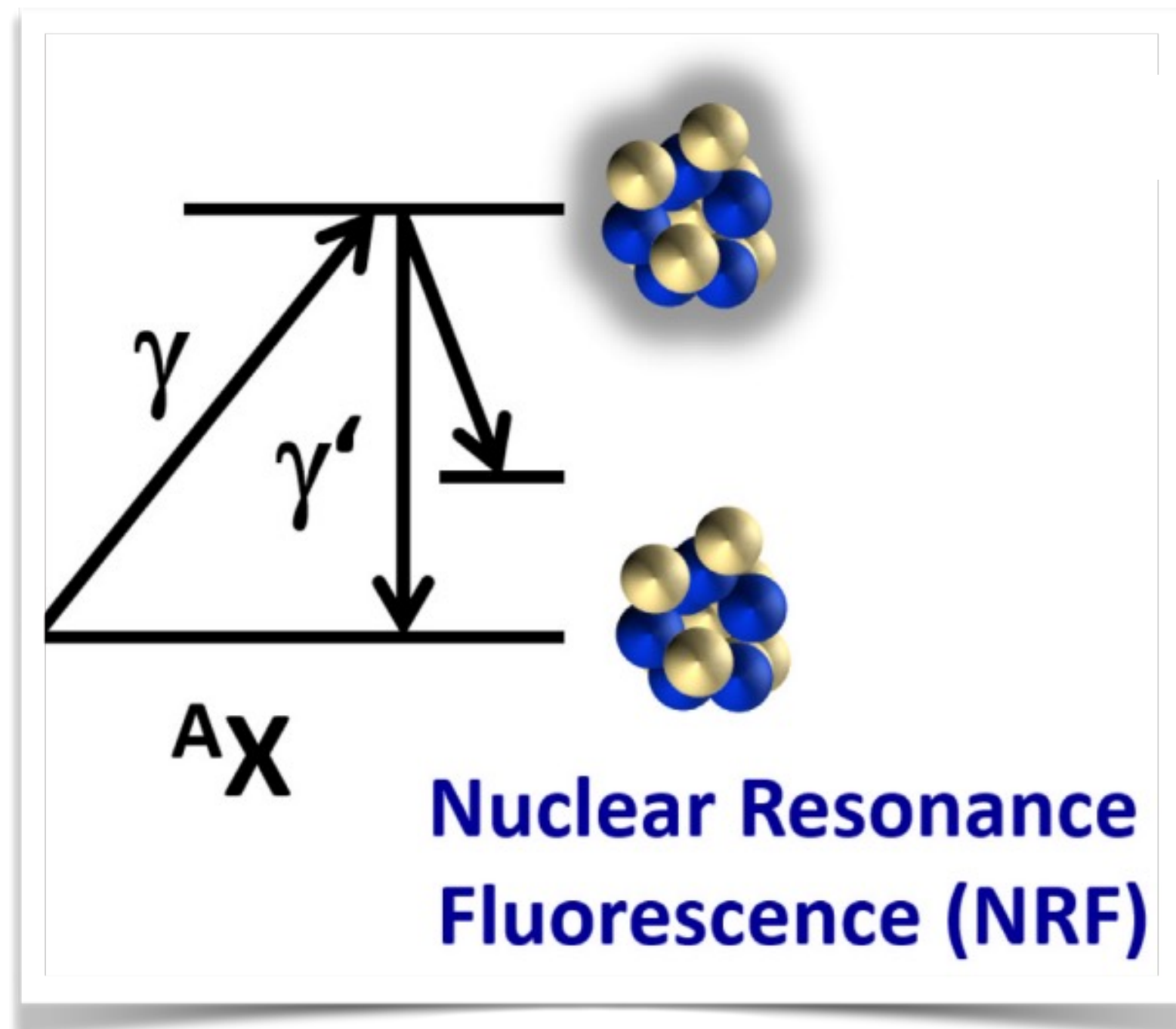


- Delbrück Scattering

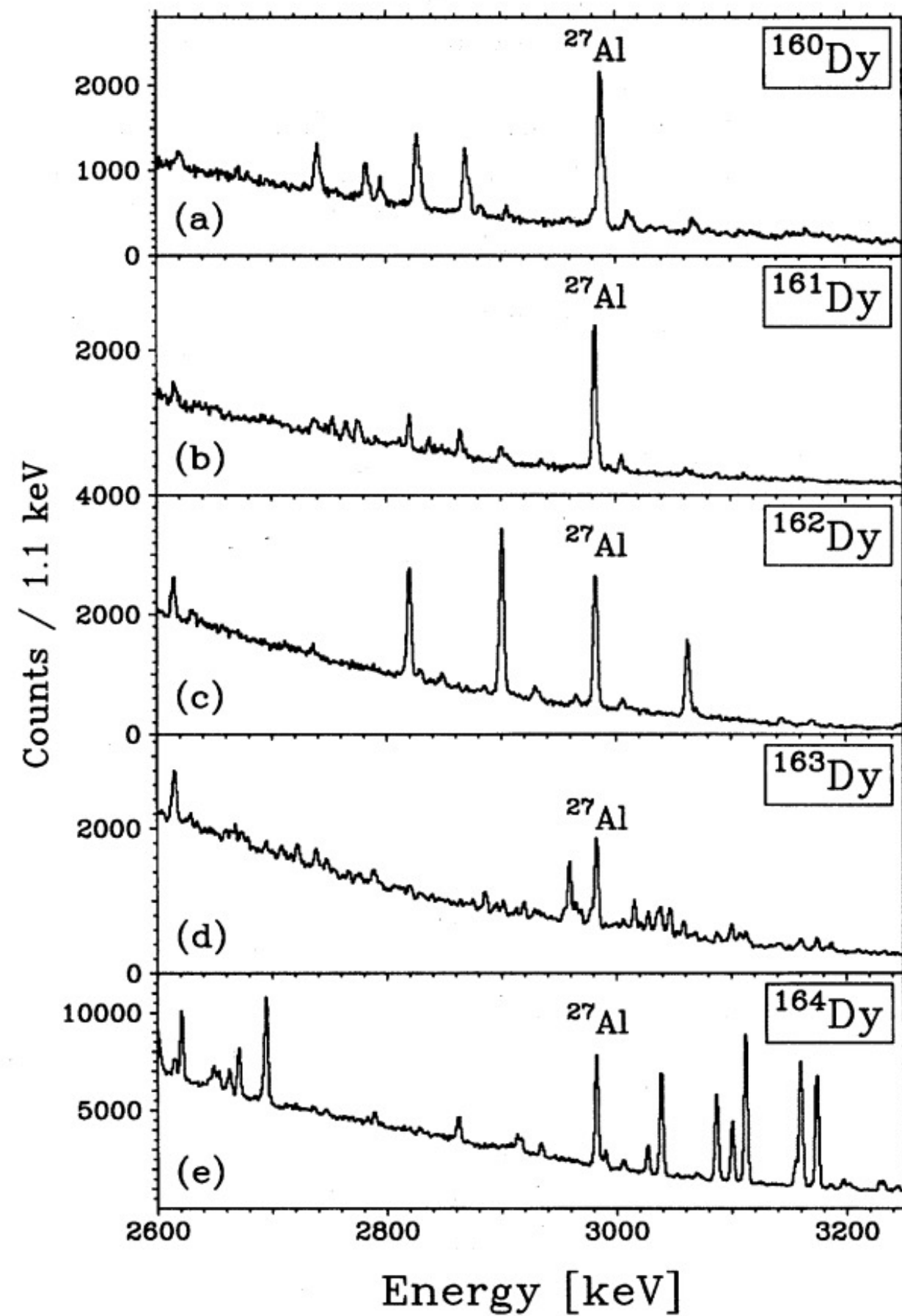


Photon scattering processes with the nucleus

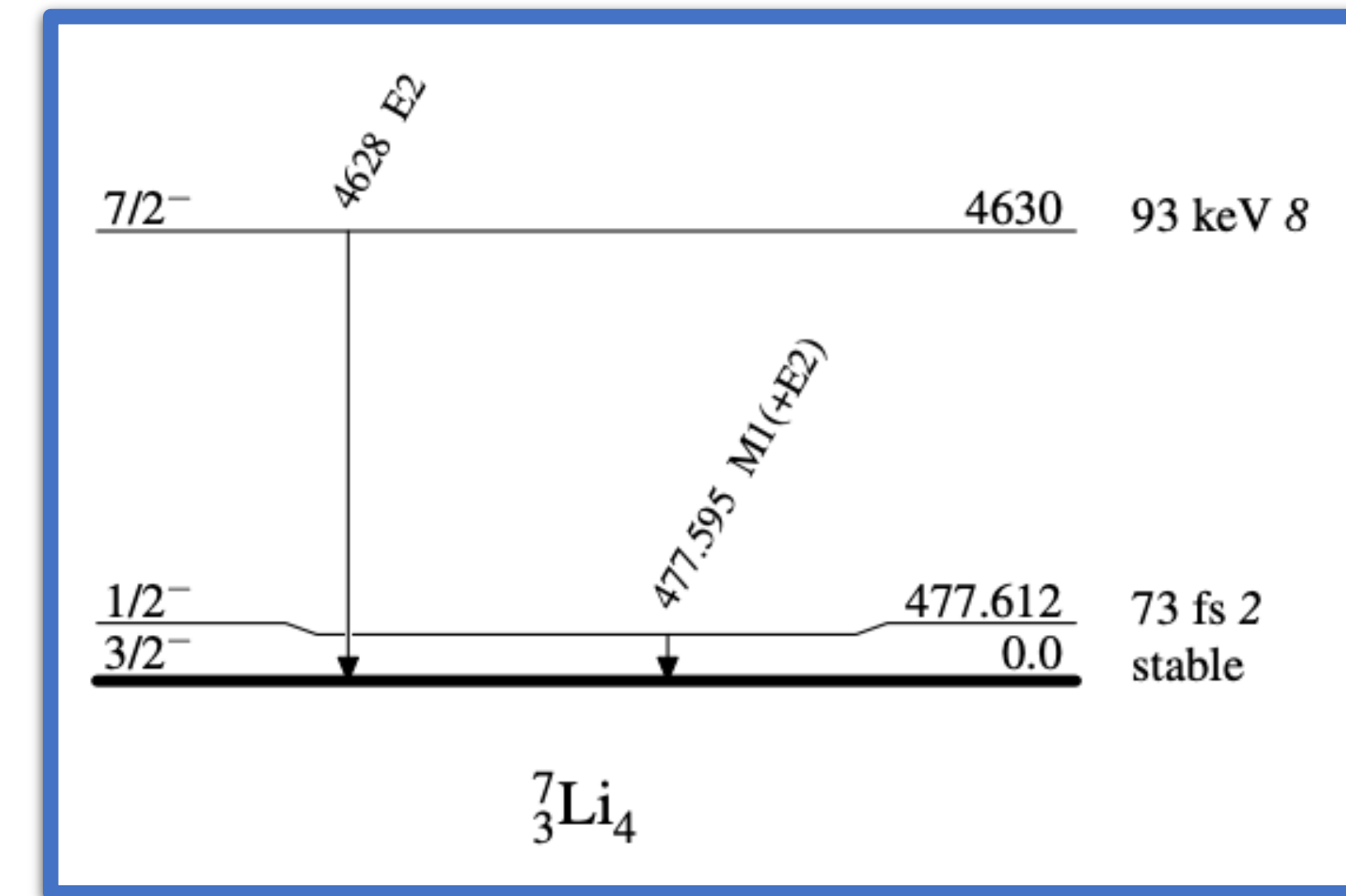
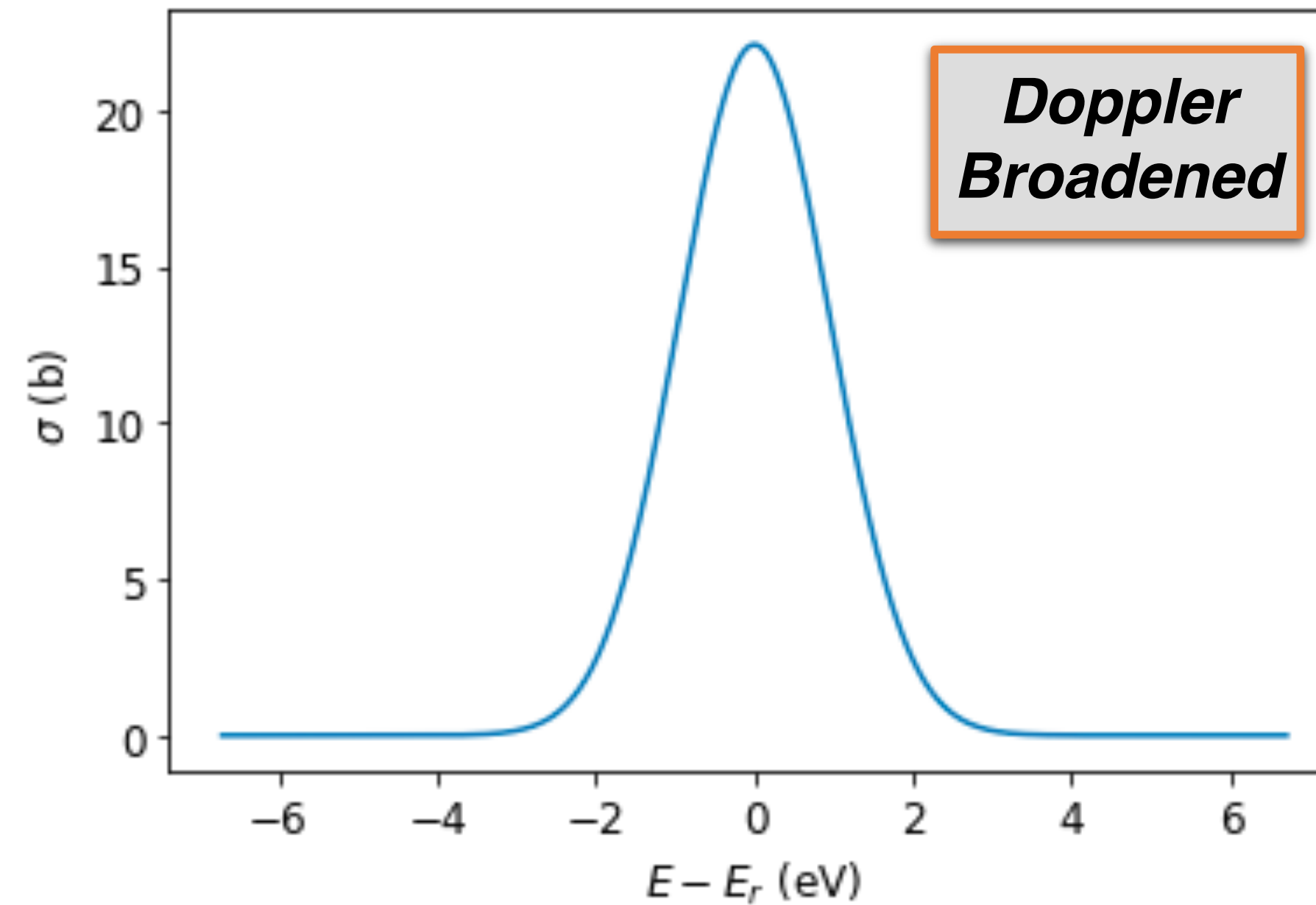
Energy Levels Are Unique to the Isotope



A Narrow Phenomenon...

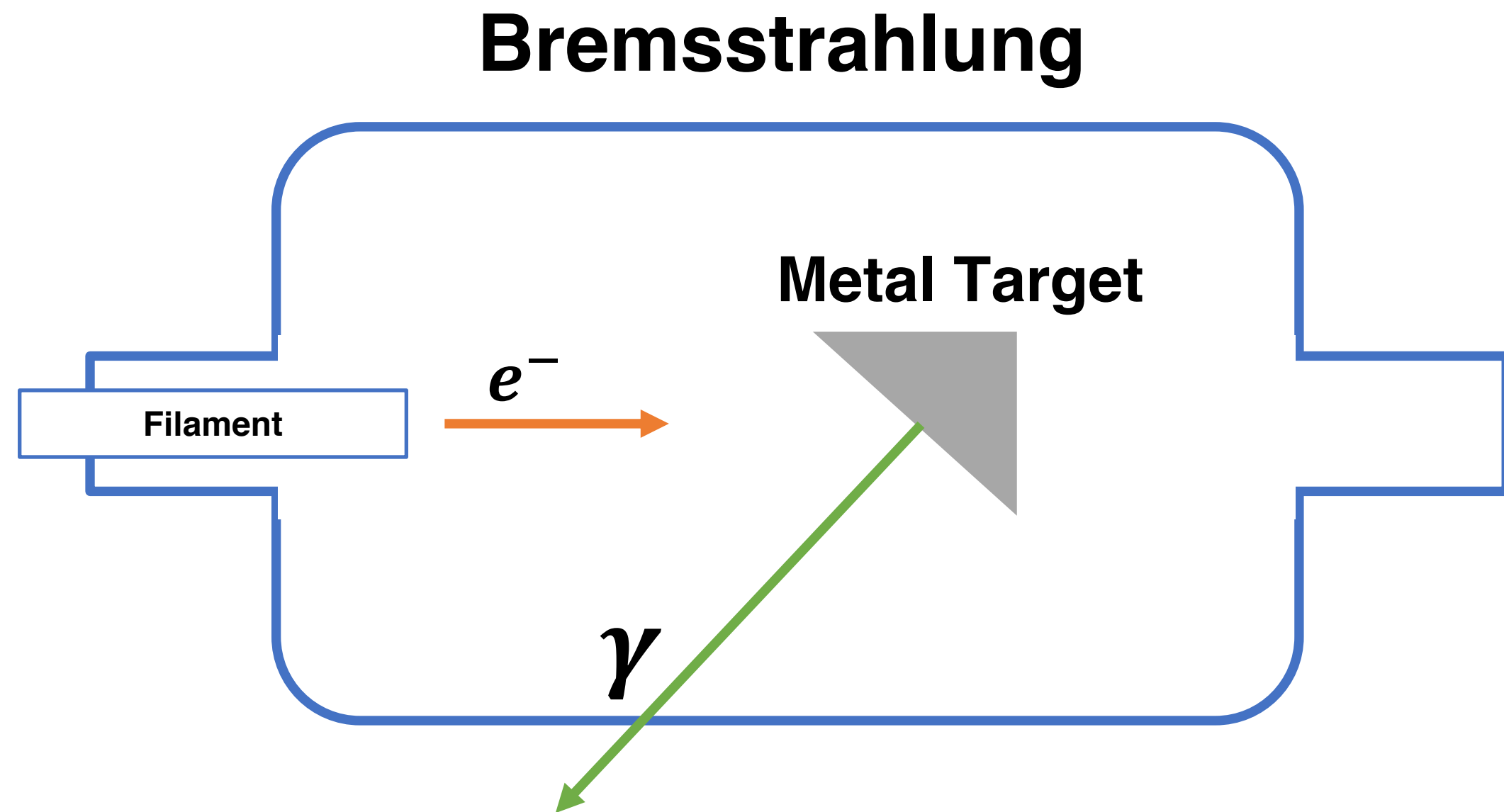


$$\frac{\Delta E}{E} ({}^7\text{Li}) = 4.69 \times 10^{-6}$$

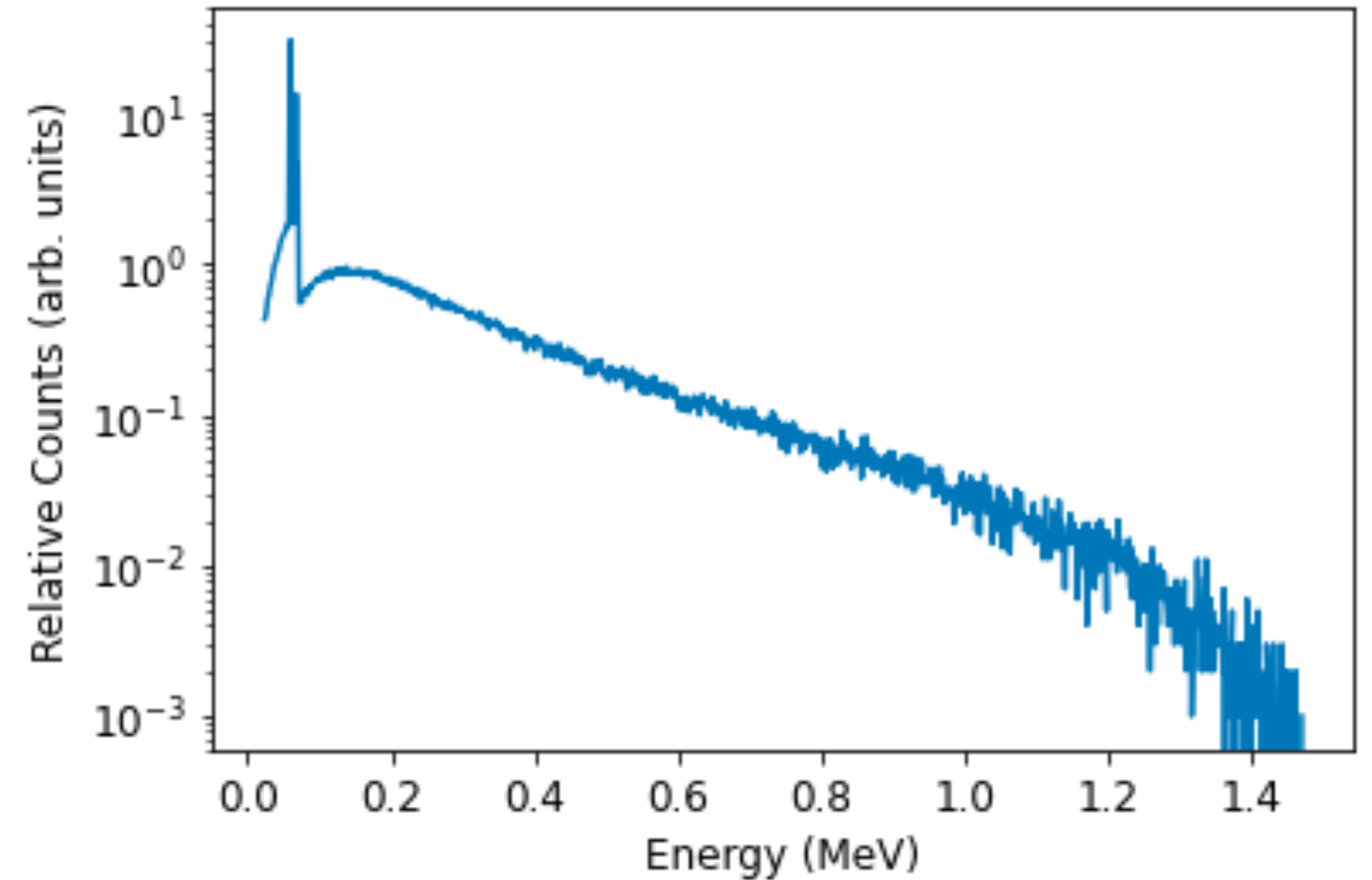


Line widths can be as low as $10^{-6} \Delta E/E$

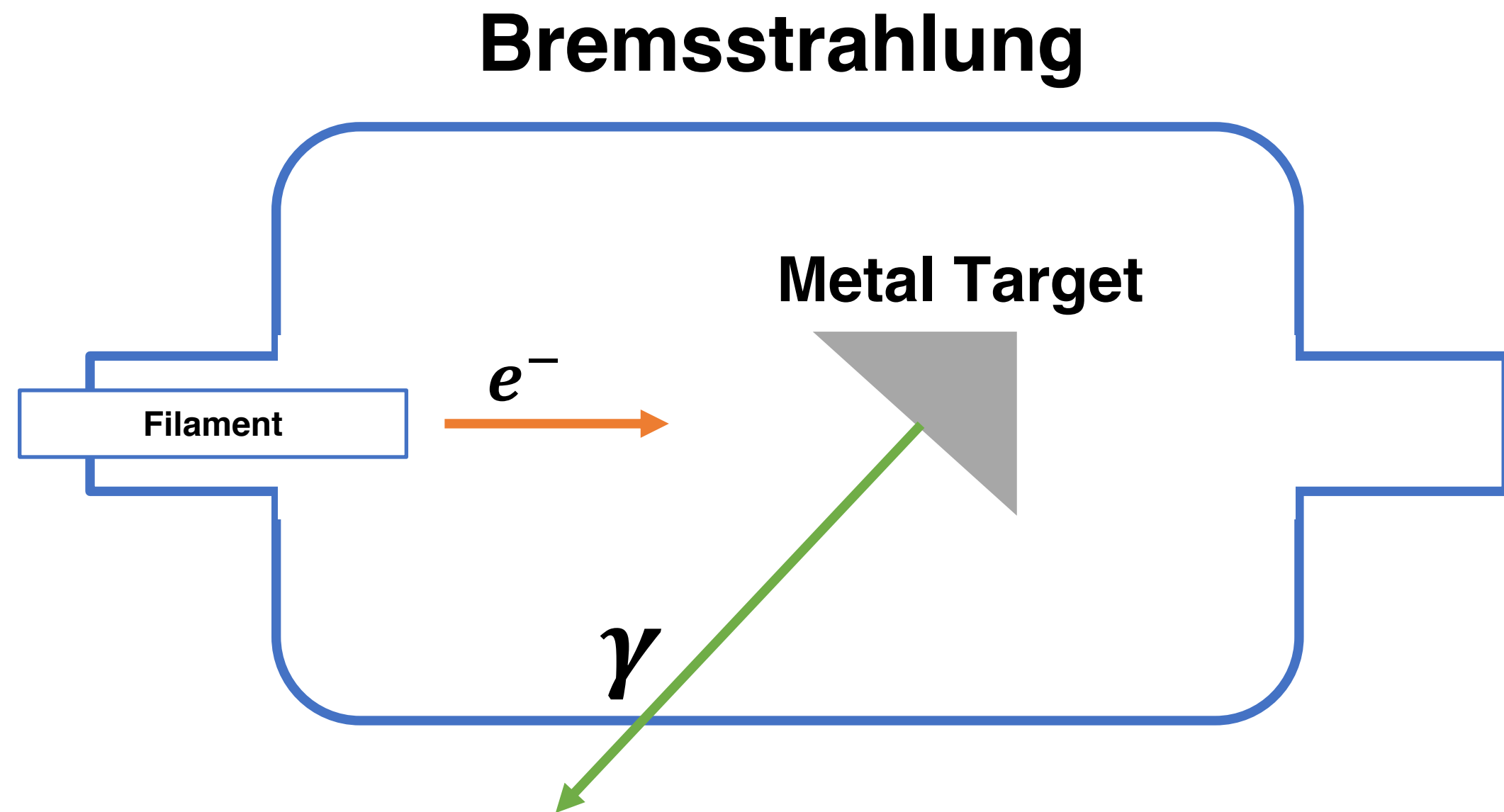
How NRF Experiments are Typically Done



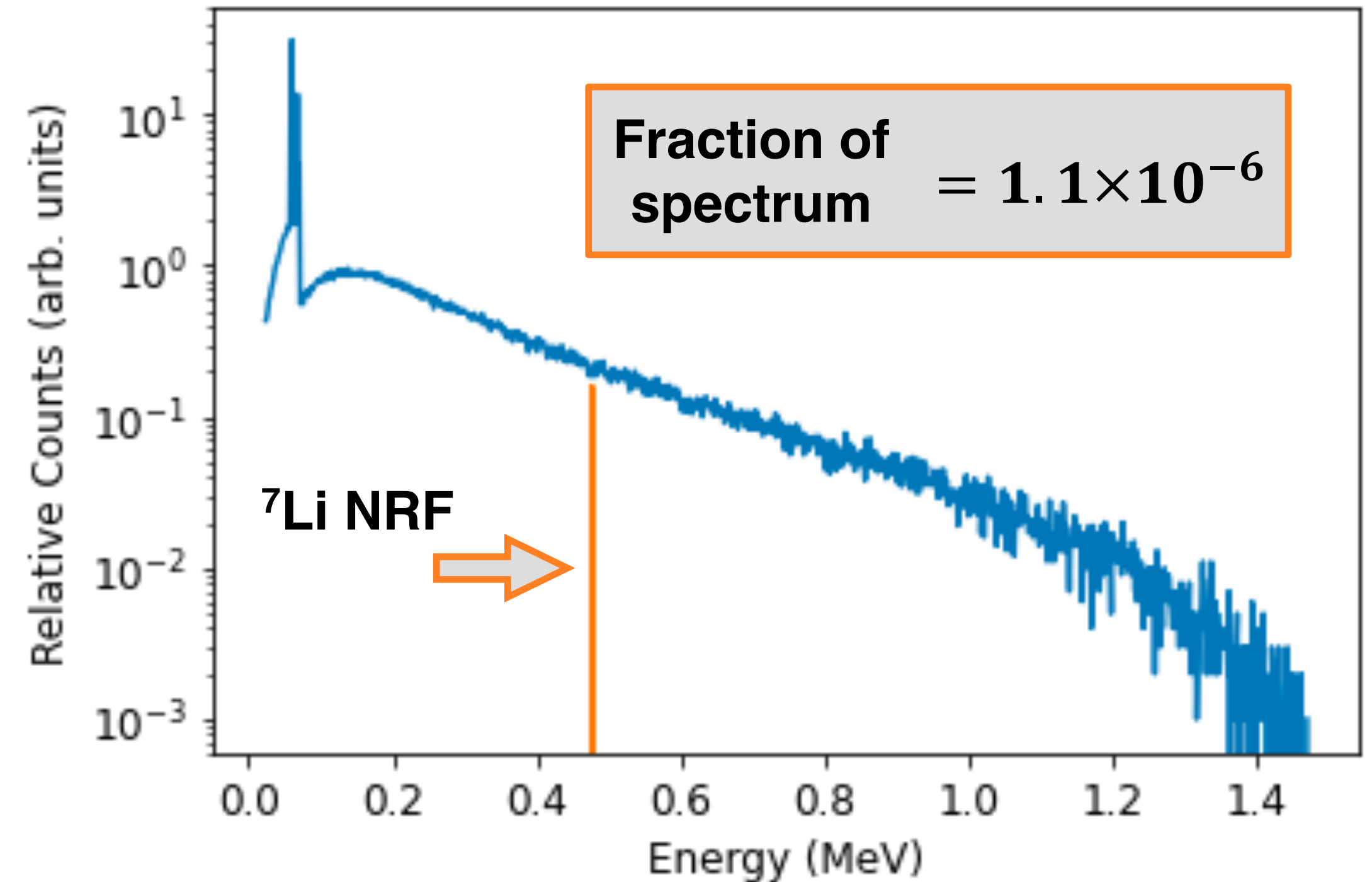
1.5 MeV Tungsten Spectrum



How NRF Experiments are Typically Done



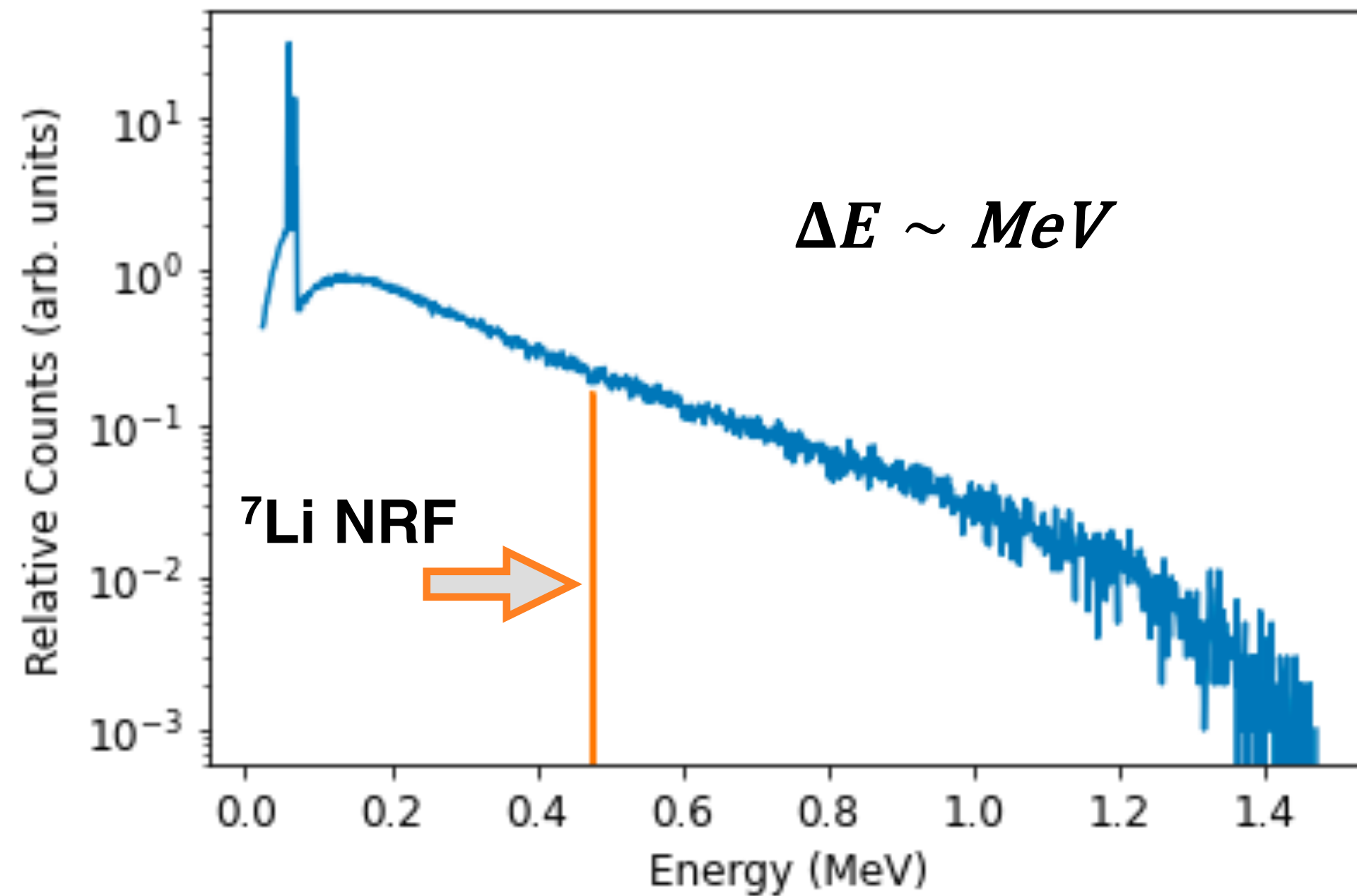
1.5 MeV Tungsten Spectrum



Not an ideal source for single resonance line measurements

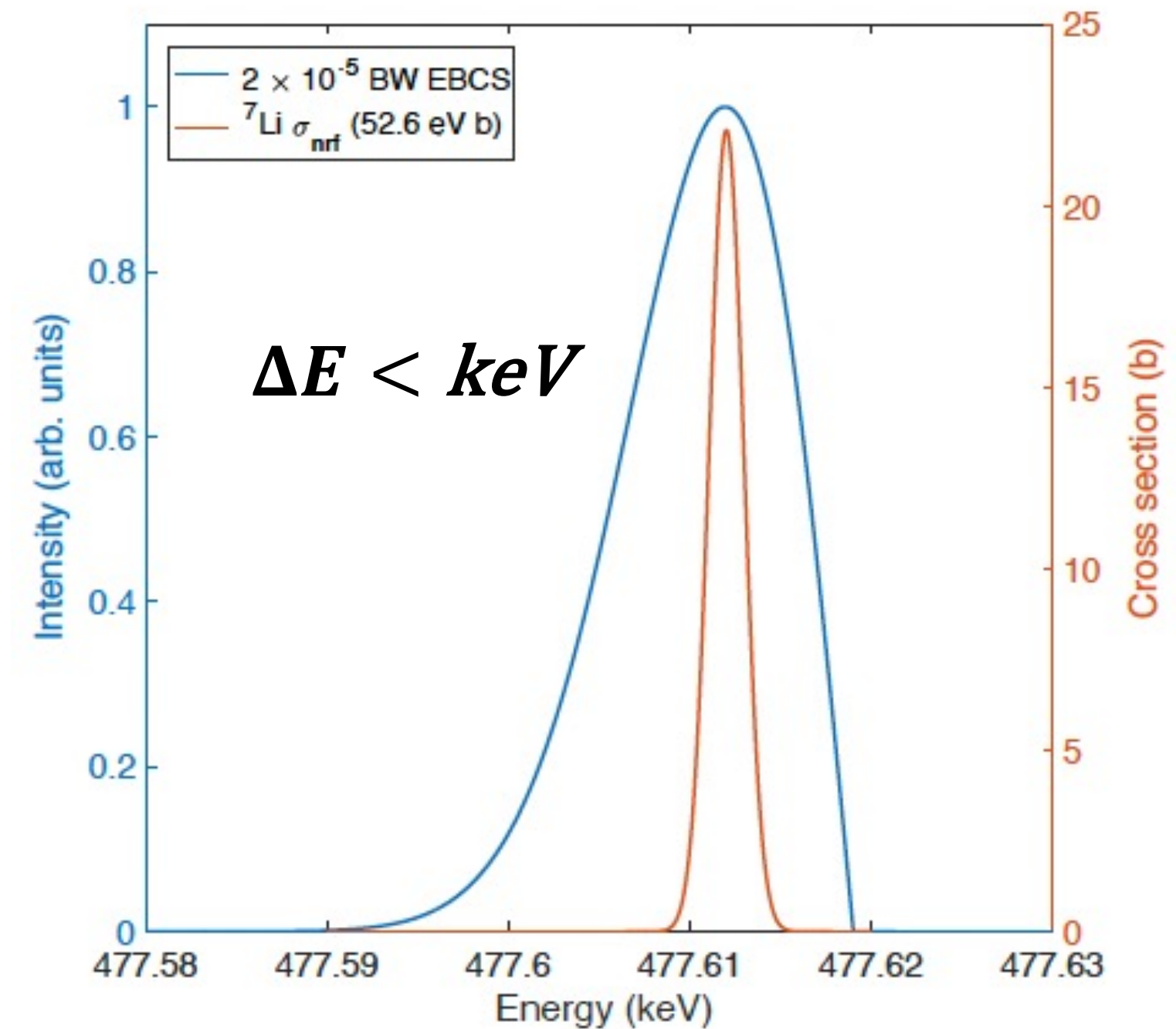
Laser-Compton Scattering has the Edge

Bremsstrahlung



Fraction of spectrum = 1.1×10^{-6}

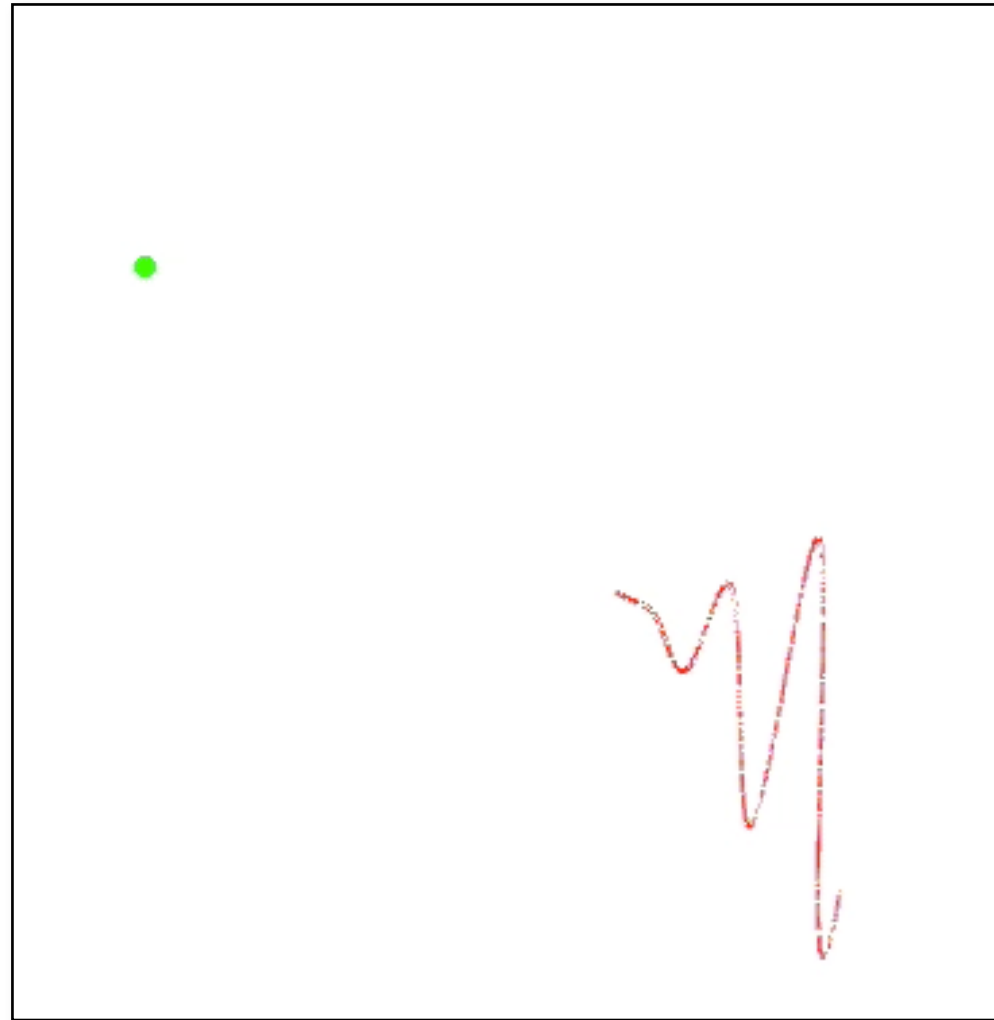
LCS



Fraction of spectrum = 0.21

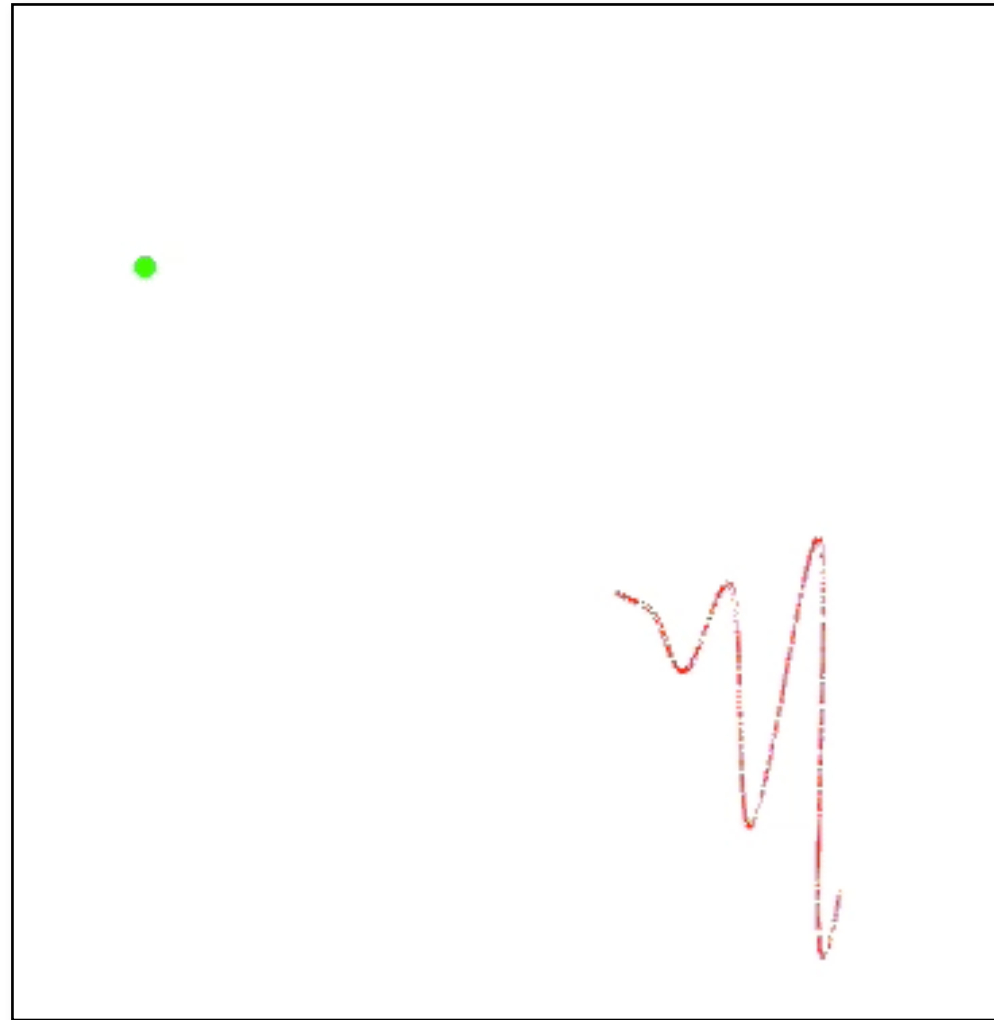
LCS has narrow bandwidths that make probing these lines much better

Laser-Compton Source



$$E_{\gamma} = \frac{4\gamma^2}{1 + \gamma^2\theta^2 + 4\gamma k_0 \lambda_c} E_L$$

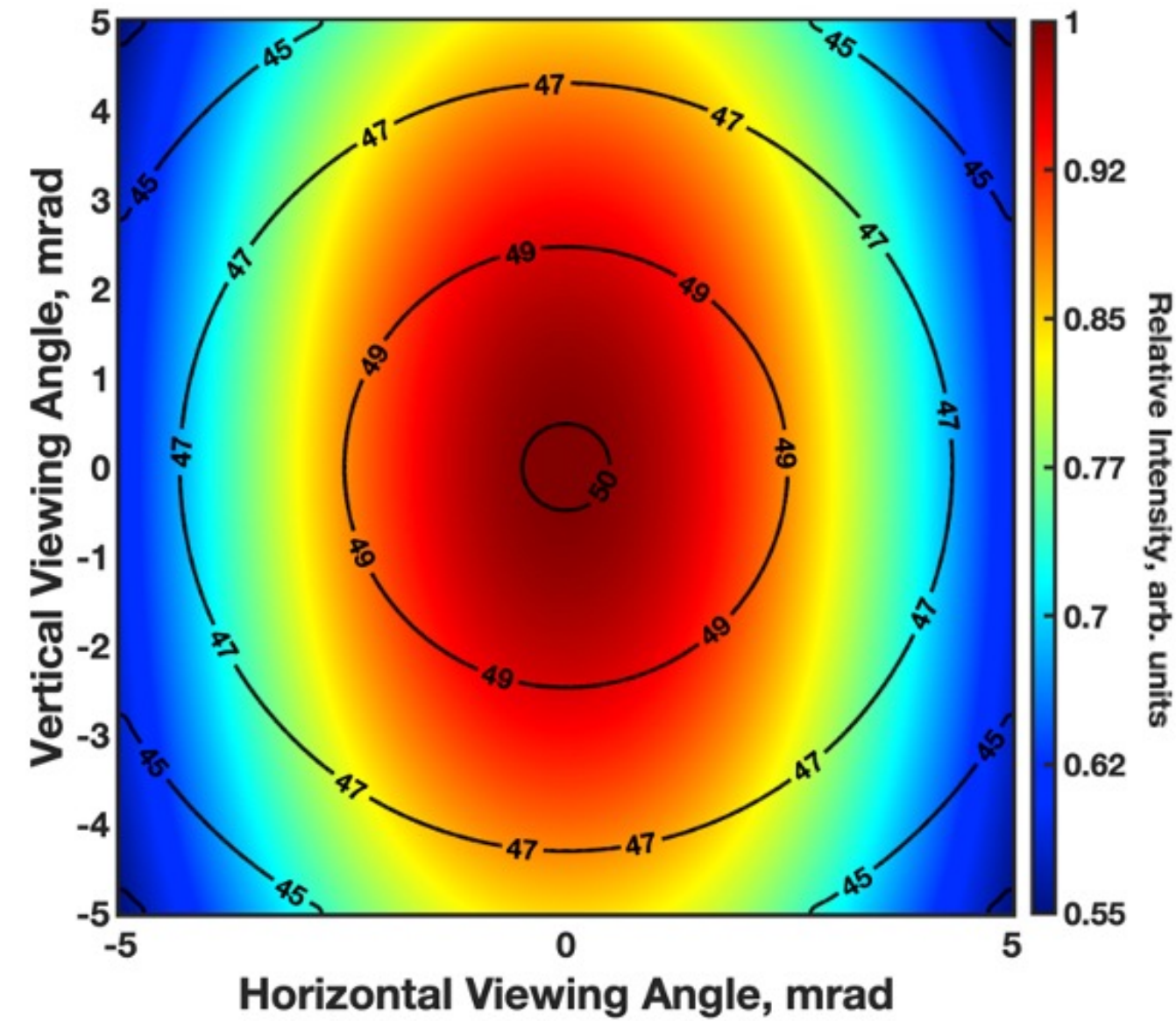
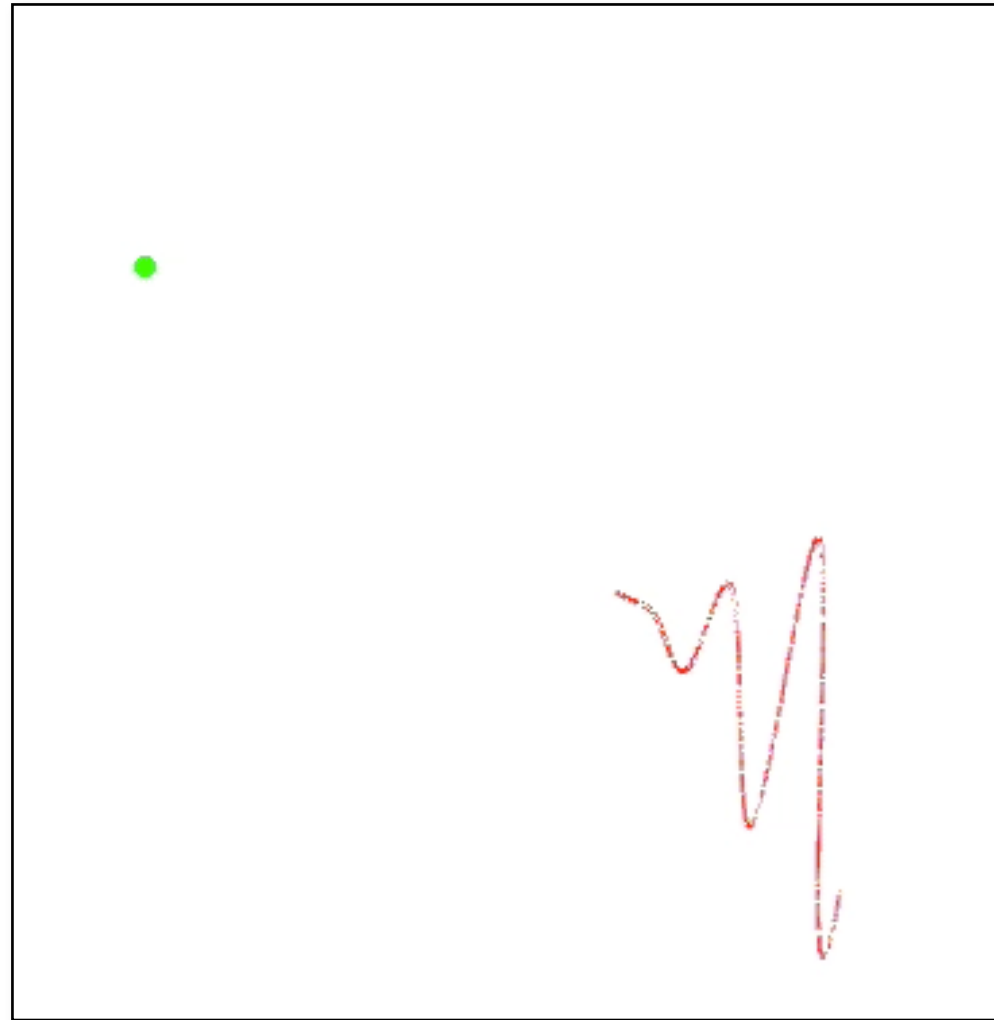
Laser-Compton Source



Double Doppler
upshift

$$E_{\gamma} = \frac{4\gamma^2}{1 + \gamma^2\theta^2 + 4\gamma k_0 \lambda_c} E_L$$

Laser-Compton Source

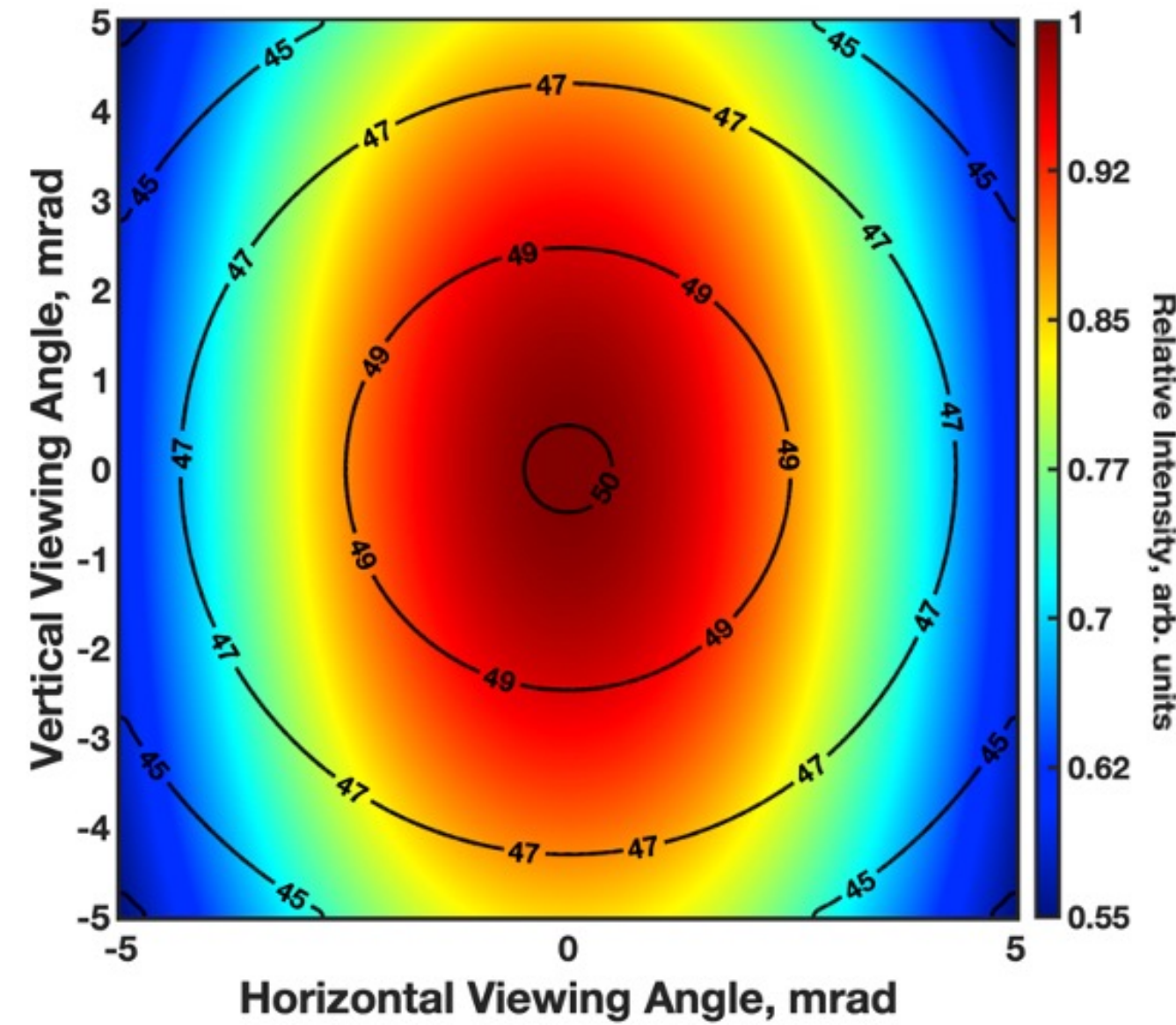
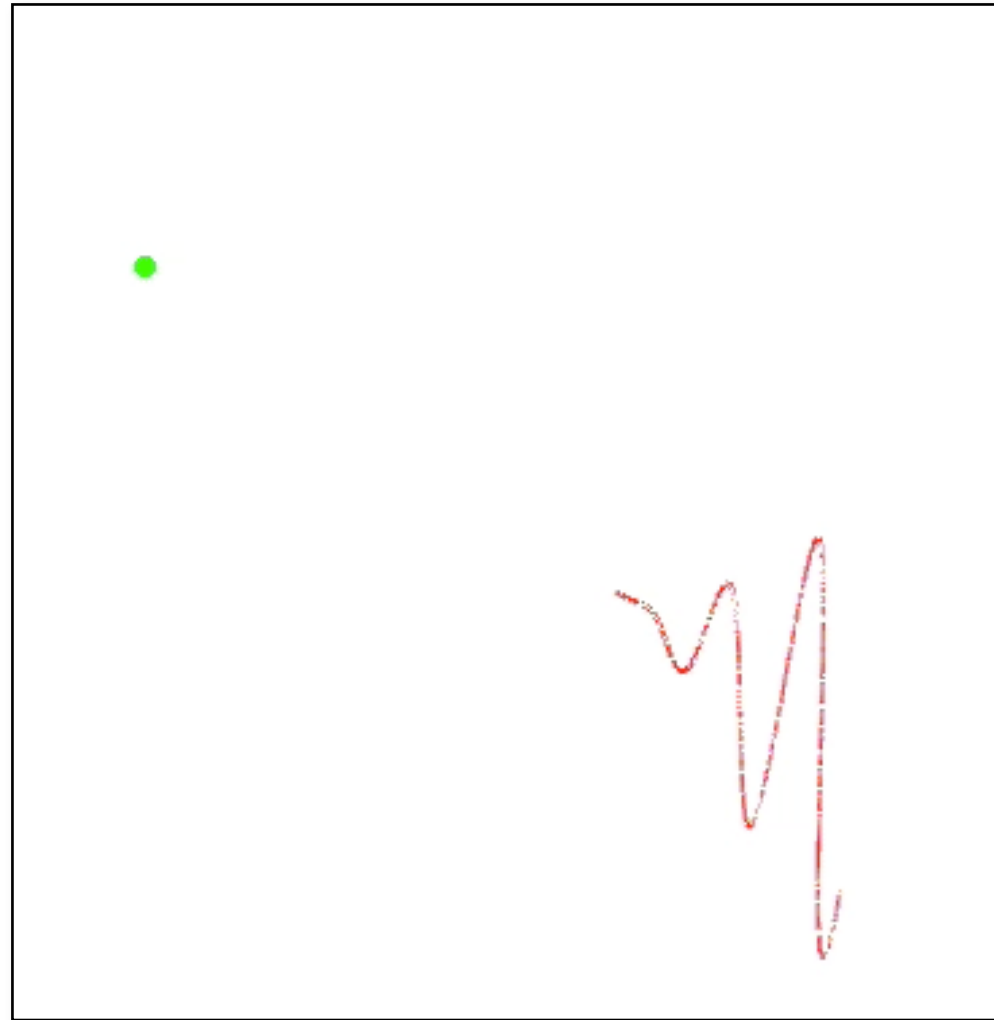


Double Doppler
upshift

$$E_\gamma = \frac{4\gamma^2}{1 + \gamma^2\theta^2 + 4\gamma k_0^- \lambda_c} E_L$$

Angle correlated
spectrum

Laser-Compton Source

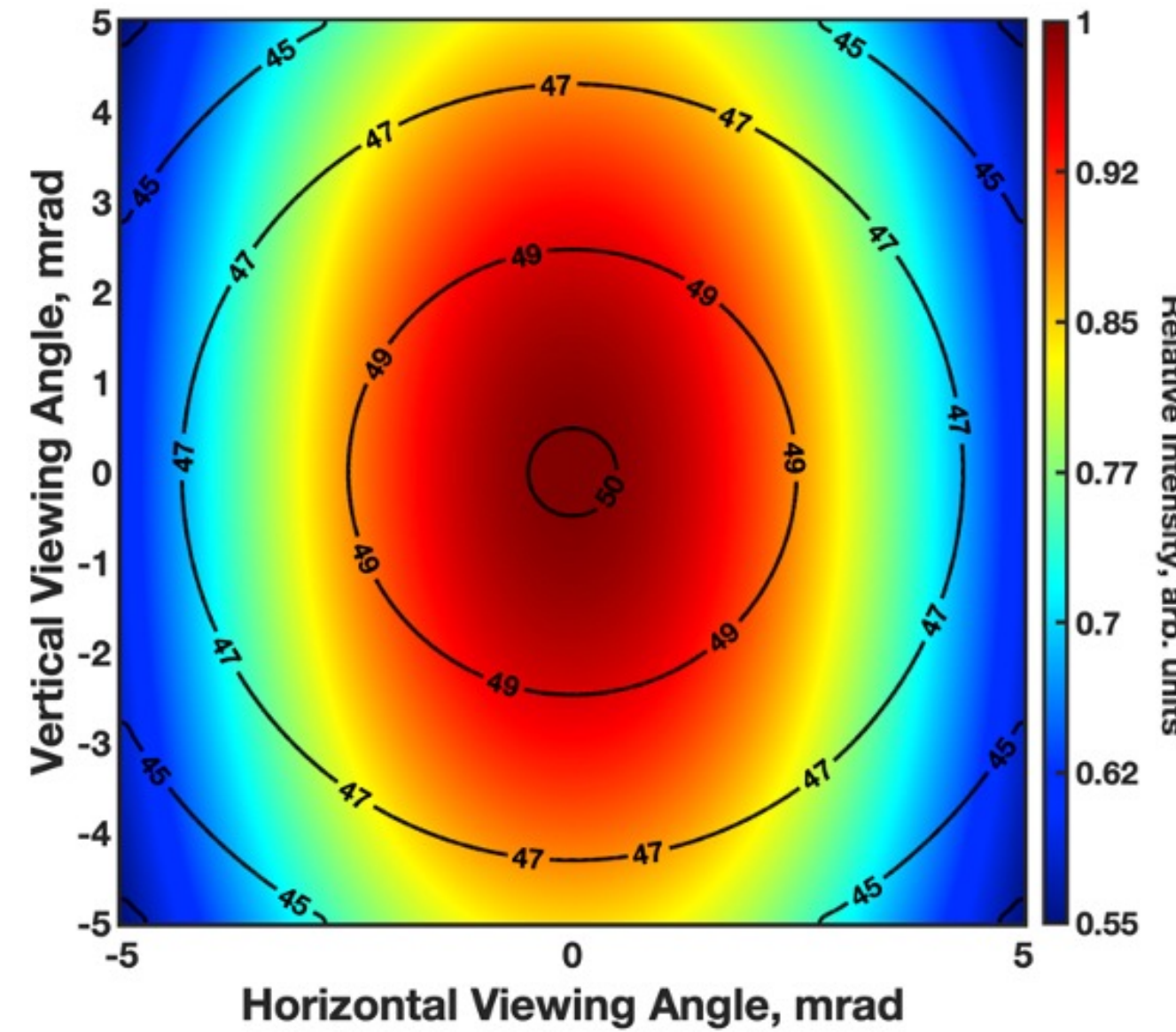
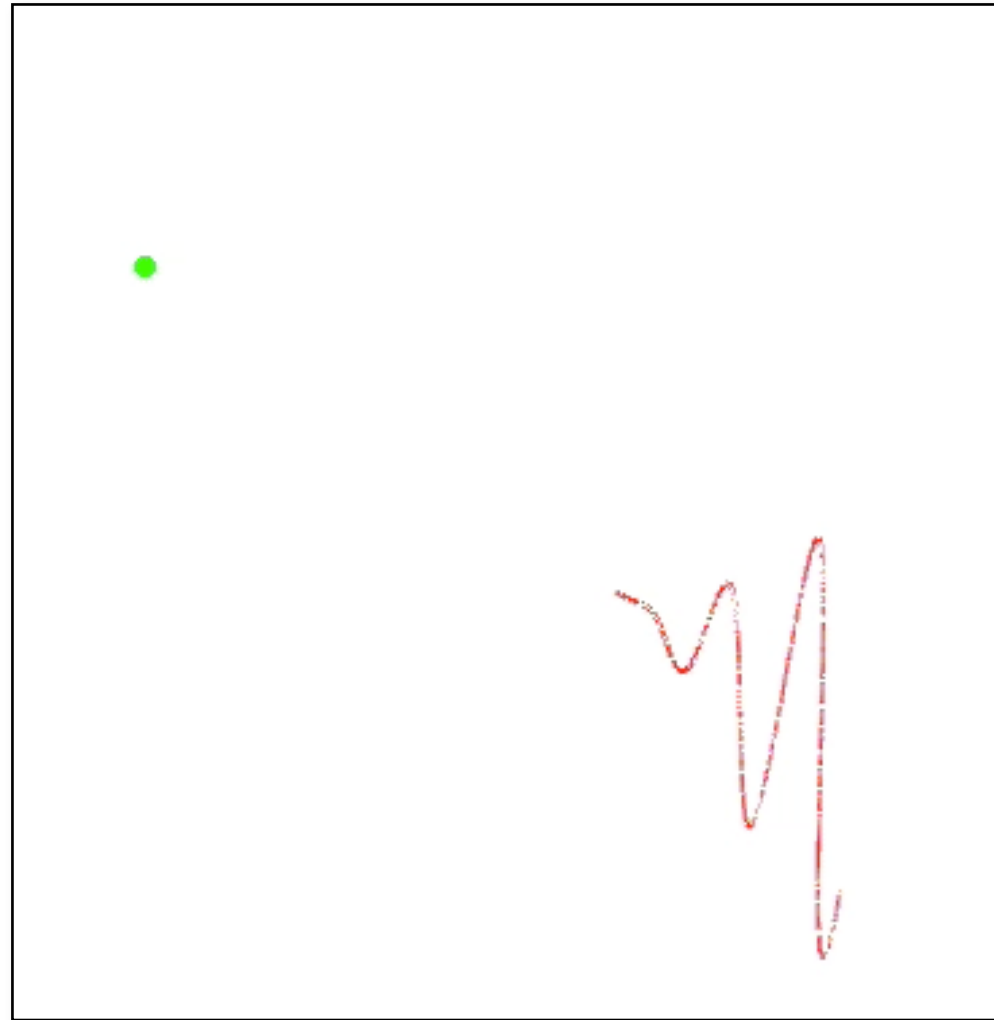


$$E_\gamma = \frac{4\gamma^2}{1 + \gamma^2\theta^2 + 4\gamma k_0^- \lambda_c} E_L$$

↙ Double Doppler upshift
↗ Angle correlated spectrum

$$\frac{dN}{d\Omega d\omega} = \int \frac{d\sigma}{d\Omega} \delta\left(\omega - \omega_l \frac{\kappa_l}{\kappa}\right) (1 + \beta_0) n_l(x_\mu) n_e(x_\mu) d^4 x_\mu$$

Laser-Compton Source



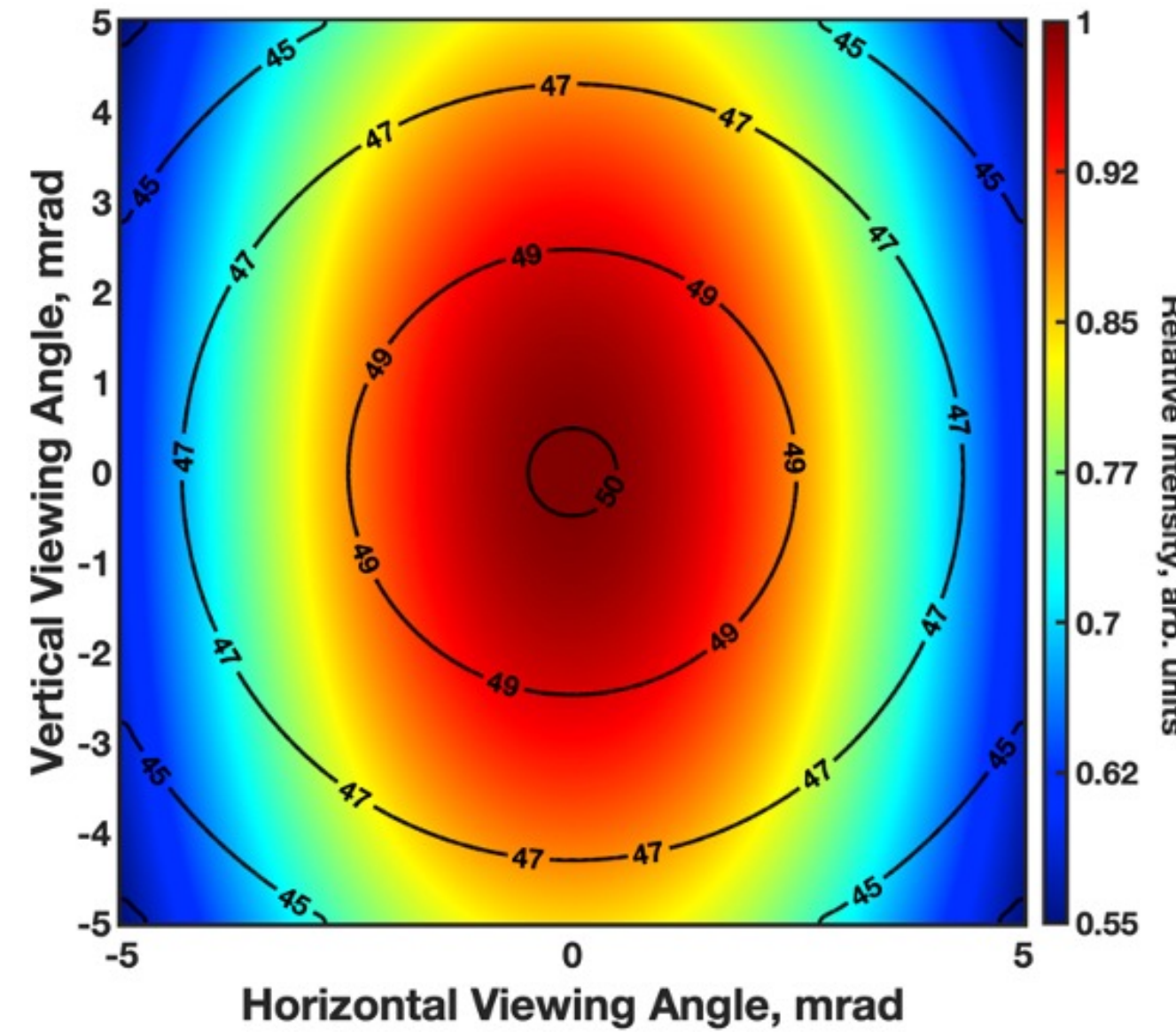
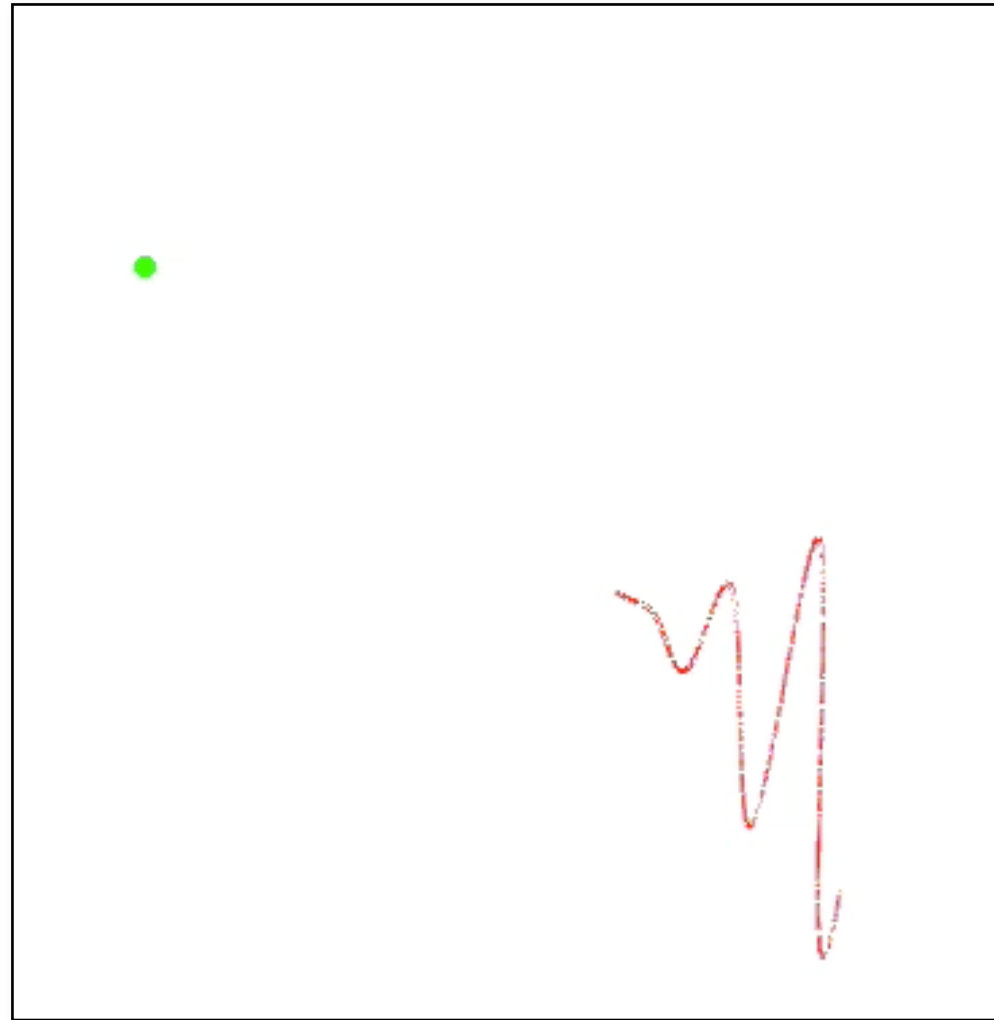
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↖ Angle correlated spectrum

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↗ Laser beam properties

Laser-Compton Source



$$E_\gamma = \frac{4\gamma^2}{1 + \gamma^2\theta^2 + 4\gamma k_0^- \lambda_c} E_L$$

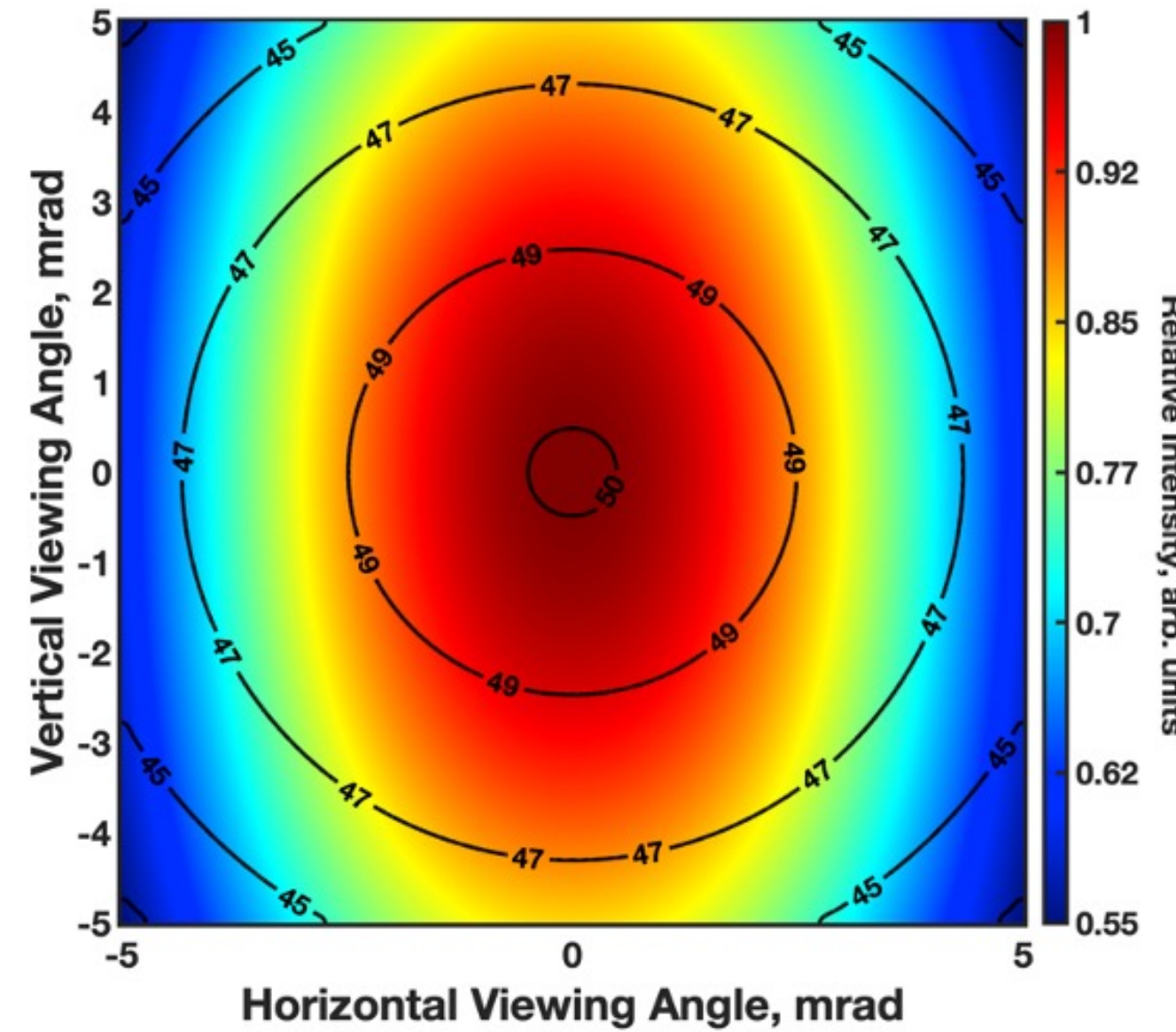
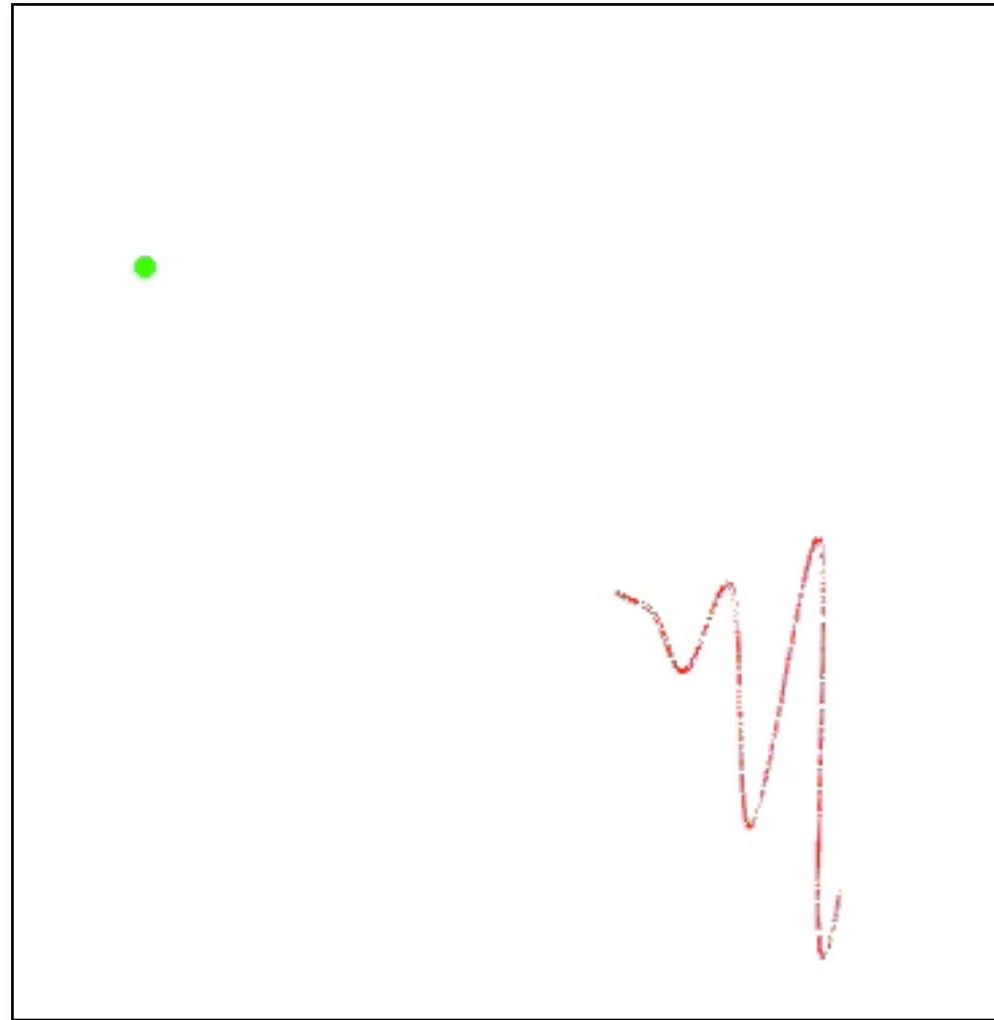
↙ Double Doppler upshift
↘ Angle correlated spectrum

$$\frac{dN}{d\Omega d\omega} = \int \frac{d\sigma}{d\Omega} \delta\left(\omega - \omega_l \frac{\kappa_l}{\kappa}\right) (1 + \beta_0) n_l(x_\mu) n_e(x_\mu) d^4x_\mu$$

↗ Laser beam properties

↖ Electron beam properties

Laser-Compton Source



$$E_\gamma = \frac{4\gamma^2}{1 + \gamma^2\theta^2 + 4\gamma k_0^- \lambda_c} E_L$$

↙ Double Doppler upshift
↗ Angle correlated spectrum

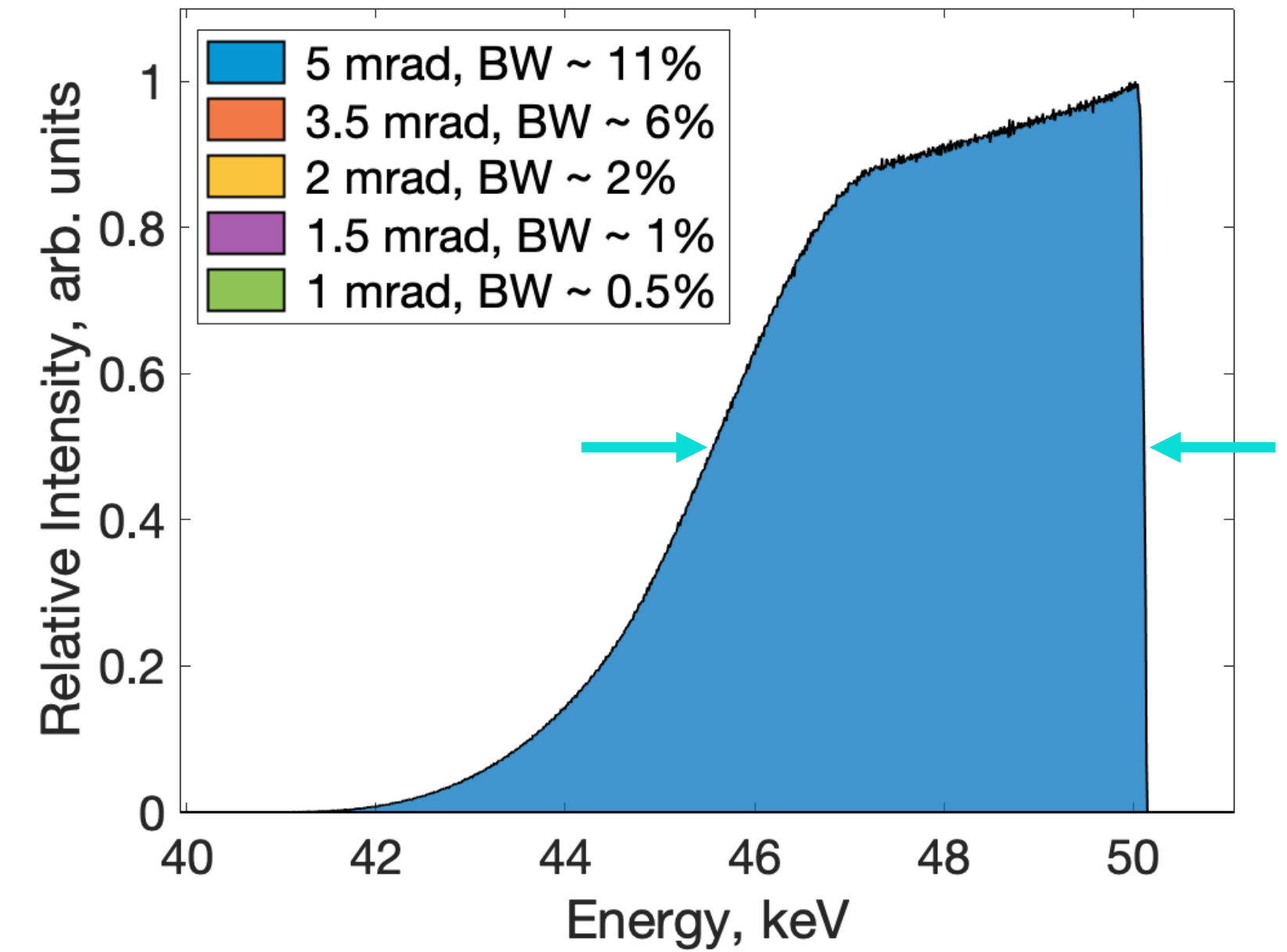
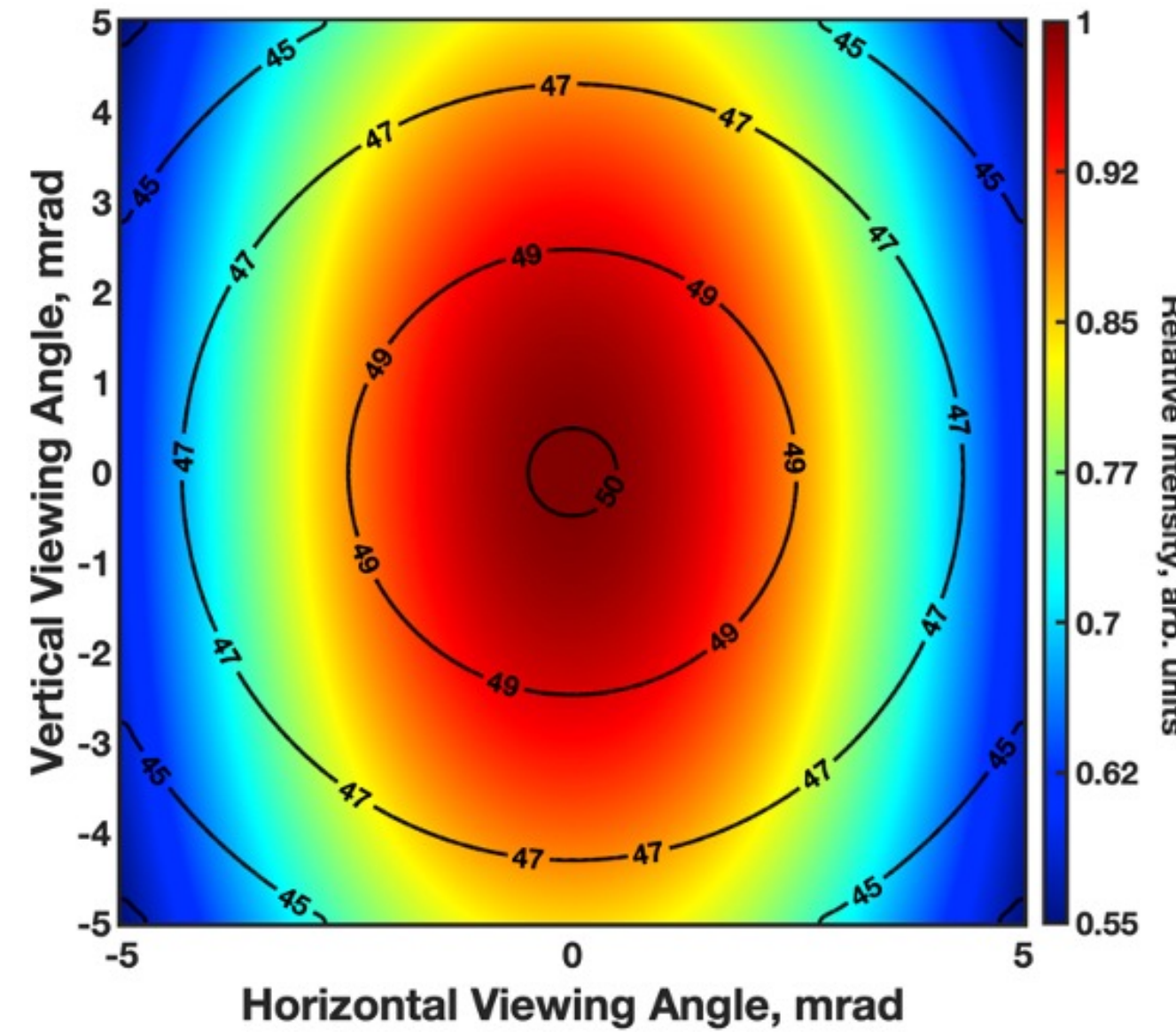
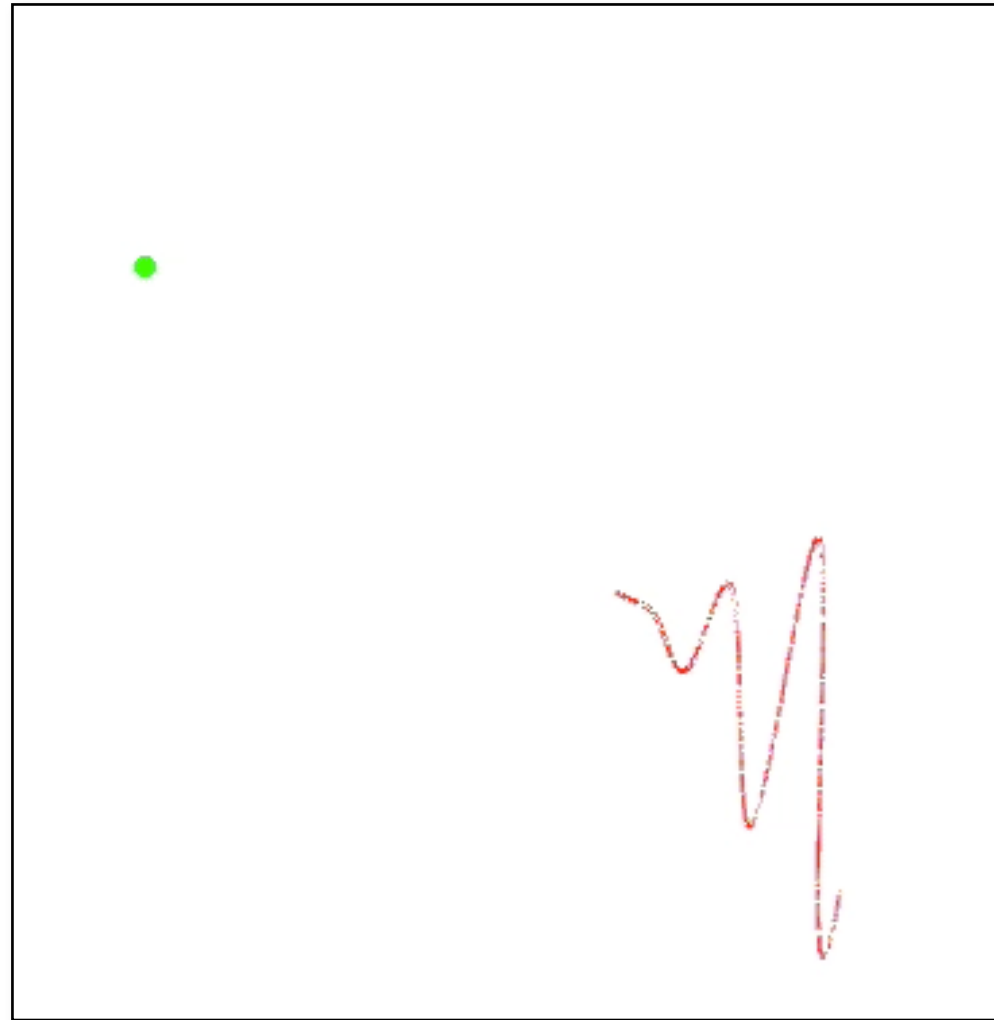
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↑
Klein-Nishina

↗
Laser beam properties

↖
Electron beam properties

Laser-Compton Source



$$E_\gamma = \frac{4\gamma^2}{1 + \gamma^2\theta^2 + 4\gamma k_0^- \lambda_c} E_L$$

↙ Double Doppler upshift
↖ Angle correlated spectrum

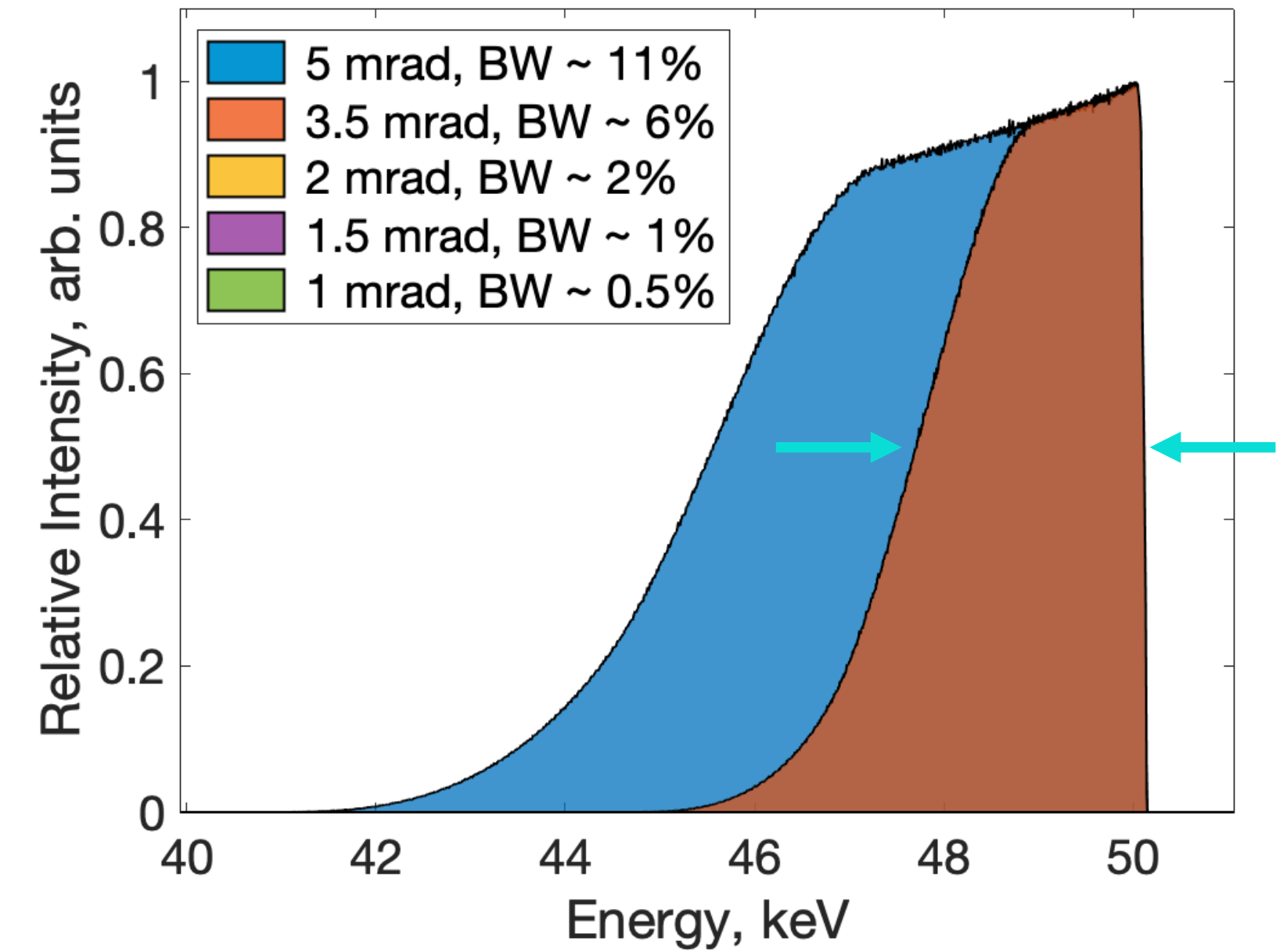
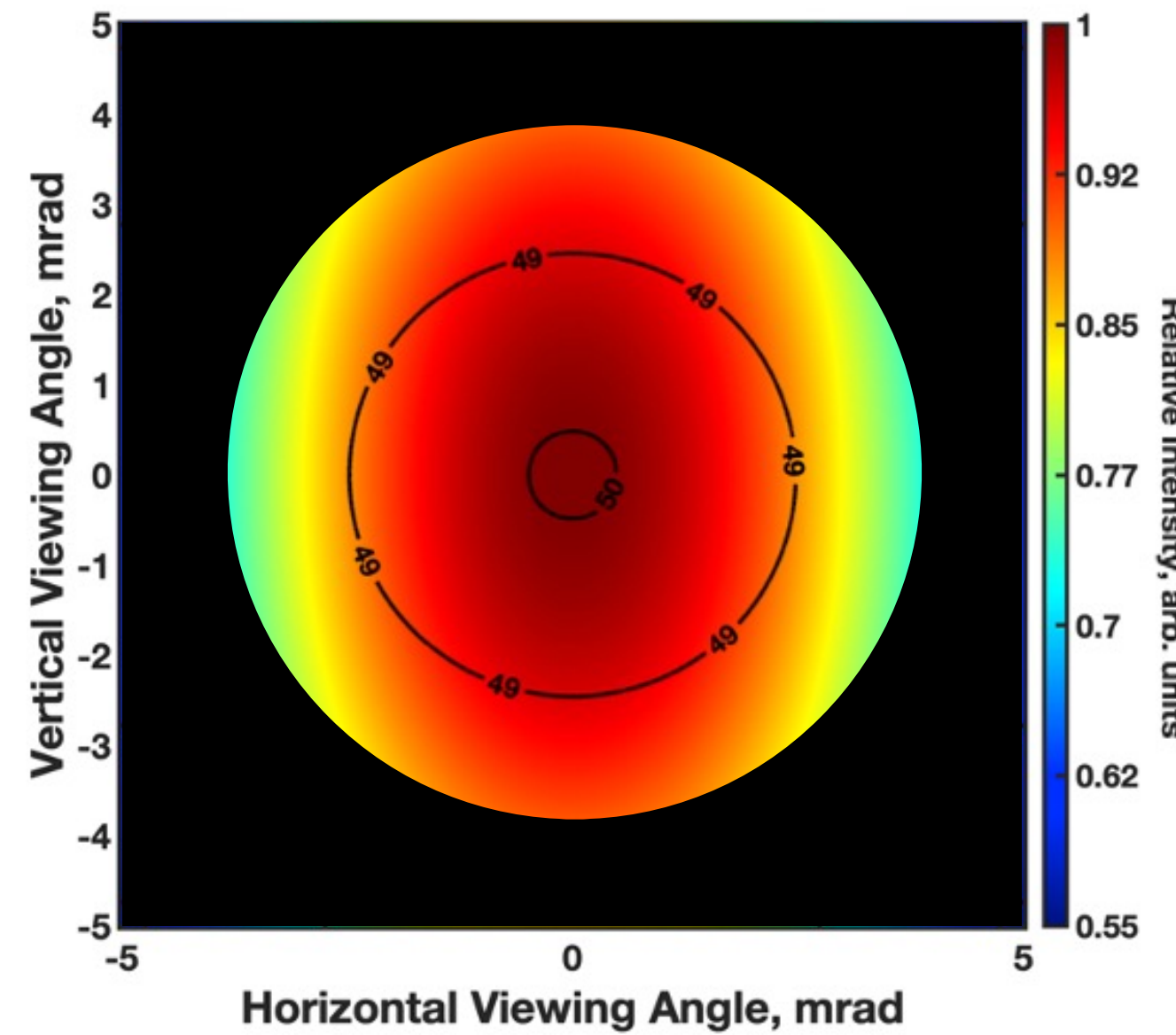
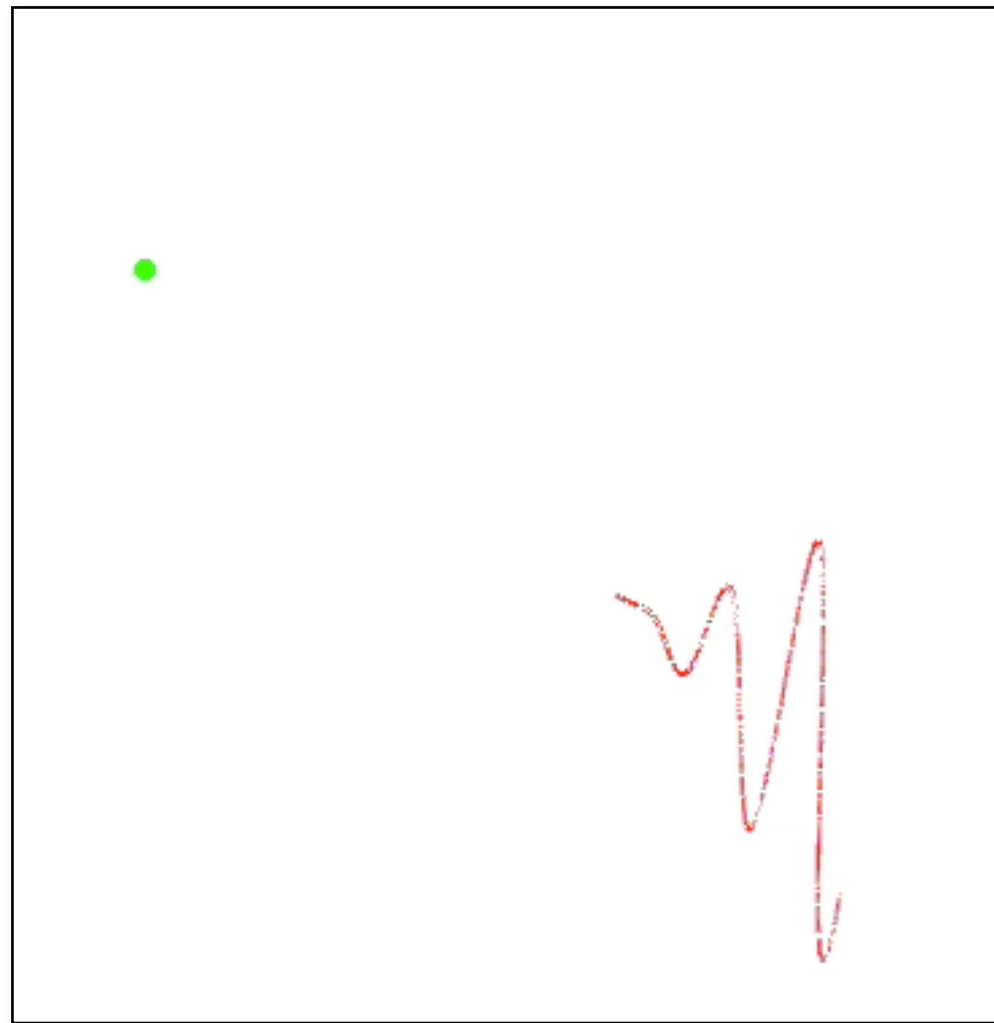
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Klein-Nishina

↗
Laser beam properties

↖
Electron beam properties

Laser-Compton Source



$$E_\gamma = \frac{4\gamma^2}{1 + \gamma^2\theta^2 + 4\gamma k_0^- \lambda_c} E_L$$

↙ **Double Doppler upshift**
↗ **Angle correlated spectrum**

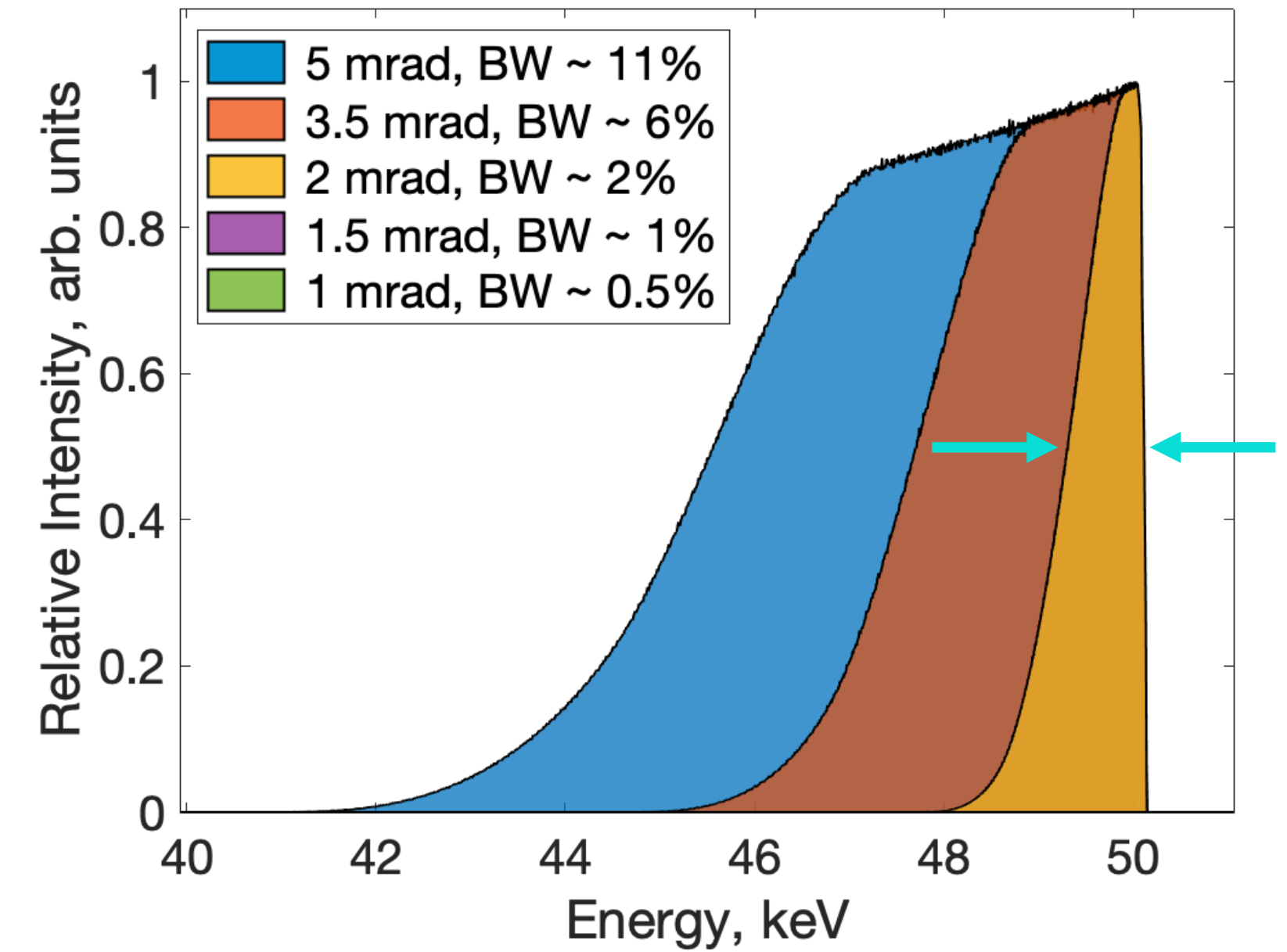
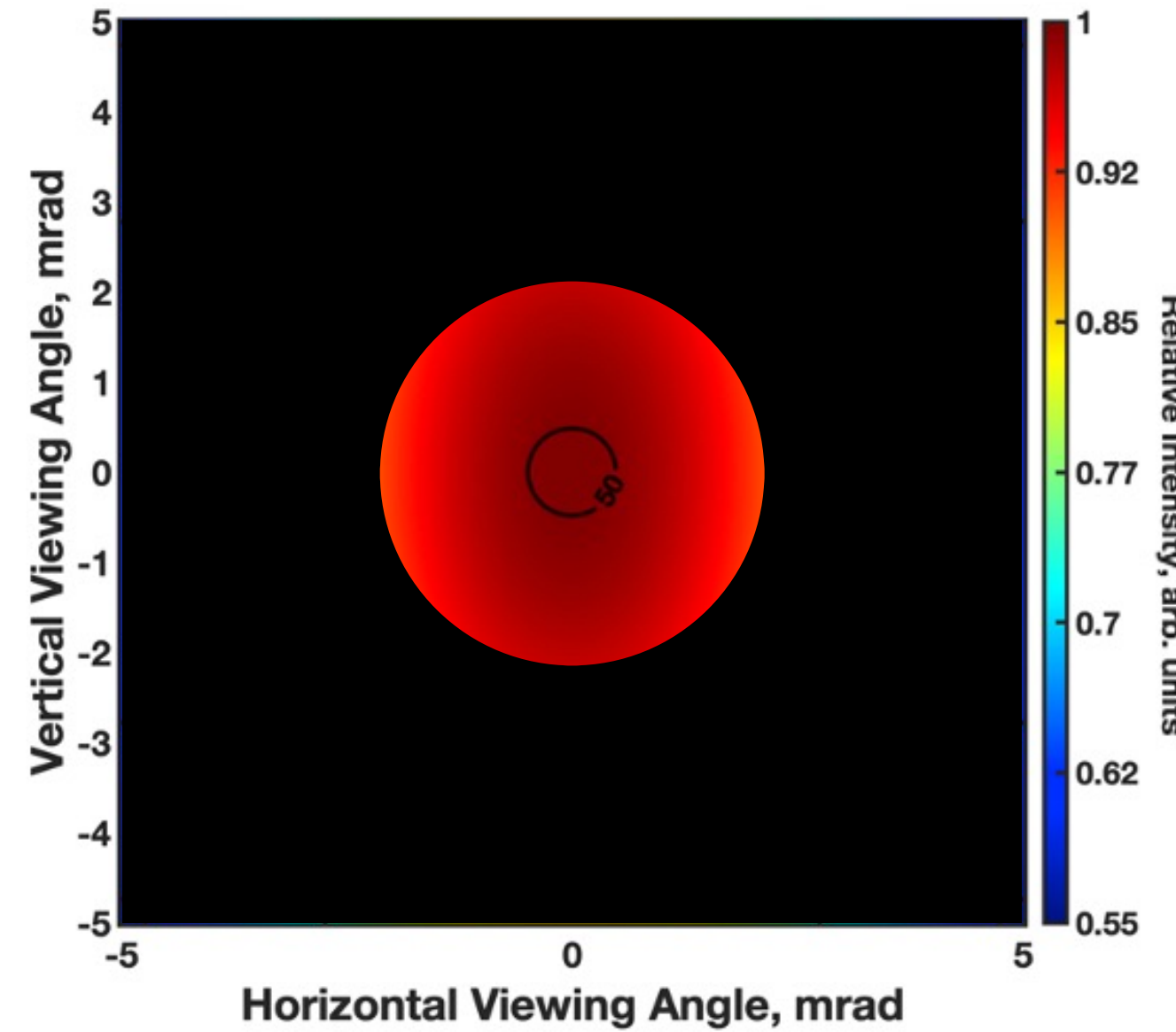
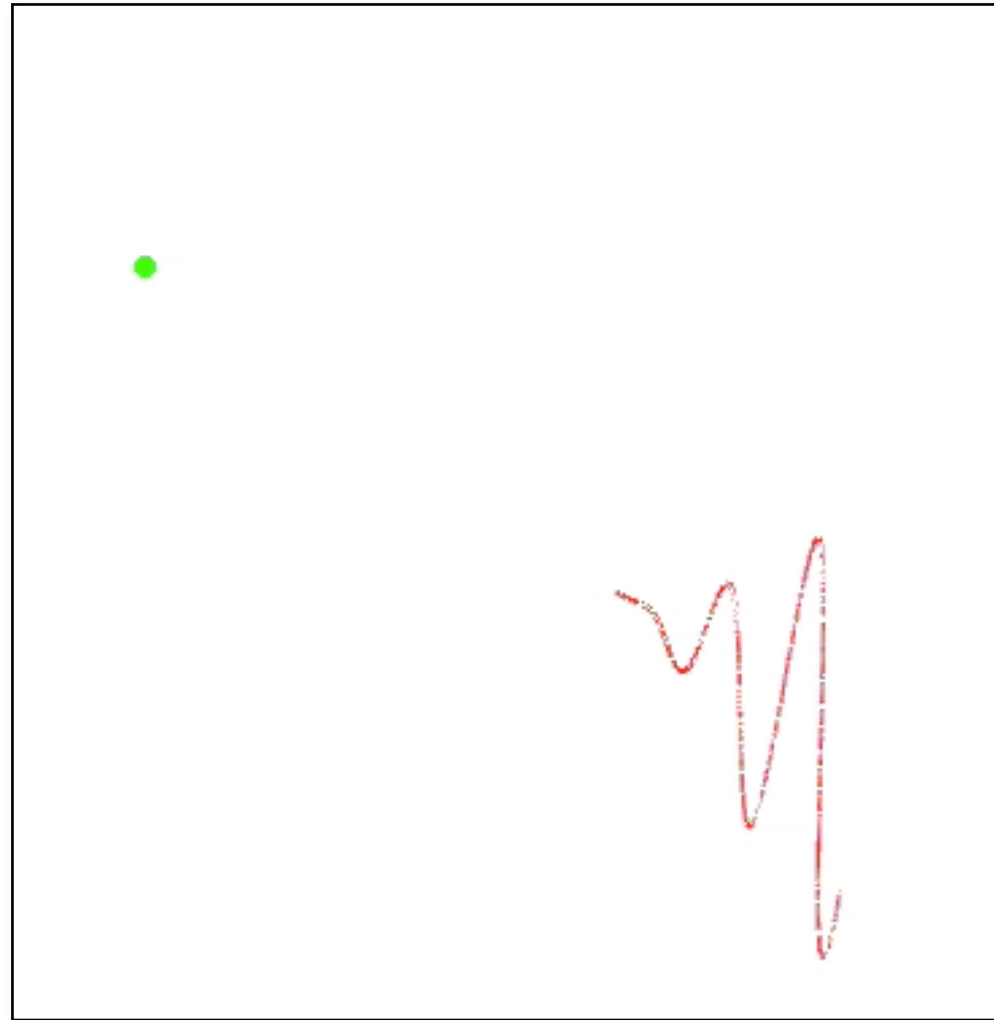
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↑
Klein-Nishina

↗
Laser beam properties

↖
Electron beam properties

Laser-Compton Source



$$E_\gamma = \frac{4\gamma^2}{1 + \gamma^2\theta^2 + 4\gamma k_0^- \lambda_c} E_L$$

↙ Double Doppler upshift
↖ Angle correlated spectrum

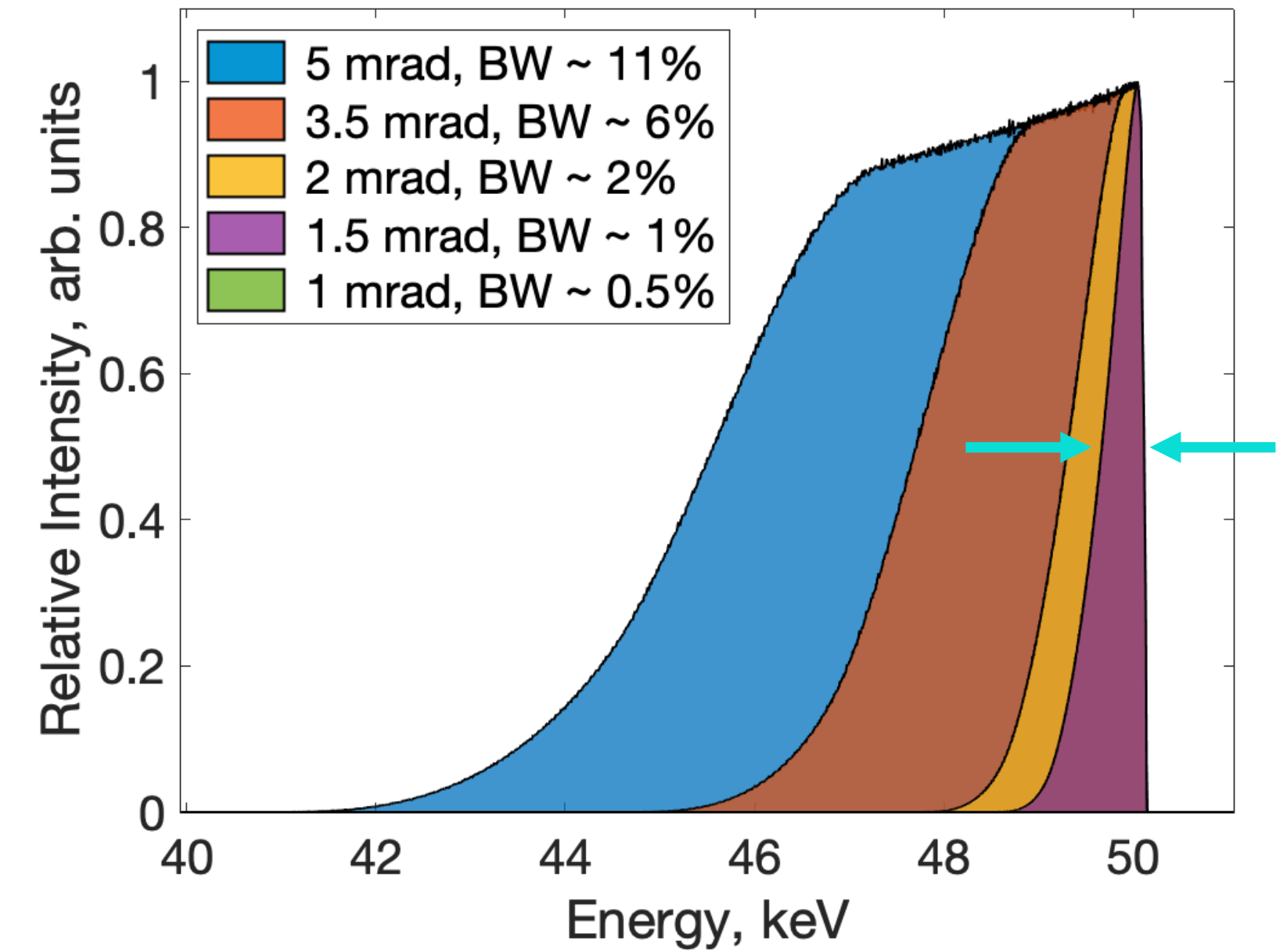
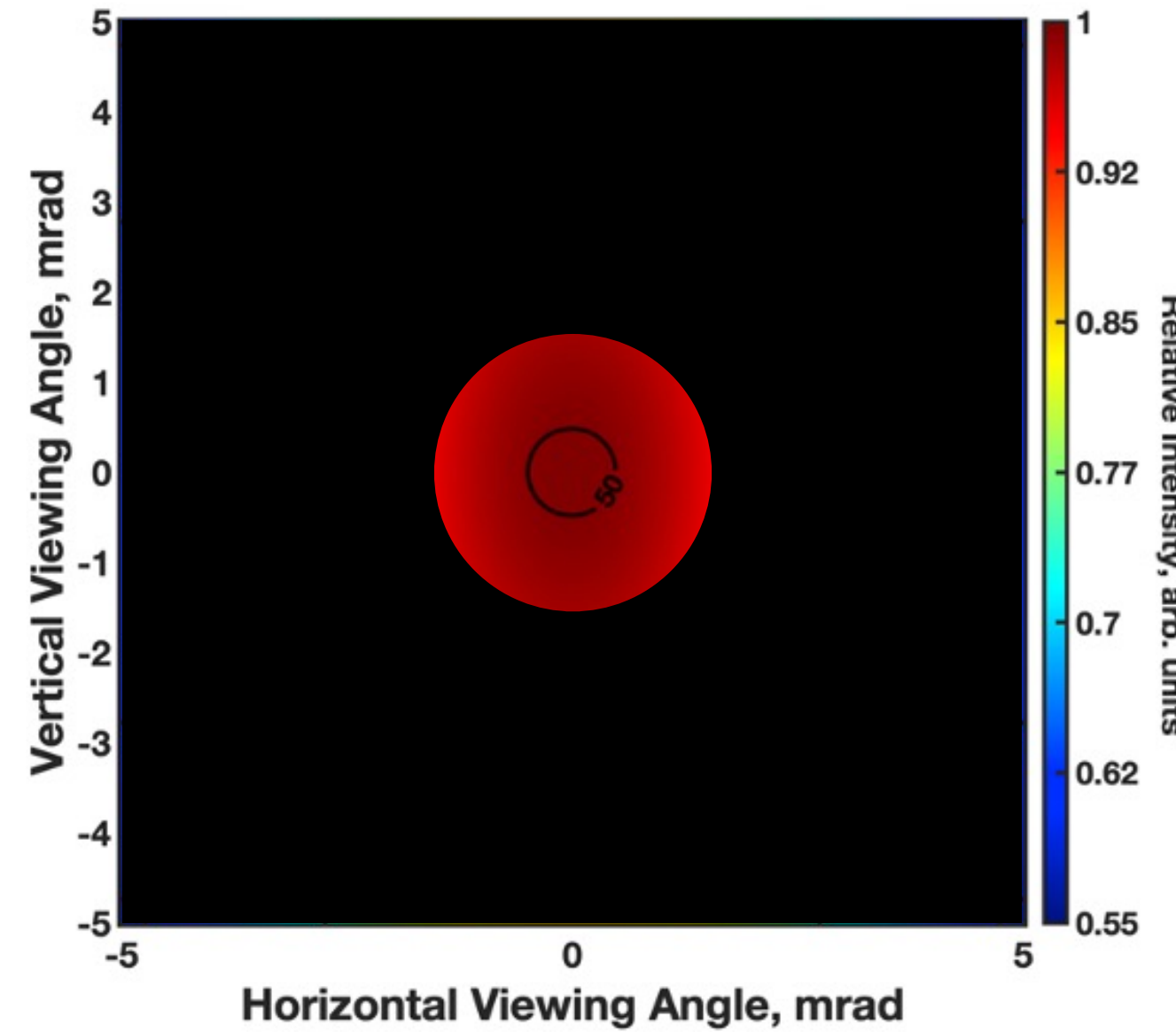
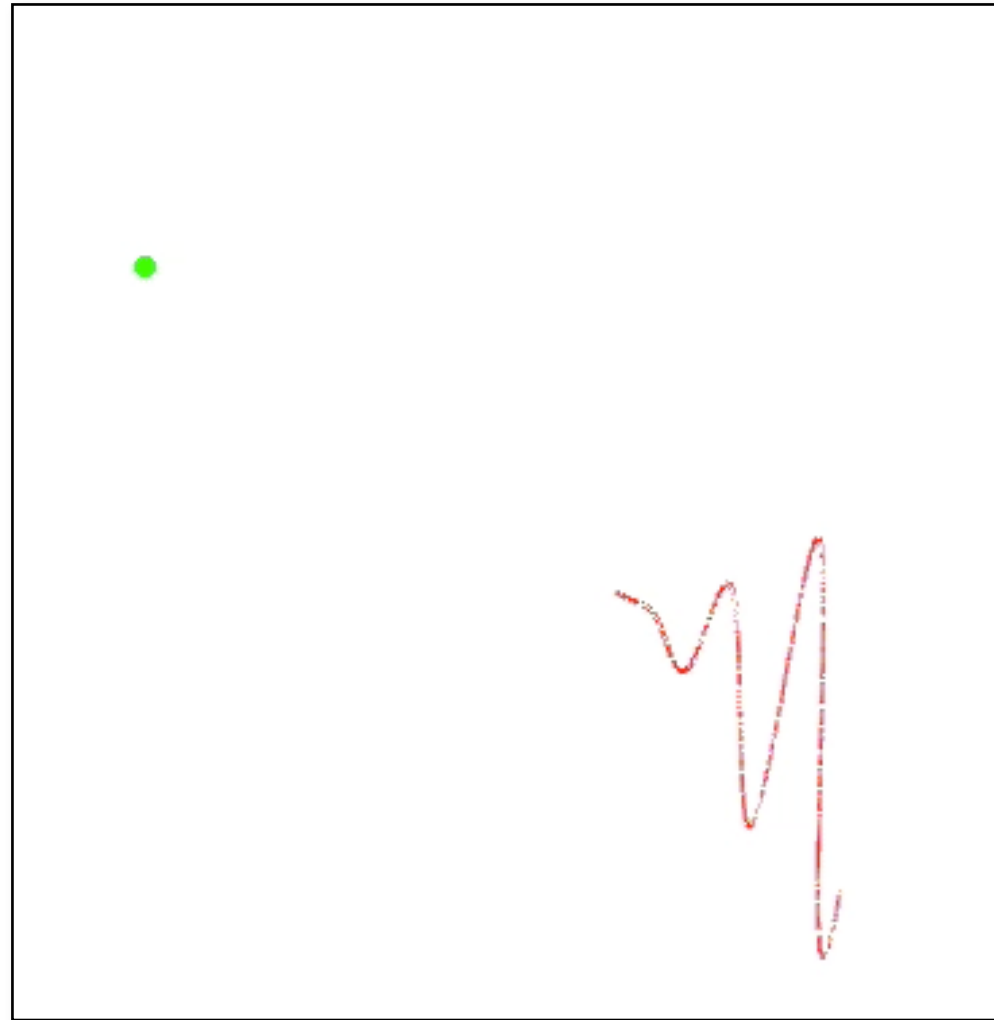
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↑ Klein-Nishina

↗ Laser beam properties

↖ Electron beam properties

Laser-Compton Source



$$E_\gamma = \frac{4\gamma^2}{1 + \gamma^2\theta^2 + 4\gamma k_0^- \lambda_c} E_L$$

↙ **Double Doppler upshift**
↖ **Angle correlated spectrum**

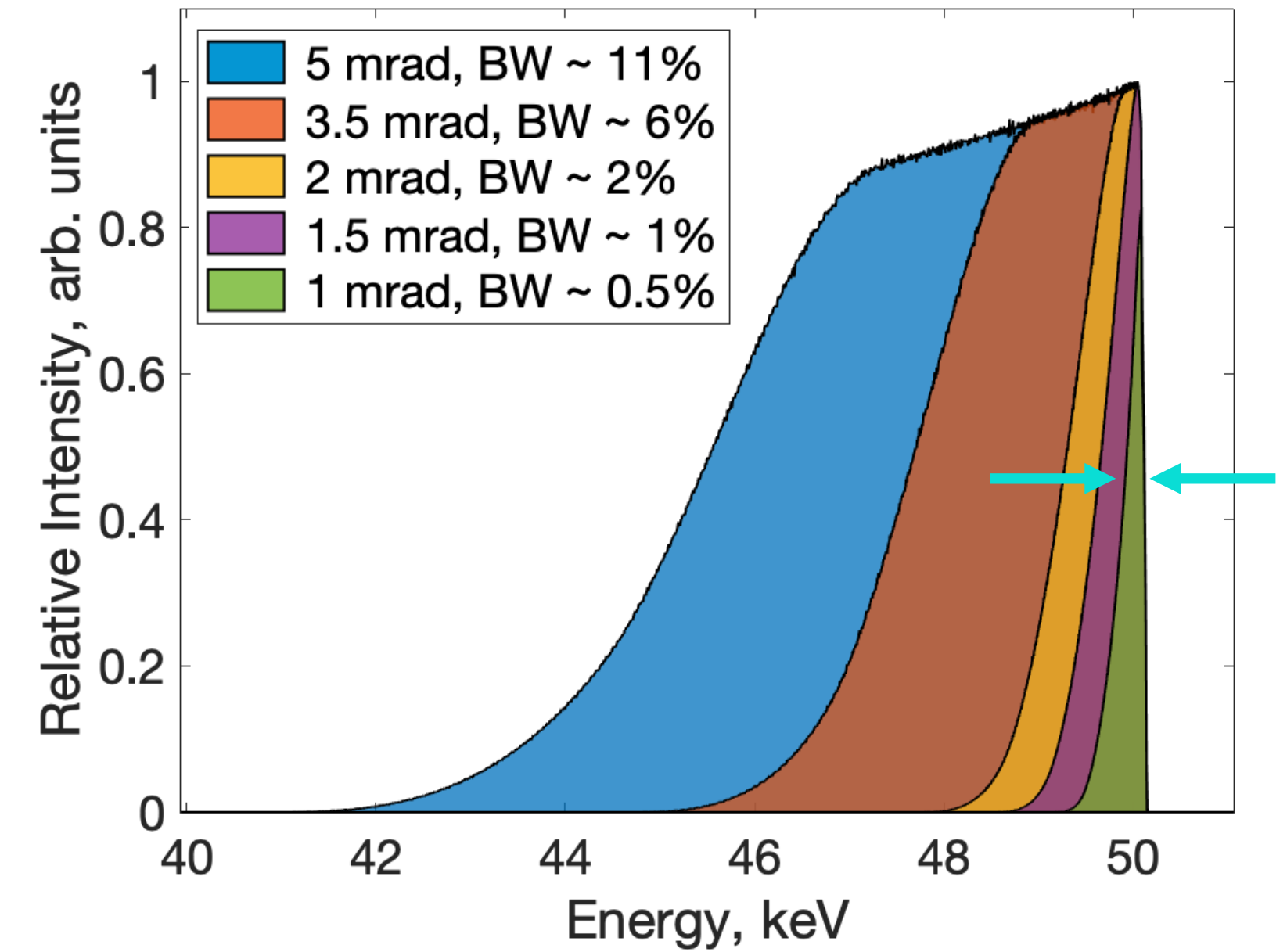
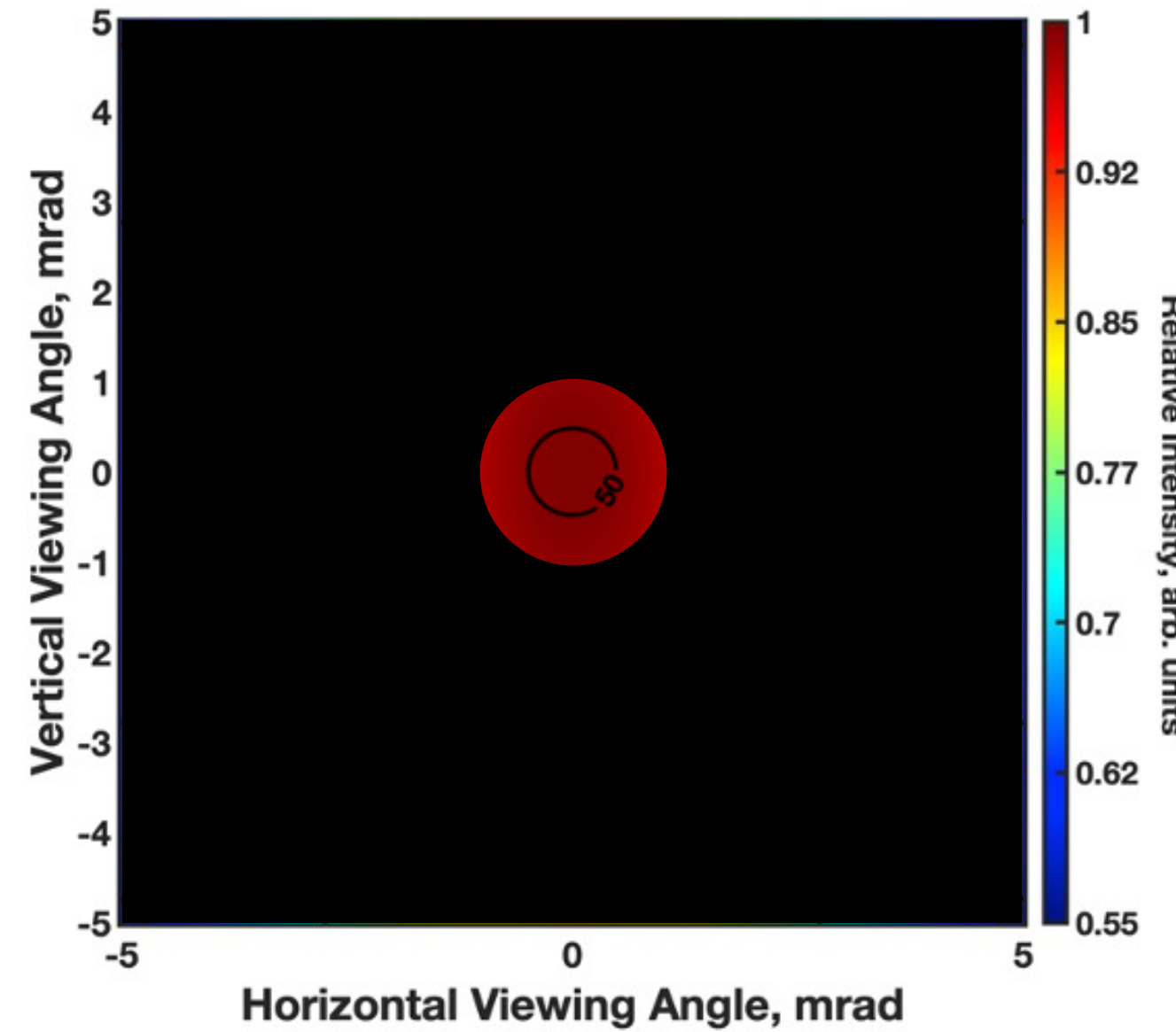
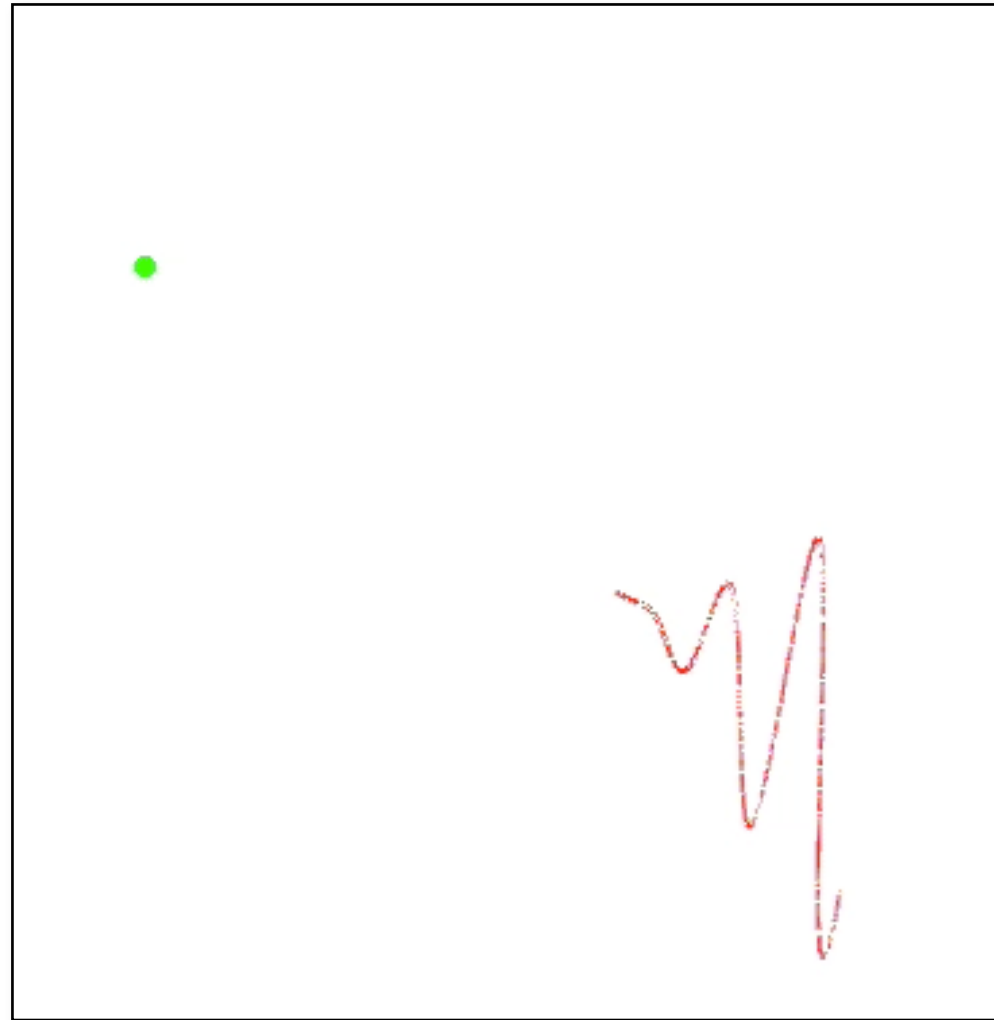
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Klein-Nishina

Laser beam properties

Electron beam properties

Laser-Compton Source



$$E_\gamma = \frac{4\gamma^2}{1 + \gamma^2\theta^2 + 4\gamma k_0^- \lambda_c} E_L$$

↙ **Double Doppler upshift**
↗ **Angle correlated spectrum**

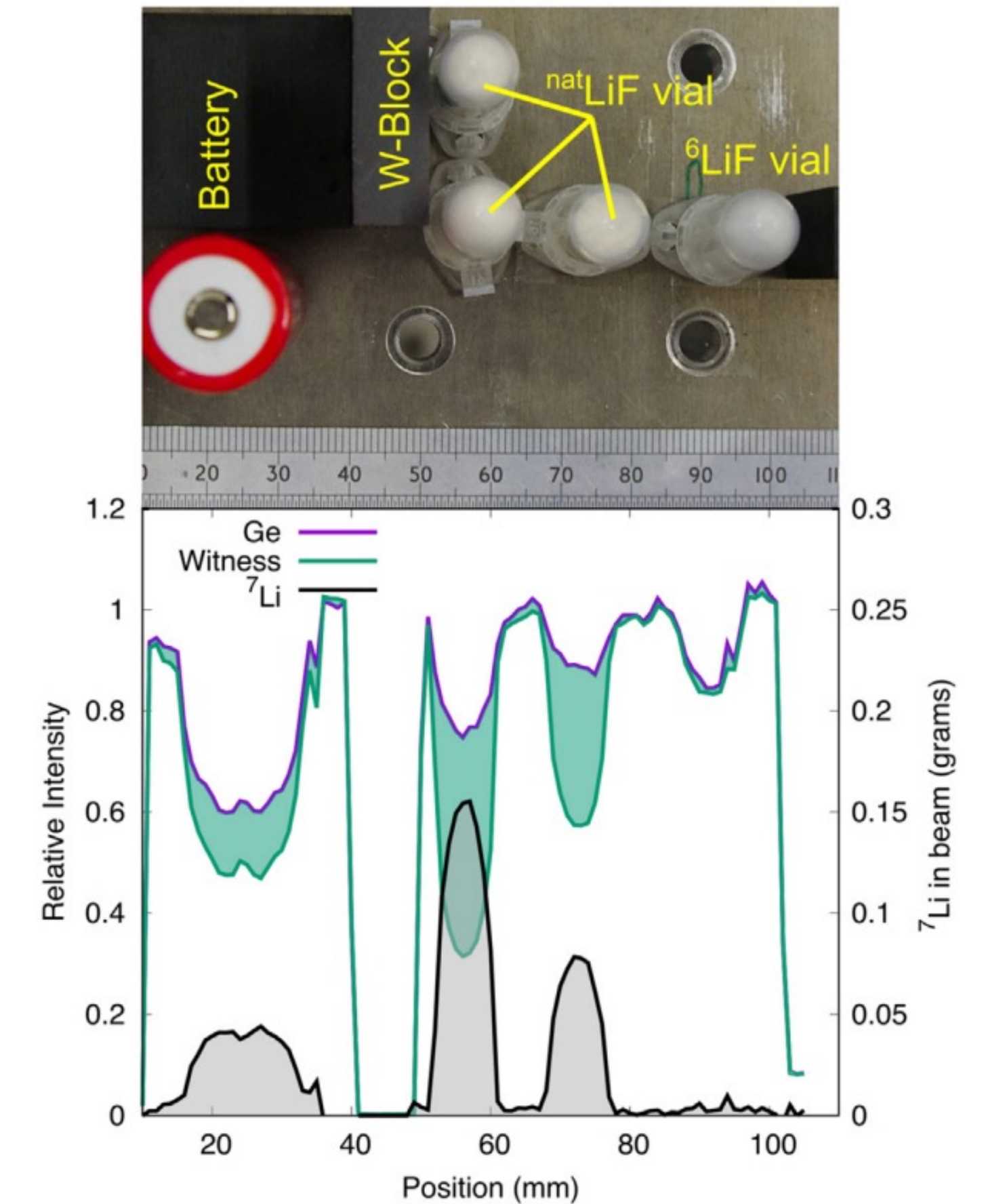
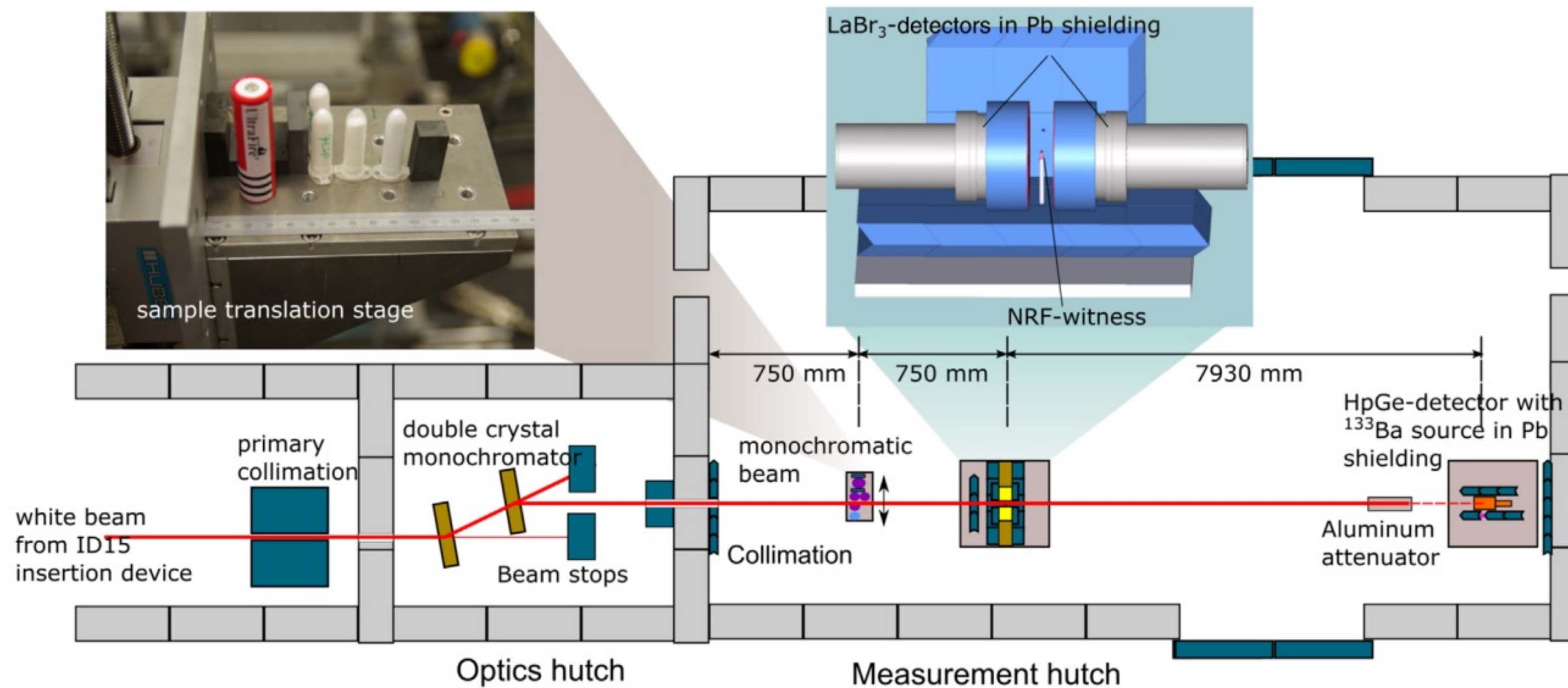
$$\frac{dN}{d\Omega d\omega} = \int \frac{d\sigma}{d\Omega} \delta\left(\omega - \omega_l \frac{\kappa_l}{\kappa}\right) (1 + \beta_0) n_l(x_\mu) n_e(x_\mu) d^4 x_\mu$$

Klein-Nishina

Laser beam properties

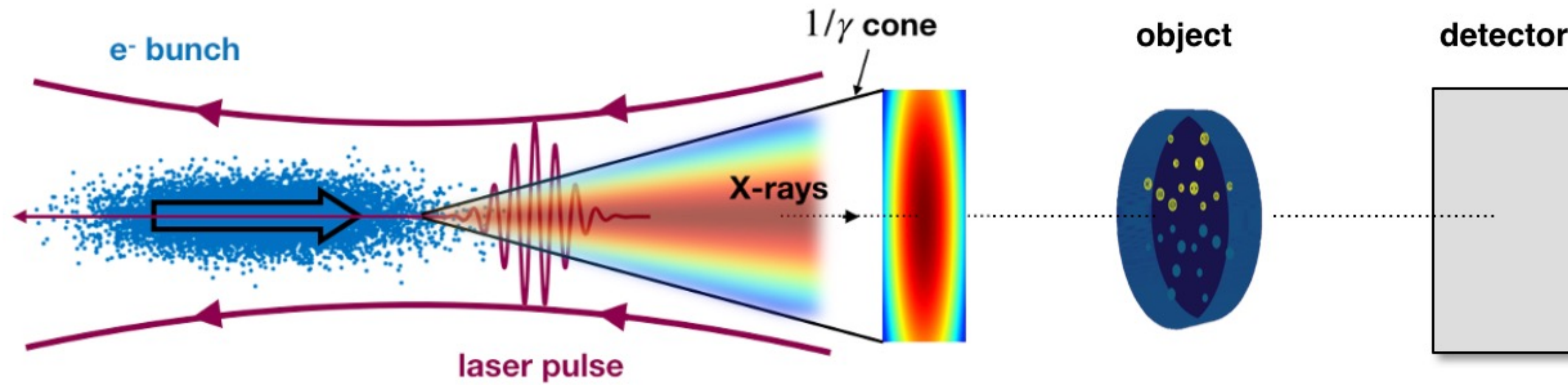
Electron beam properties

1D Imaging has been Demonstrated

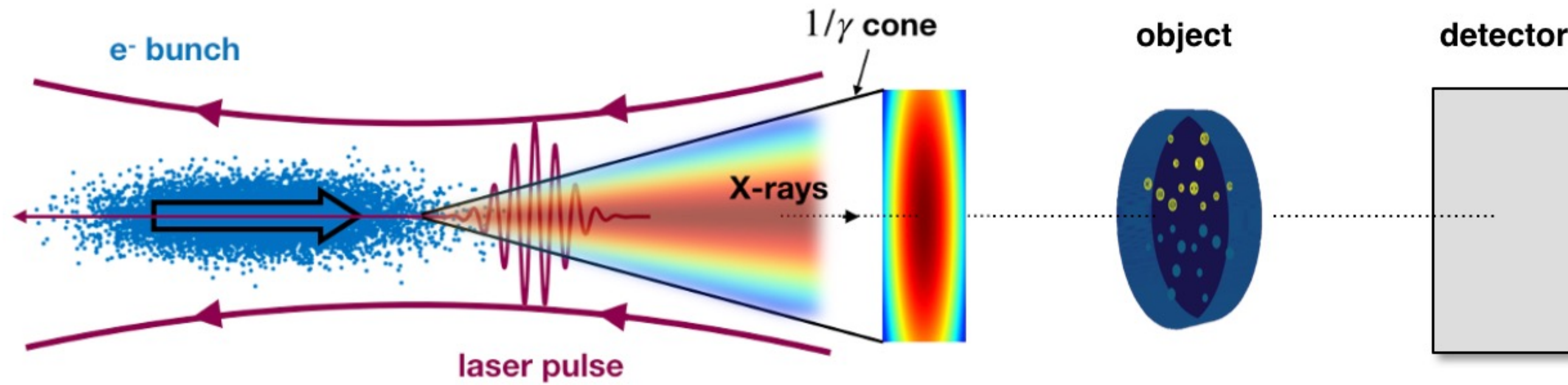


Experiment performed at ESRF with a 10^{-3} bandwidth source.

Computational Demonstration of 2D Li-7 Imaging

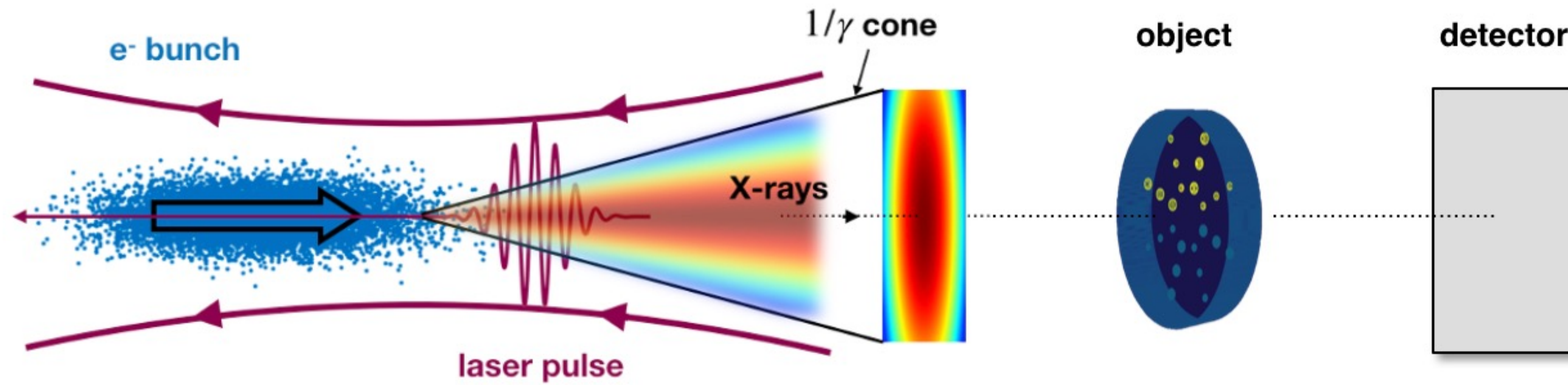


Computational Demonstration of 2D Li-7 Imaging



e^- beam: GPT

Computational Demonstration of 2D Li-7 Imaging

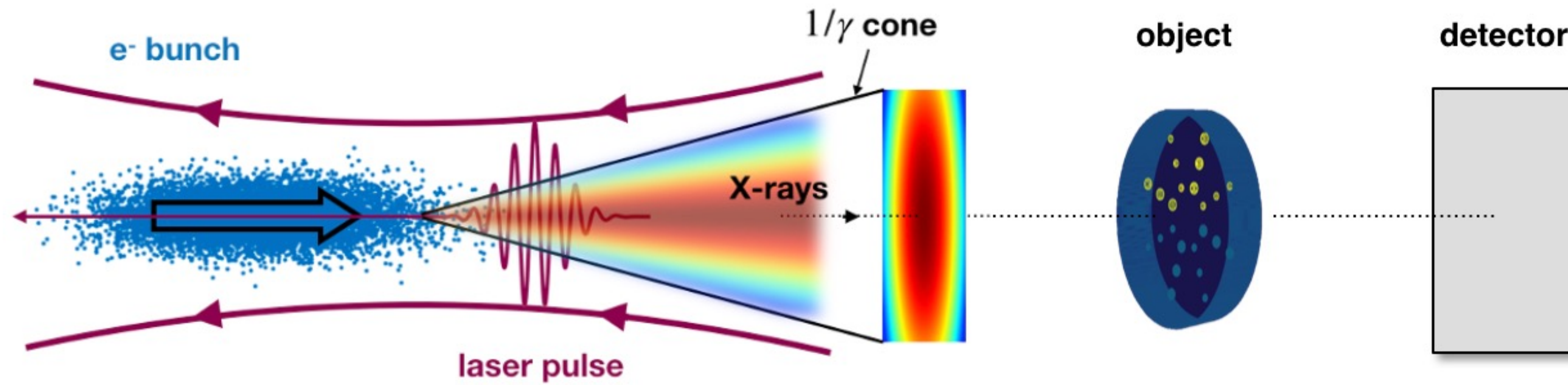


e^- beam: GPT

e^- bunch / laser
pulse interaction:
Mathematica

This method retains the spatial-energy x-ray spectrum required for accurate simulation.

Computational Demonstration of 2D Li-7 Imaging



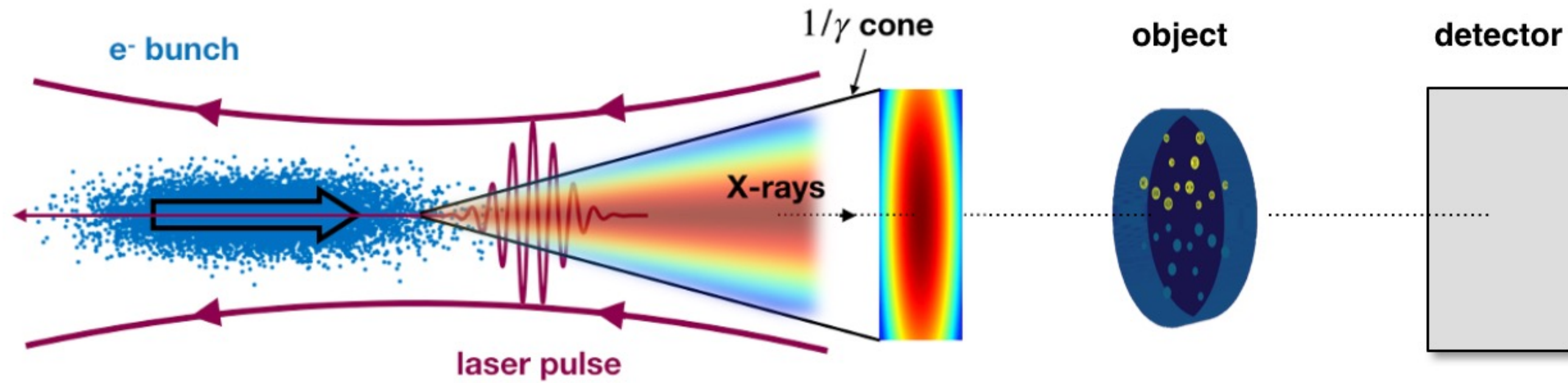
e⁻ beam: GPT

**e⁻ bunch / laser
pulse interaction:
Mathematica**

**x-ray propagation
through object and
image generation:
Matlab/Geant4 w/ G4NRF**

This method retains the spatial-energy x-ray spectrum required for accurate simulation.

Computational Demonstration of 2D Li-7 Imaging

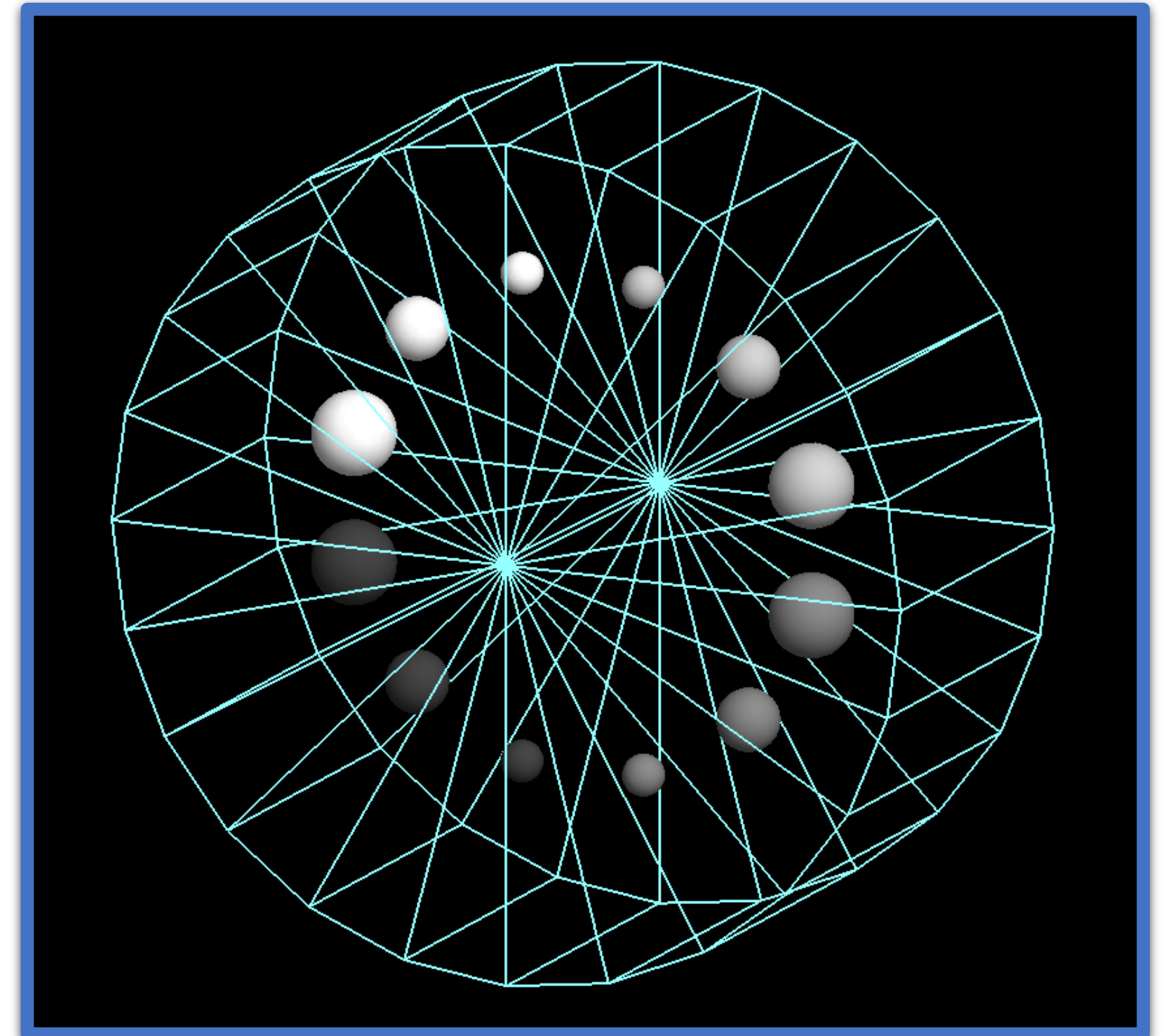


e^- beam: GPT

e^- bunch / laser pulse interaction: Mathematica

x-ray propagation through object and image generation: Matlab/Geant4 w/ G4NRF

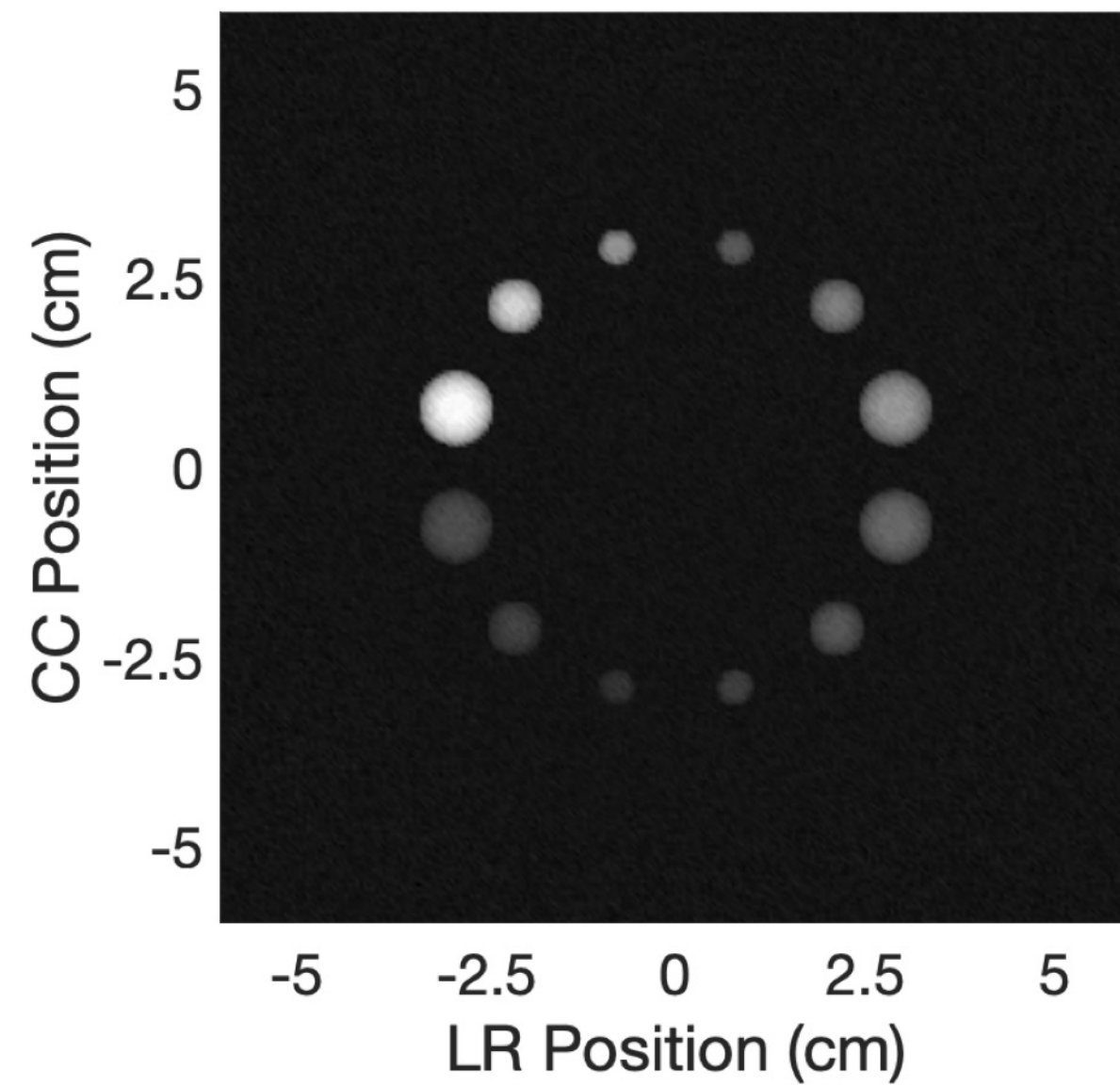
Computational Phantom



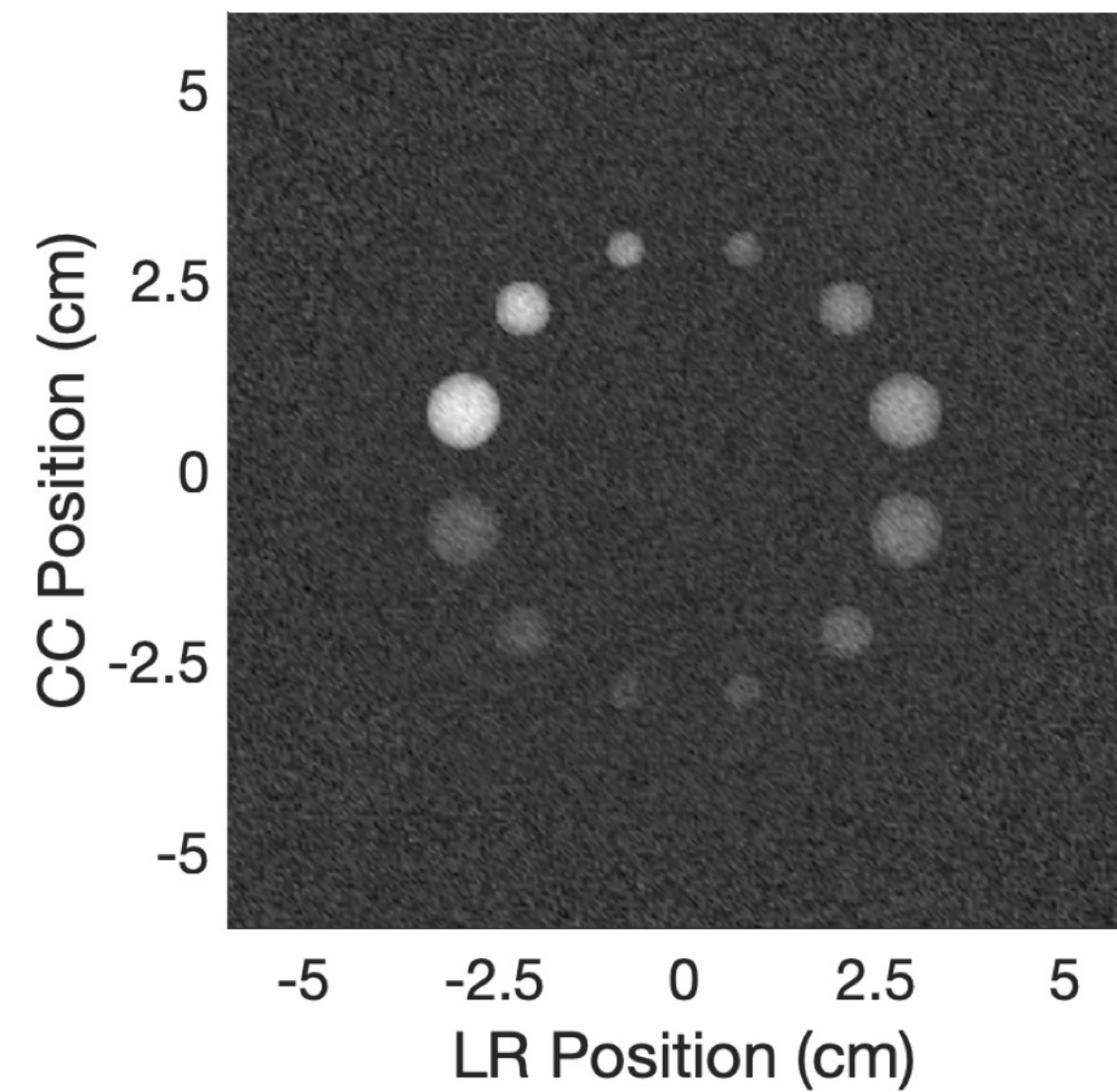
4.2 cm water cylinder with Li inserts of varying concentrations.

Bandwidth is Important

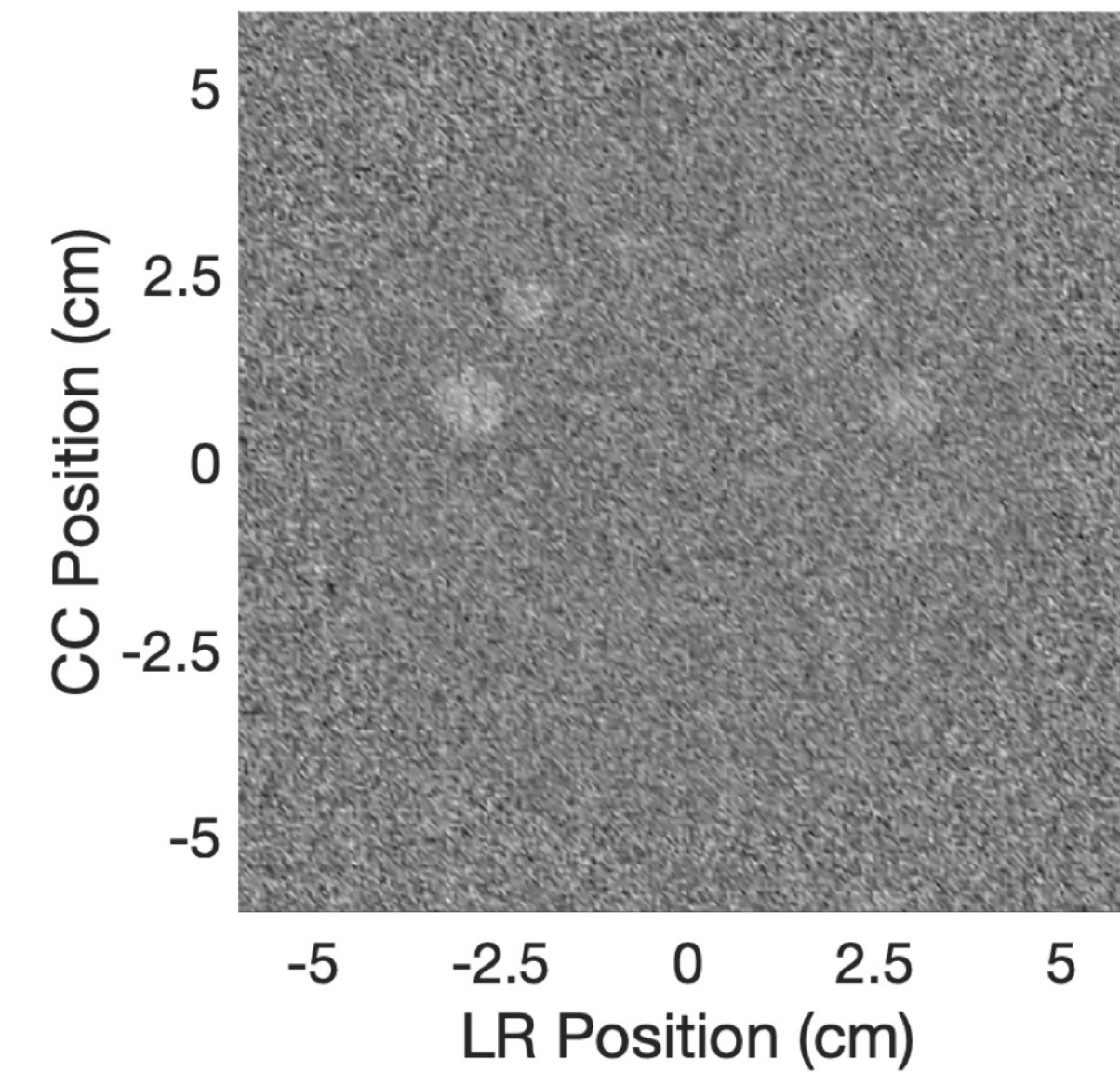
$$\frac{\Delta E}{E} = 2.3 \times 10^{-5}$$



$$\frac{\Delta E}{E} = 1.0 \times 10^{-4}$$

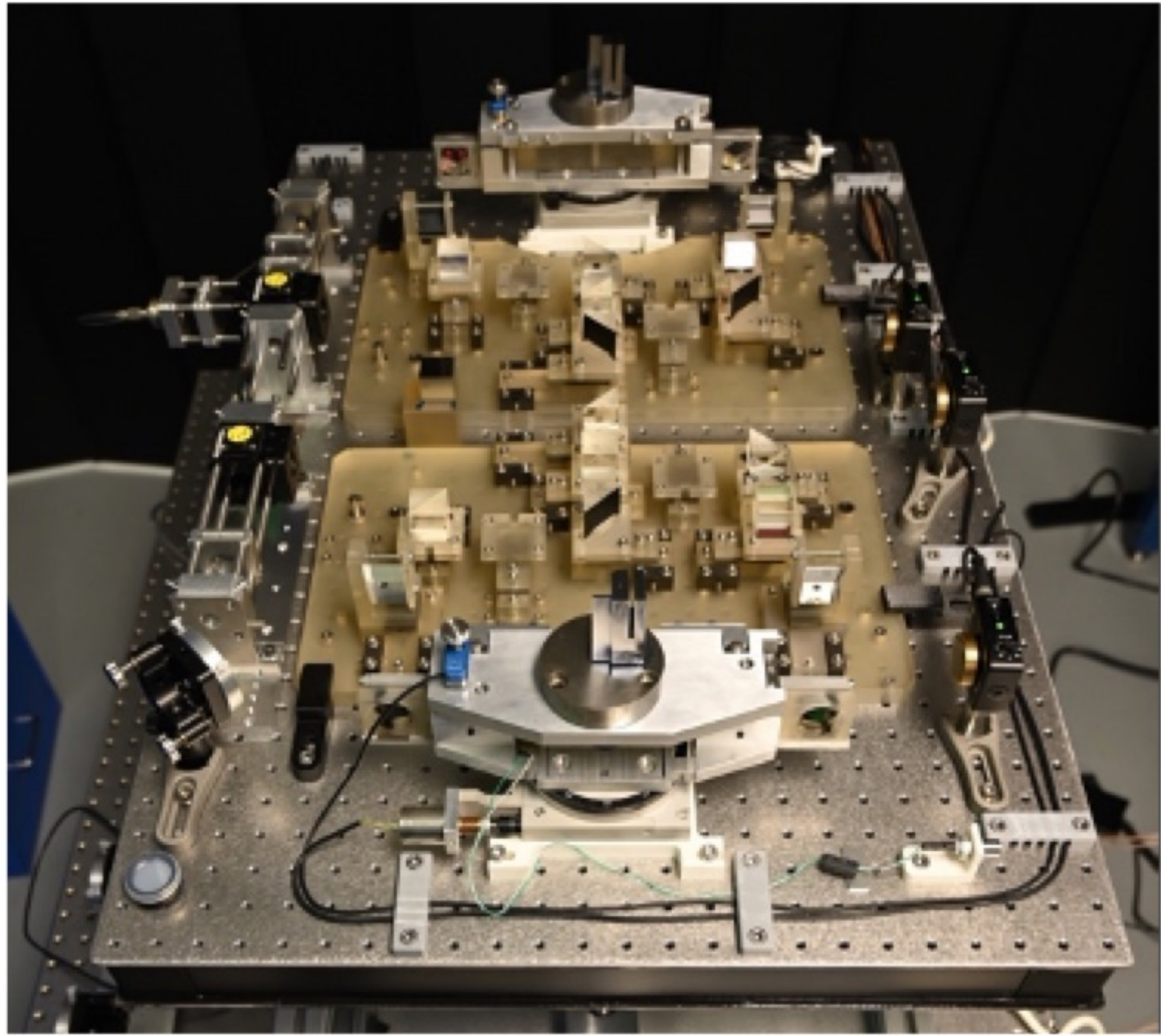


$$\frac{\Delta E}{E} = 1.1 \times 10^{-3}$$



Images generated using a dual-energy approach.
Contrast increases with smaller bandwidths.

GAMS Monochromator



Speaker: **Michael Jentschel**

Institute Laue Langevin, Lumitron Technologies Inc.

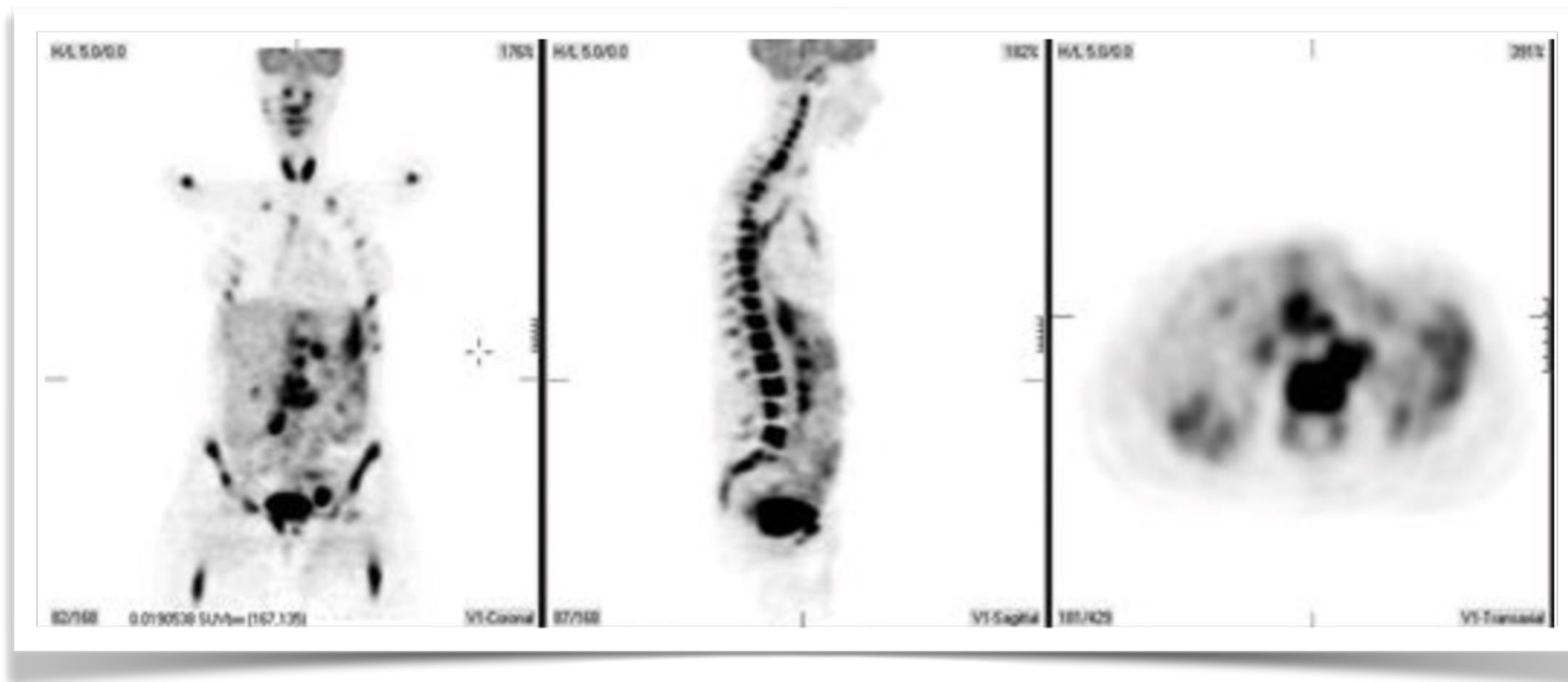
**Combination of a Diffraction Based
Ultra-Narrow Band Width Filter with a
Laser Compton Photon Source**

Wednesday, 13 September
Junior Ballroom, 9:55 AM

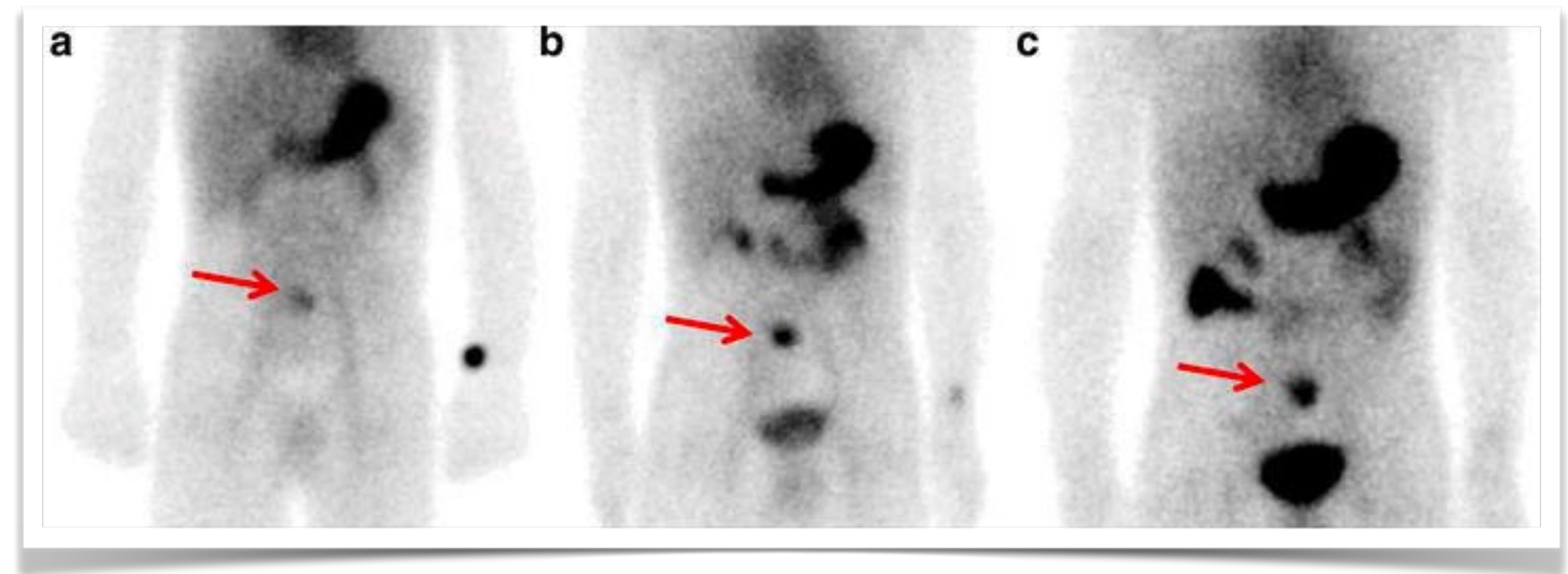
Double crystal monochromator will allow further bandwidth filtering to improve contrast

Could LCS-NRF be used for Medical Imaging?

PET



SPECT



We can learn from the PET and SPECT communities.

Could We Image a Clinically Used Radiotracer?

Isotope	Abundance (%)	Energy (keV)	Integrated σ (eV b)
<i>F-19</i>	100	109.894	0.25
		1458.7	26.57
		1554.038	414.68
		3908.17	38.25
		4556.1	14.07
<i>Cu-63</i>	69.2	669.93	9.86
		962.02	4.98
		1412.16	0.78
		1547	6.31
		2012.92	13.11
<i>Cu-65</i>	30.9	770.64	14.33
		1115.556	7.49
		1623.43	0.62
		1725	6.40
		2107.44	3.48
		2212.84	1.63
		2329.05	12.43
<i>Ga-69</i>	60.1	574.22	4.69
		872.147	9.22
		1028.59	0.69
		1107.04	9.66
		1723.71	5.90
		1891.64	22.26

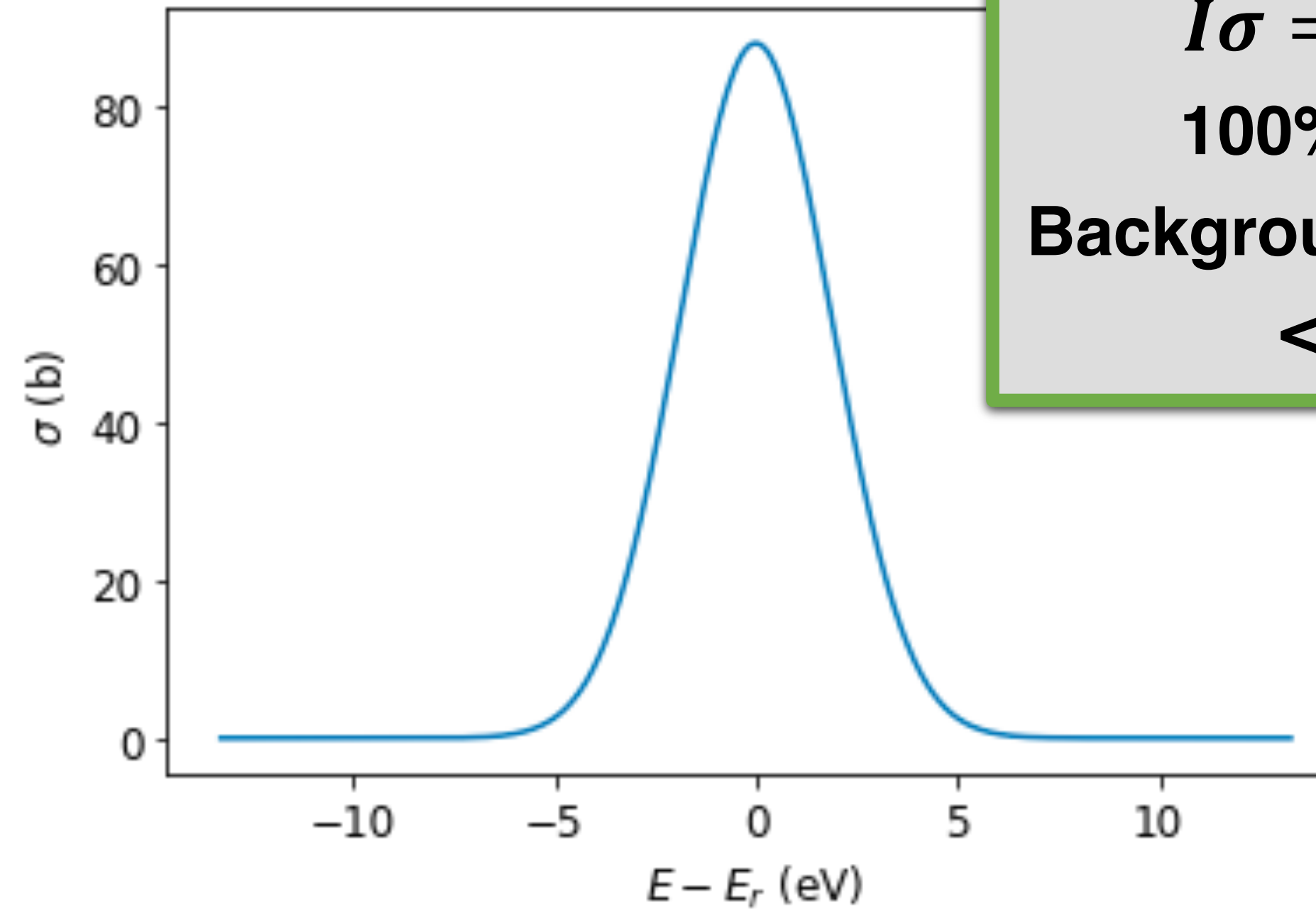
Isotope	Abundance (%)	Energy (keV)	Integrated σ (eV b)
<i>Ga-71</i>	39.9	389.94	14.41
		511.495	4.47
		910.16	8.82
		964.66	2.17
		1109.31	7.50
		1631.4	4.39
		1719.5	8.89
		2064.06	2.51
<i>Rb-85</i>	72.2	151.192	0.07
		731.829	0.50
		868.94	1.24
		919.73	3.00
		950.95	0.69
		1175.56	1.92
		1384.24	0.91
<i>Rb-87</i>	27.8	402.588	0.20
		845.44	12.14
		1389.78	4.78
		1463	1.95

Only dipole transitions considered

Candidate: ^{19}F

Mass fraction of elements in human body

Element	Mass Fraction	Element	Mass Fraction
Oxygen	0.65	Sulfur	2.5×10^{-3}
Carbon	0.18	Sodium	1.5×10^{-3}
Hydrogen	0.1	Chlorine	1.5×10^{-3}
Nitrogen	0.03	Magnesium	5.0×10^{-4}
Calcium	0.014	Iron	6.0×10^{-5}
Phosphorus	0.011	Fluorine	3.7×10^{-5}
Potassium	2.0×10^{-3}	Zinc	3.2×10^{-5}

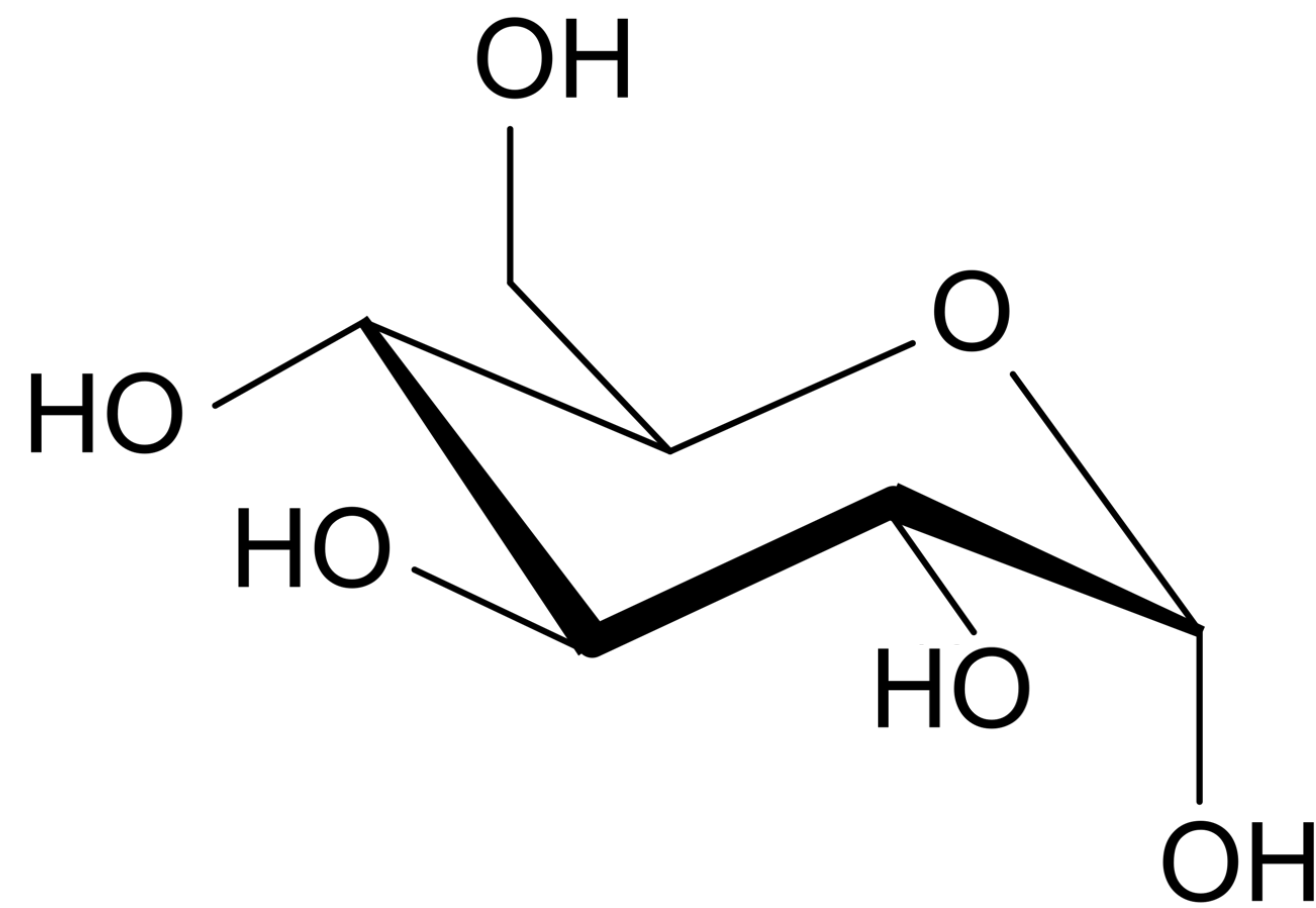


Not radioactive
 $I\sigma = 414.5 \text{ eV b}$
100% abundance
Background mass fraction
 $< 2 \times 10^{-6}$

Only 5% of total fluorine is in soft tissue.

Candidate ^{19}F

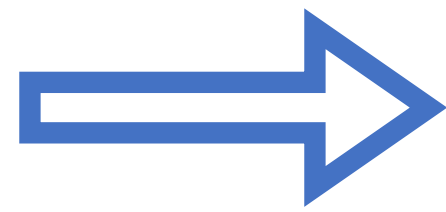
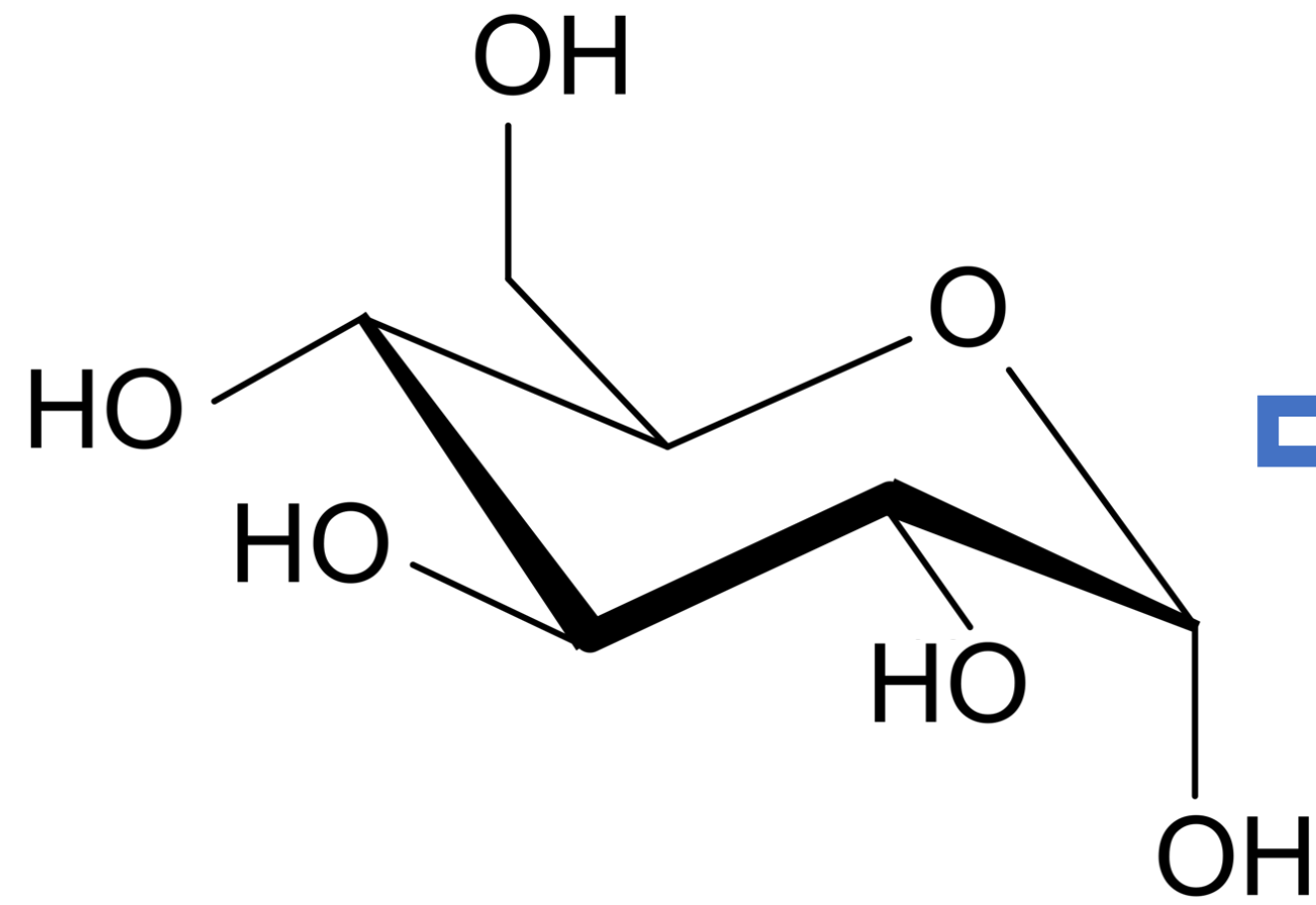
Glucose
(Sugar)



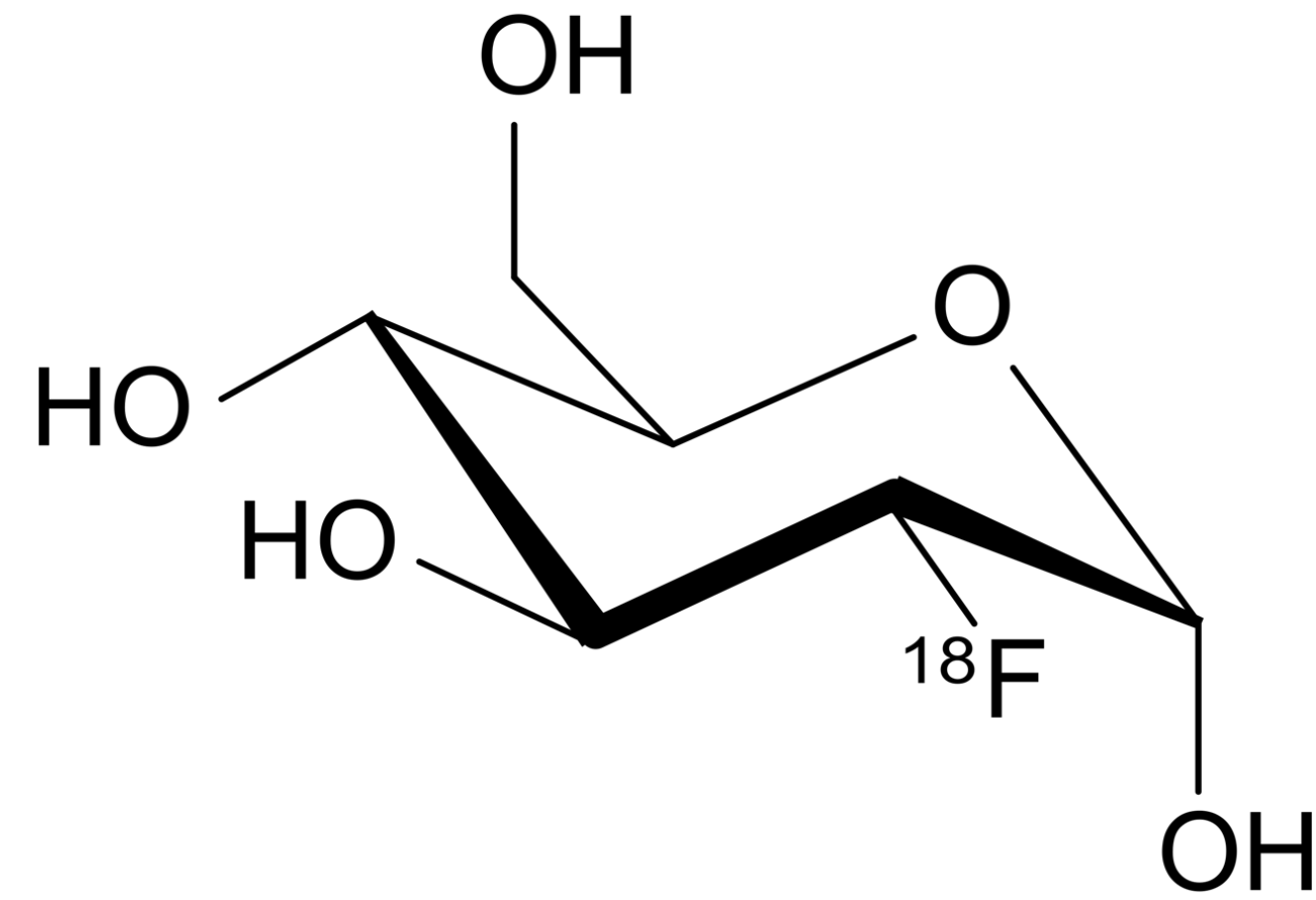
Glucose is the common molecule used for cancer PET imaging

Candidate ^{19}F

Glucose
(Sugar)



18-Fluorodeoxyglucose
(PET)

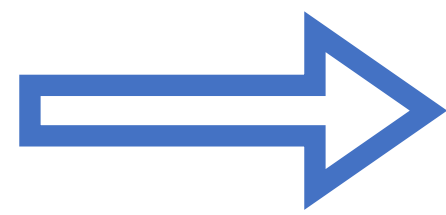
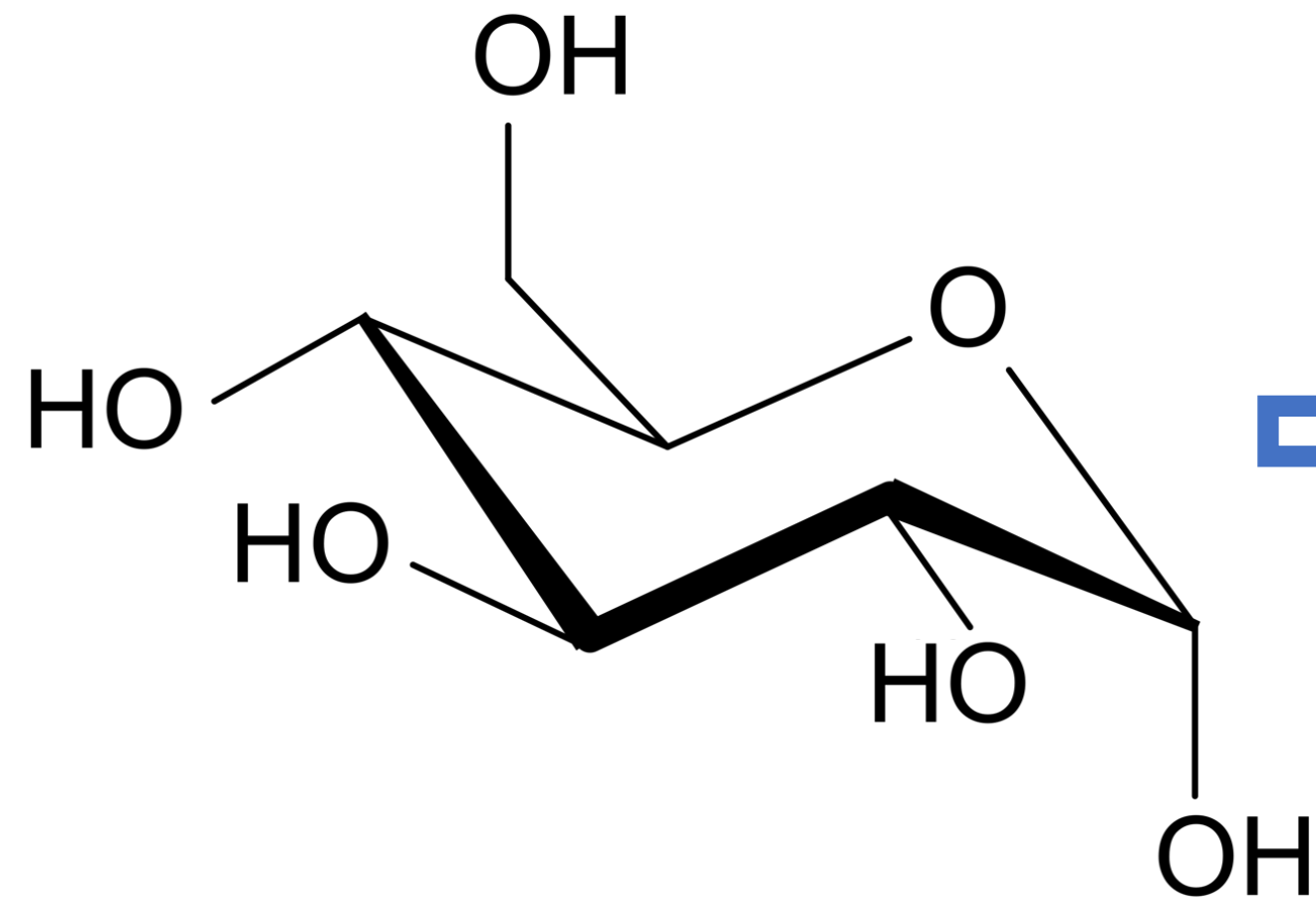


$$t_{1/2} = 110 \text{ min}$$

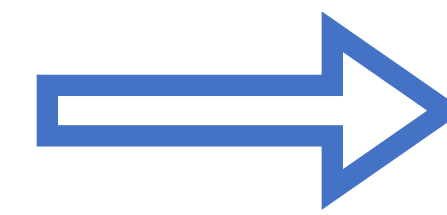
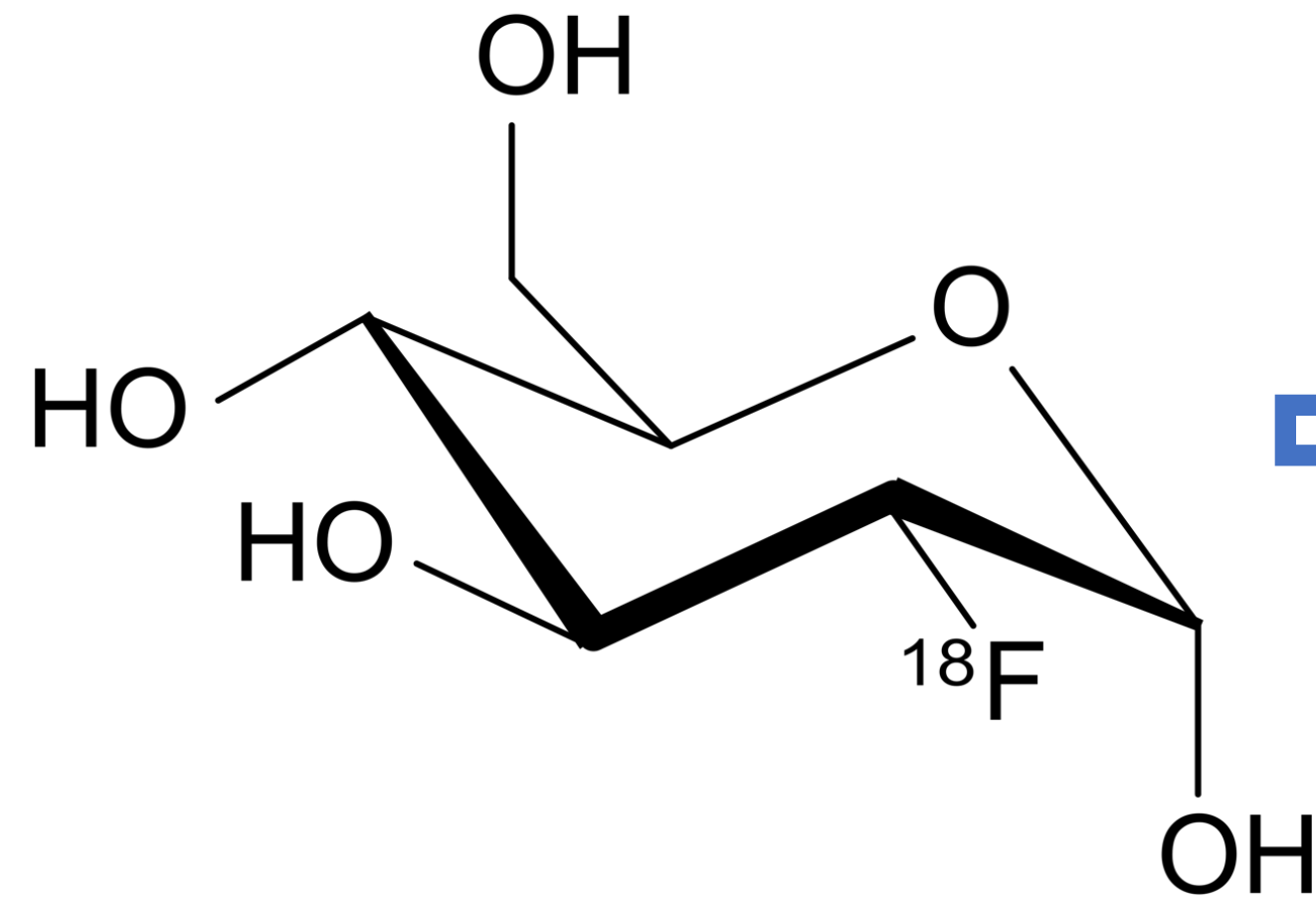
Substituting a hydroxyl group with a positron emitter

Candidate ^{19}F

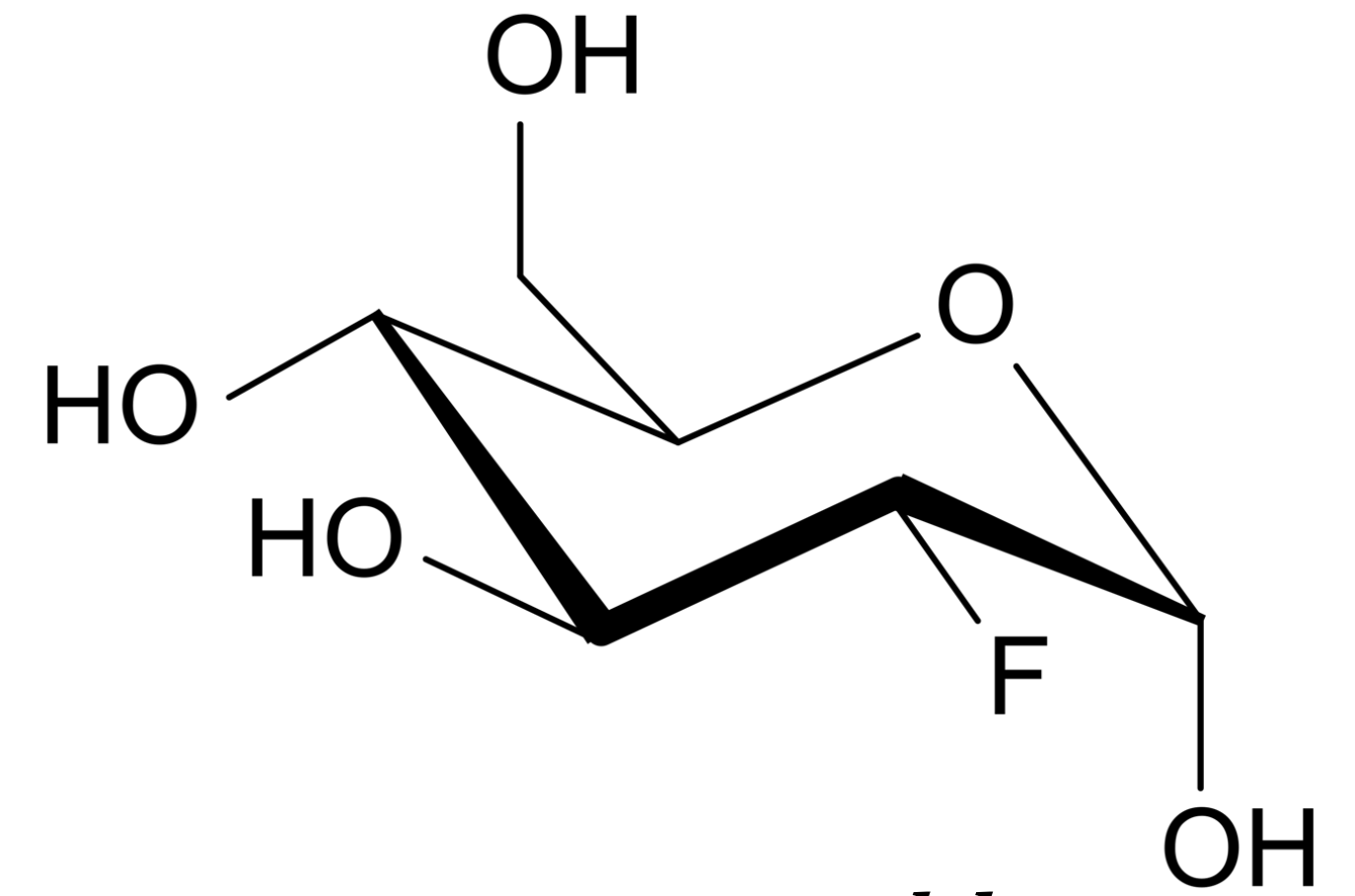
Glucose
(Sugar)



18-Fluorodeoxyglucose
(PET)



19-Fluorodeoxyglucose
(NRF - 1.5 MeV)

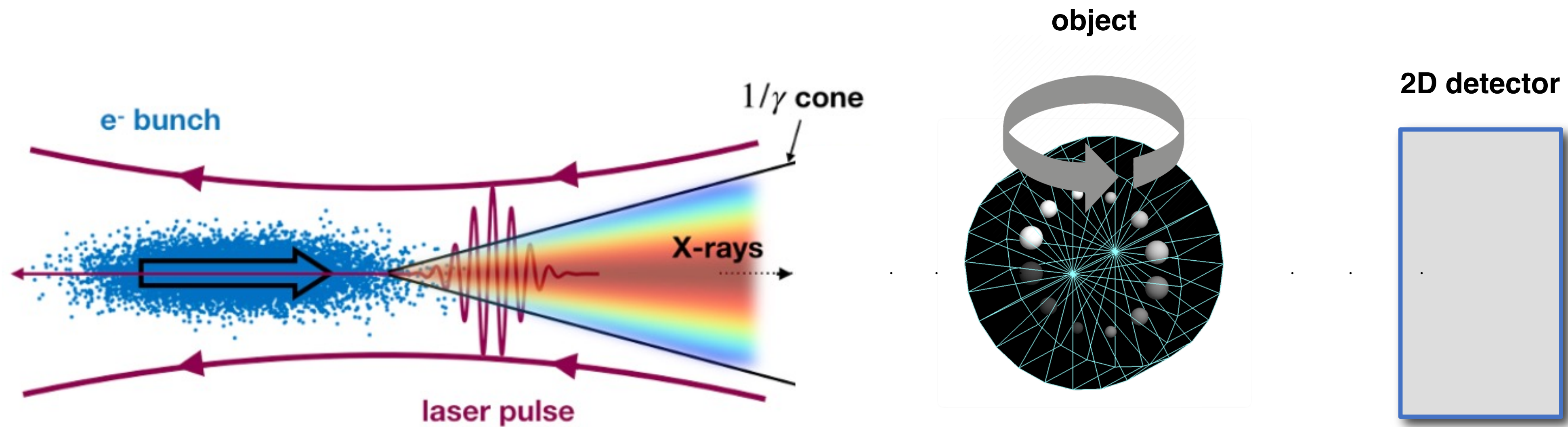


$t_{1/2} = 110 \text{ min}$

$t_{1/2} = \textit{stable}$
Abundance = 100%

Using NRF, we can image the same molecule, but with a stable isotope!

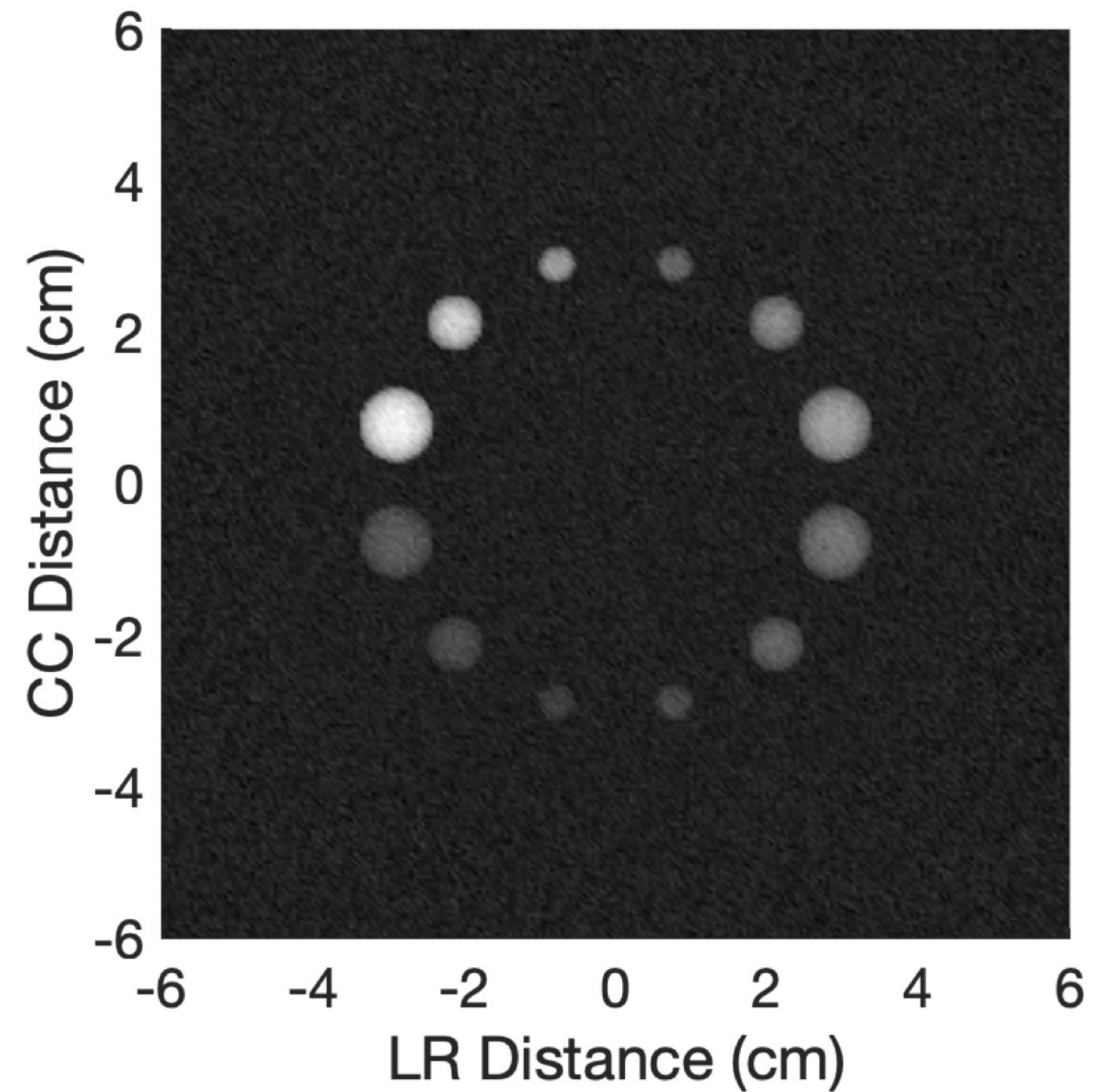
Transmission Nuclear Resonance Imaging



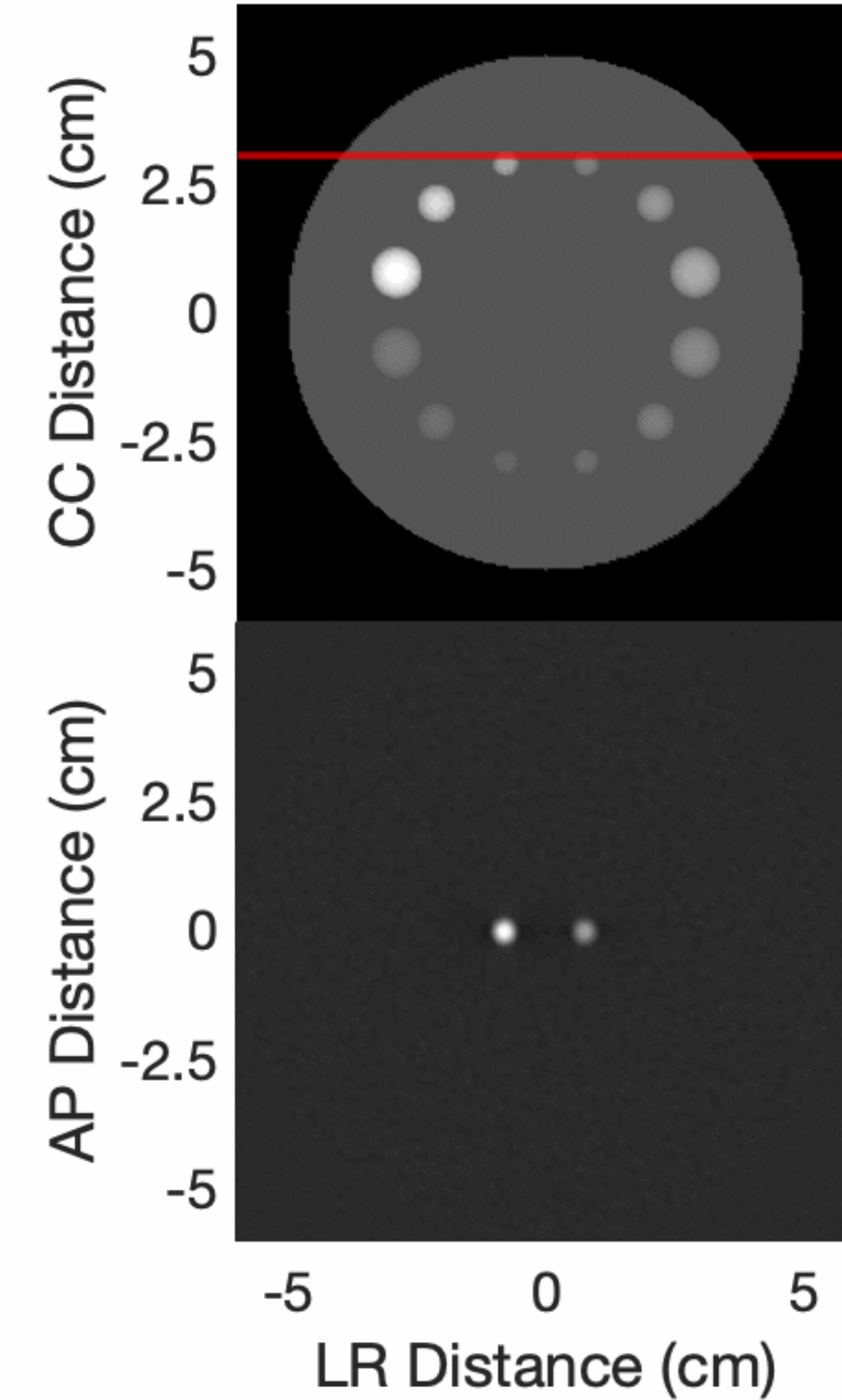
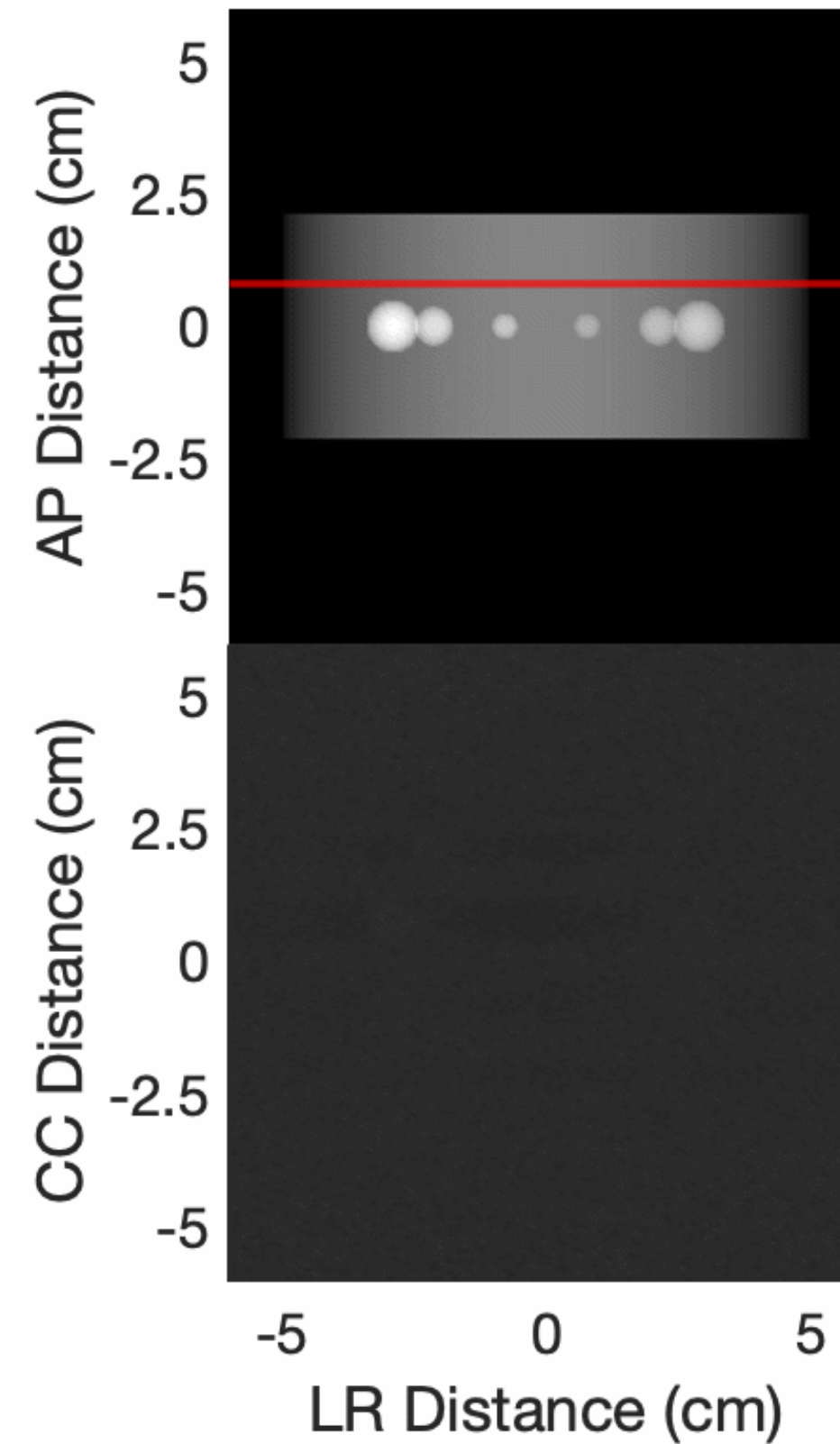
Transmission mode gives differential tomographic reconstruction capability

NR Transmission Image Reconstruction

2D Image

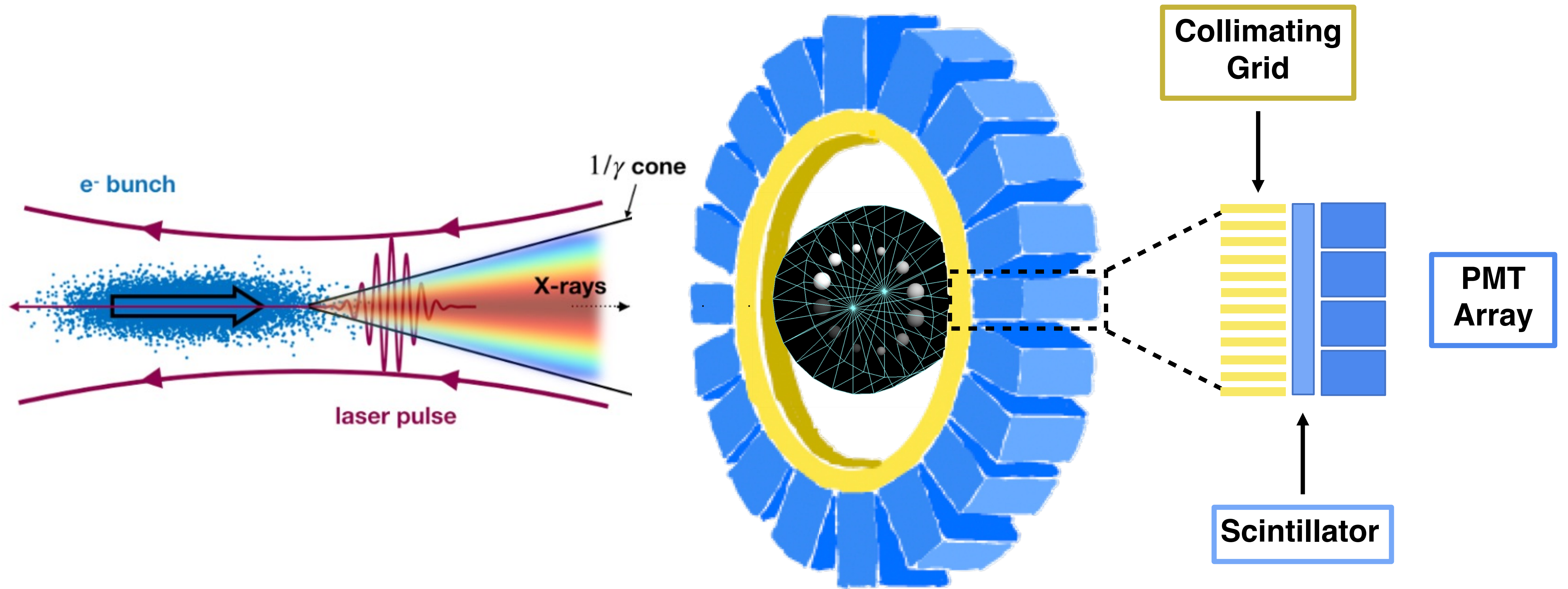


3D Reconstruction



Transmission mode gives differential tomographic reconstruction capability

Fluorescence Nuclear Resonance Imaging



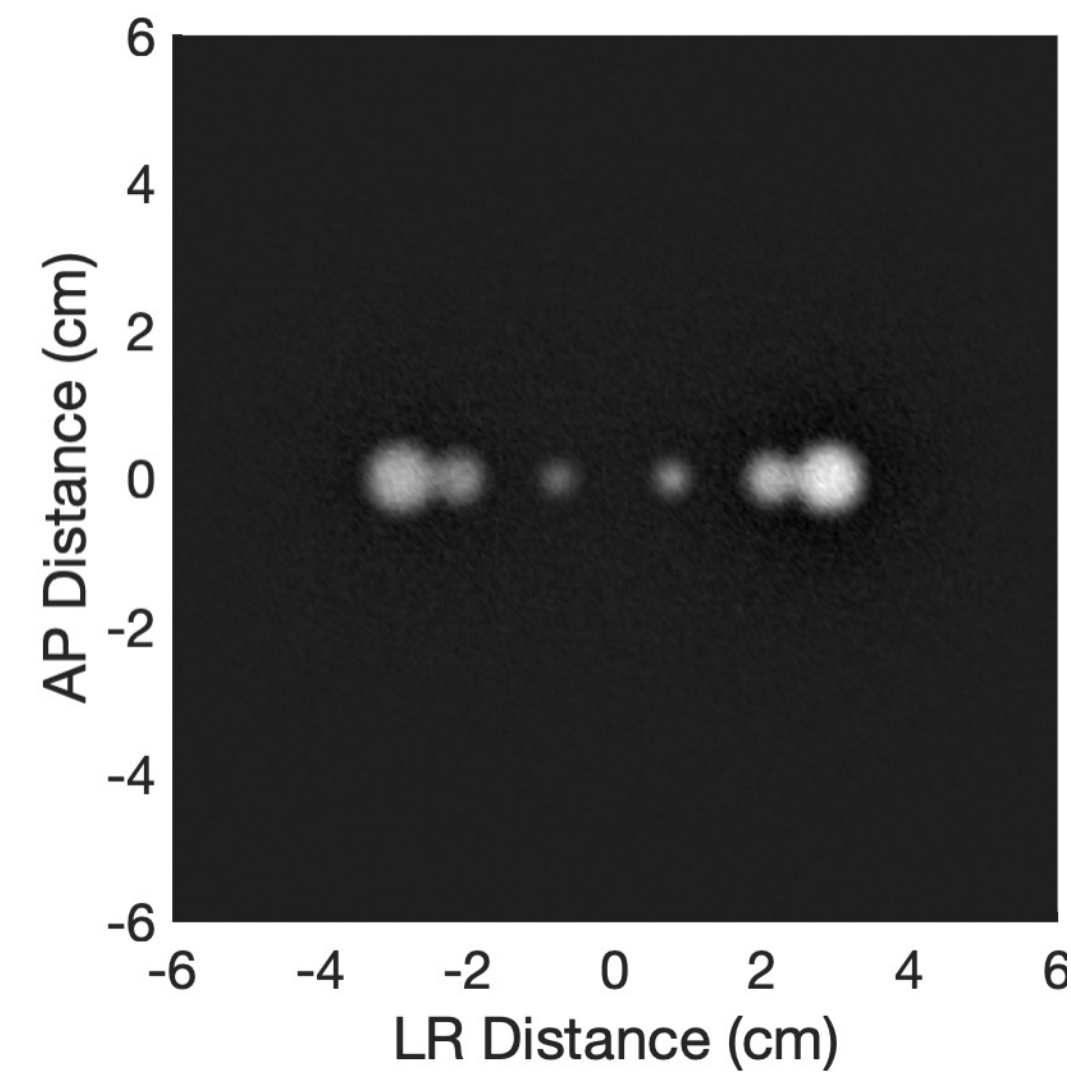
Fluorescence mode enables 3D reconstruction without rotation

NR Fluorescence Image Reconstruction

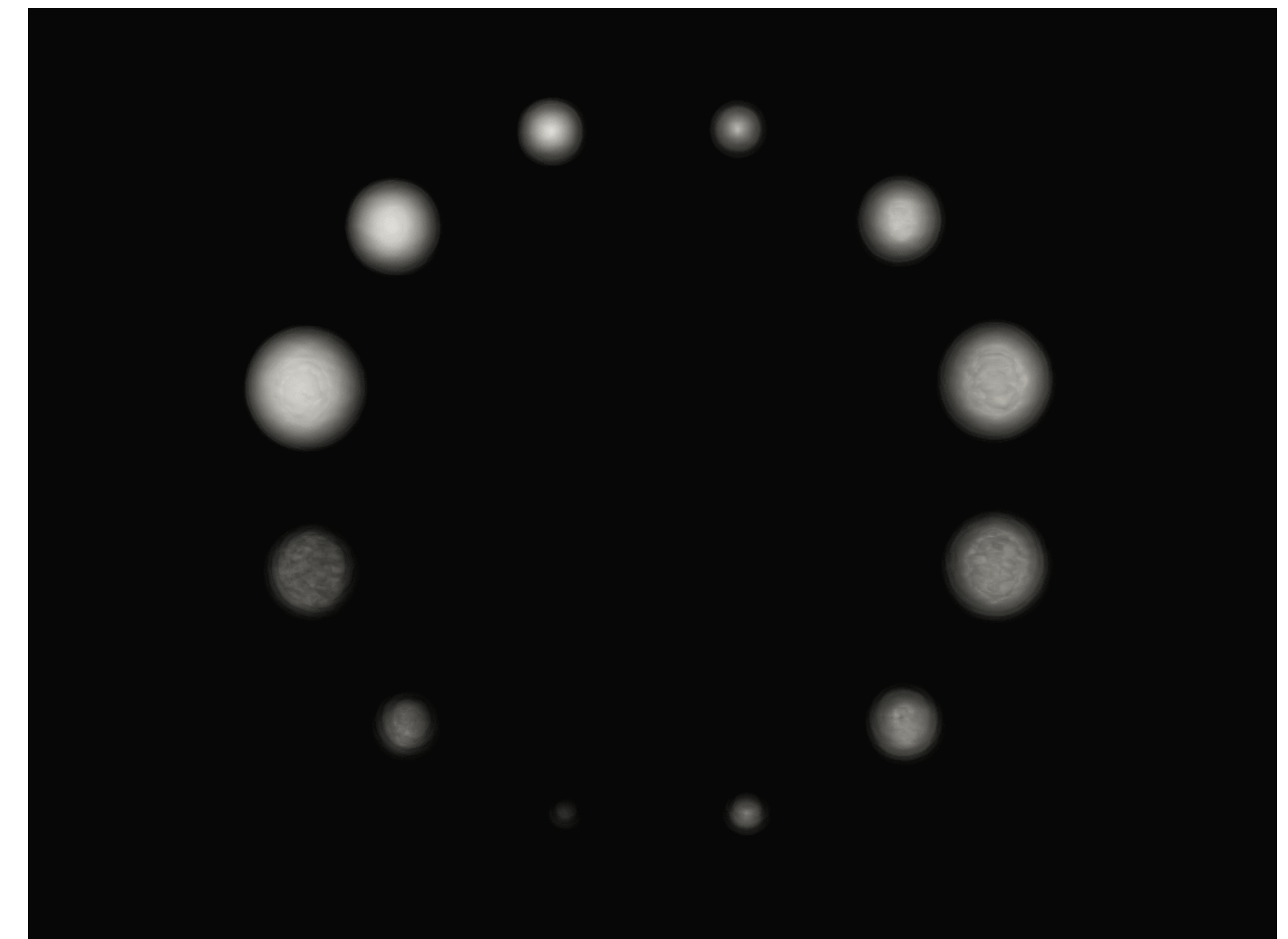
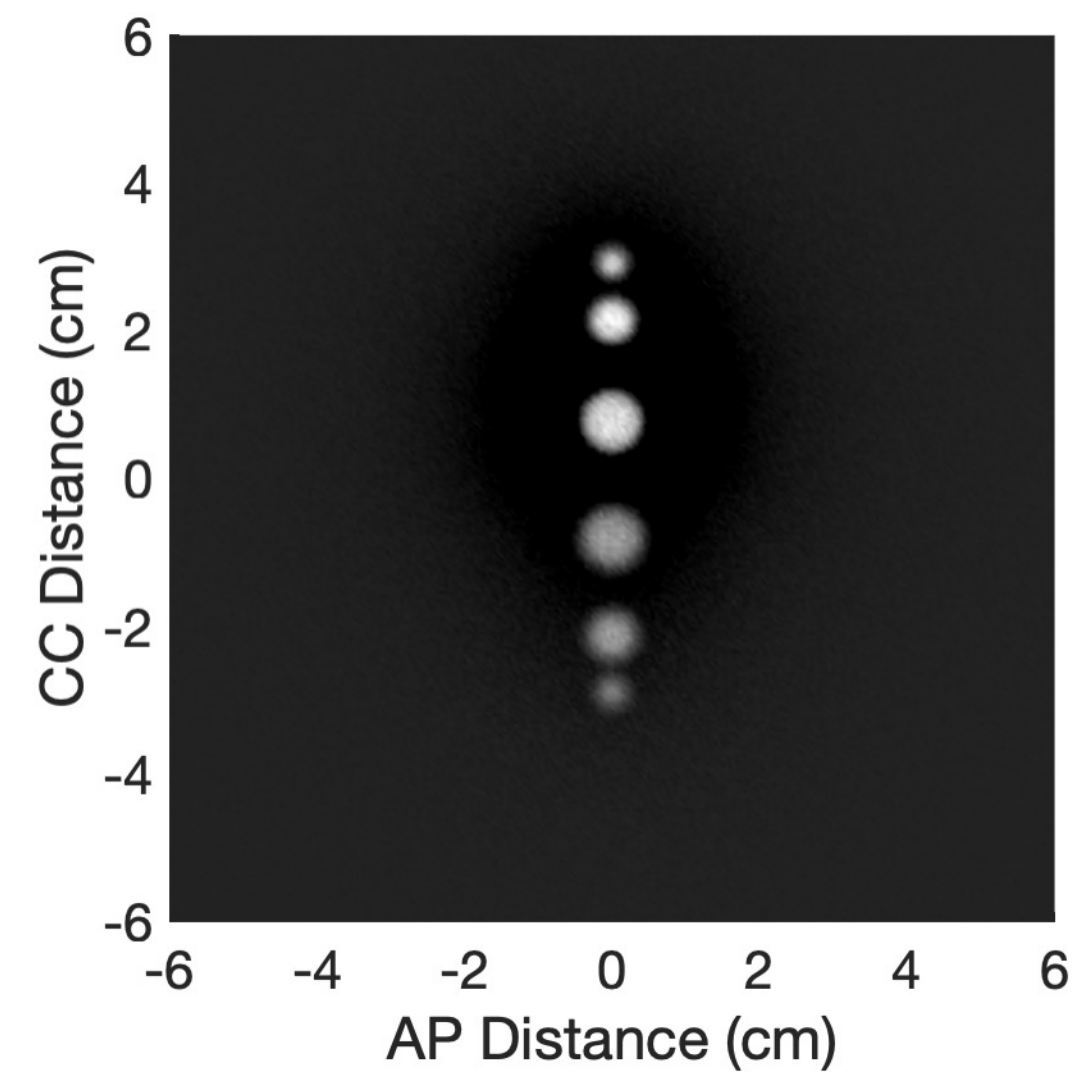
2D Images

3D Reconstruction

Top-view



Side-view



Fluorescence mode enables 3D reconstruction without rotation

NR Fluorescence Image Reconstruction

Imaging Modality	Dose (mSv)	Time
<i>PET</i>	7 - 9	~30 min
<i>PET-CT</i>	16 - 27	~30 min
<i>SPECT</i>	9 - 31	~30 min
<i>LCS-NR Transmission</i>	3.5	< 1 min
<i>LCS-NR Fluorescence</i>	9.7	seconds

Fluorescence mode enables 3D reconstruction without rotation

Conclusion

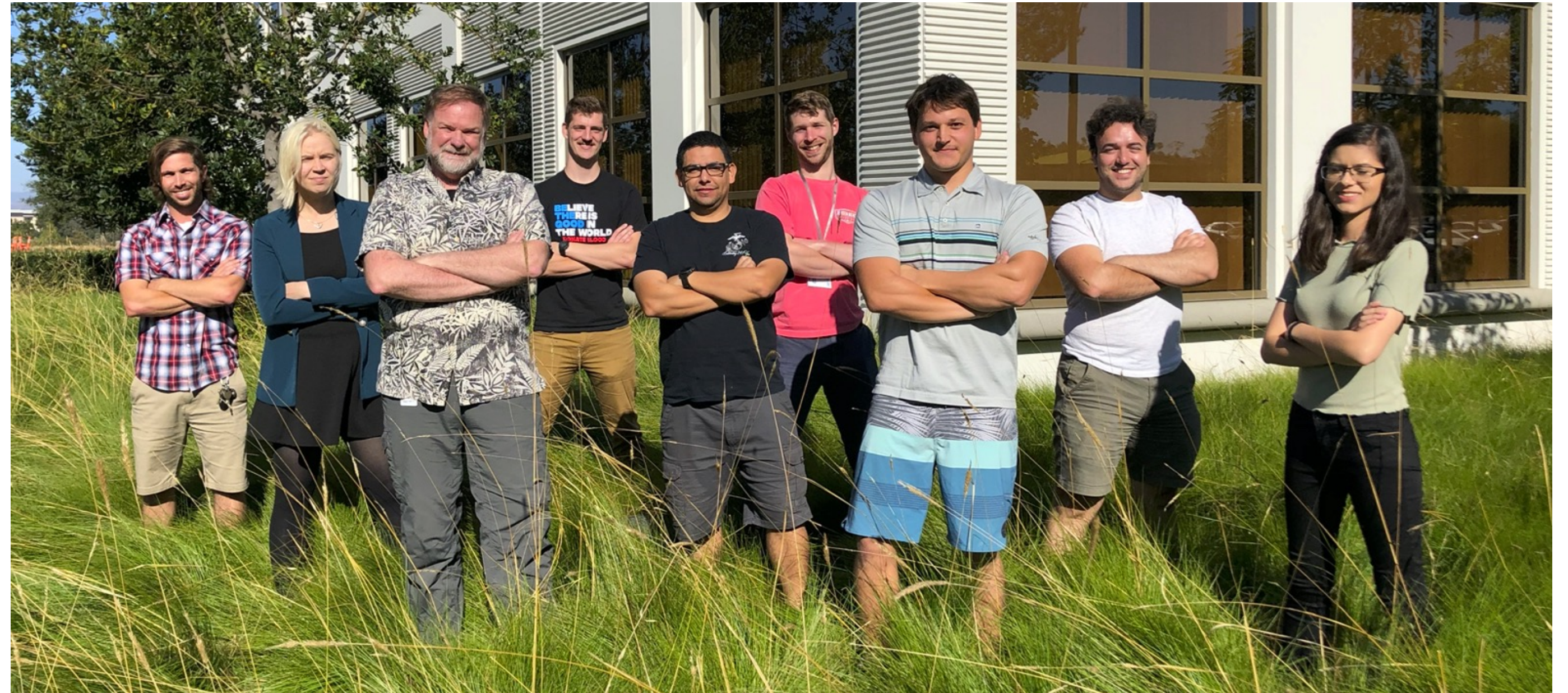
- 1) Demonstrated 2D and 3D LCS-NR medical imaging**
- 2) Bandwidth is important for signal
LCS + monochromator can achieve this**
- 3) Pool of isotopes to image
Isotope specific tags could be developed**
- 4) Dose is comparable to similar imaging modalities**

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Christine Nguyen



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Dr. Ferenc Raksi



Thank You!

Extra Viewgraphs

Source Parameters

Electron Beam Parameters		Laser Parameters	
Micro-bunch charge	25 pC	Laser micro-pulse energy	10 mJ
Pulse structure	1000 micro-bunches/pulse	Laser wavelength	354 nm
Repetition rate	400 Hz	Repetition rate	400 Hz
e ⁻ beam energy	30 – 100 MeV	Laser pulse duration	2 ps
e ⁻ beam energy spread	0.03%	Laser beam spot size	> 5 μm
RF	11.424 GHz		
e ⁻ beam emittance	0.2 mm mrad	X-ray Characteristics	
e ⁻ beam size at the interaction point / spot size (RMS)	5 μm	Total X-ray flux	> 10 ¹² ph s ⁻¹
e ⁻ bunch length	2 ps	Tunable energy range	30 keV – 3 MeV
Interaction angle	π (head-on)	X-ray spot size (RMS)	5 μm
		Minimum on-axis energy bandwidth (ΔE/E, FWHM)	10 ⁻³